



AO-Car: Transfer of Space Technology to Autonomous Driving with the Use of WORHP

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Transfer of space expertise into terrestrial applications



Transfer of space expertise into terrestrial applications



- Provide a test platform
- Increase public acceptance
- Technologies are available on earth





Research project AO-Car with terrestrial application

Autonomous and optimal navigation and control
of a vehicle in urban areas



September 2016

-

March 2018



Gefördert durch:



Bundesministerium
für Wirtschaft
und Energie

aufgrund eines Beschlusses
des Deutschen Bundestages

Research vehicle

- VW Passat GTE, Plug-in-Hybrid
- Equipped with
 - Laser scanners
 - Ultrasonic sensors
 - GNSS
 - Radar
 - Camera systems
- Control loop with a frequency of 50Hz



Goals of the research project AO-Car

Autonomous exploration of a parking lot including

- lane keeping in corridors
- turning maneuvers
- obstacle avoidance
- emergency stops
- controlled stopping
- parking



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Trajectory planning and control approach

Transfer the vehicle from state A to state B
respecting its dynamics
without any collision
and minimizing an individual optimization criterion.



Trajectory planning and control approach

Transfer the ~~vehicle~~
spacecraft
respecting its dynamics
without any collision
and minimizing an individual optimization criterion.

Optimal control problem (OCP)

$$\min_{z,u,T} J(z, u, T)$$

$$\text{s.t. } \dot{z}(t) = f(z(t), u(t)),$$

$$z(0) = z_0, \quad z(T) = z_T,$$

$$z_{\min} \leq z(t) \leq z_{\max},$$

$$u_{\min} \leq u(t) \leq u_{\max},$$

$$C(z(t), u(t), t) \leq 0 \text{ for all } t \in [0, T].$$

$$J \in \mathcal{C}^1(\mathbb{R}^n \times \mathbb{R}^m \times \mathbb{R}, \mathbb{R}),$$

$$z \in \mathcal{C}^1([0, T], \mathbb{R}^n),$$

$$u \in \mathcal{C}^0([0, T], \mathbb{R}^m),$$

$$C \in \mathcal{C}^1(\mathbb{R}^n \times \mathbb{R}^m \times \mathbb{R}, \mathbb{R}^c),$$

$$f \in \mathcal{C}^1(\mathbb{R}^n \times \mathbb{R}^m, \mathbb{R}^n).$$

Kinematic single track model

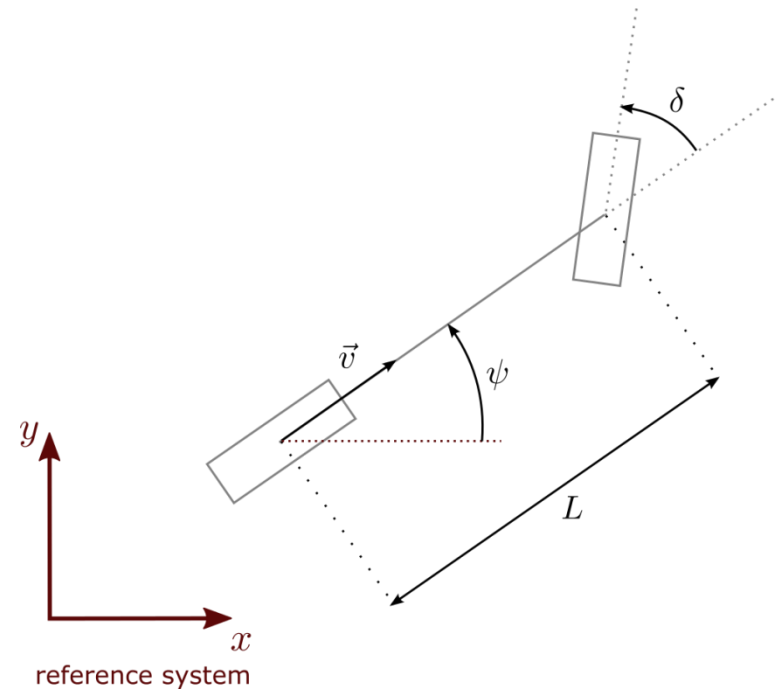
System dynamics:

$$\dot{x} = v \cdot \cos(\psi), \quad \dot{\psi} = v \cdot \frac{\tan(\delta)}{L},$$

$$\dot{y} = v \cdot \sin(\psi), \quad \dot{\delta} = \omega_{\delta},$$

$$\dot{v} = a, \quad \dot{\omega}_{\delta} = a_{\delta},$$

$$\dot{a} = j.$$



Kinematic single track model

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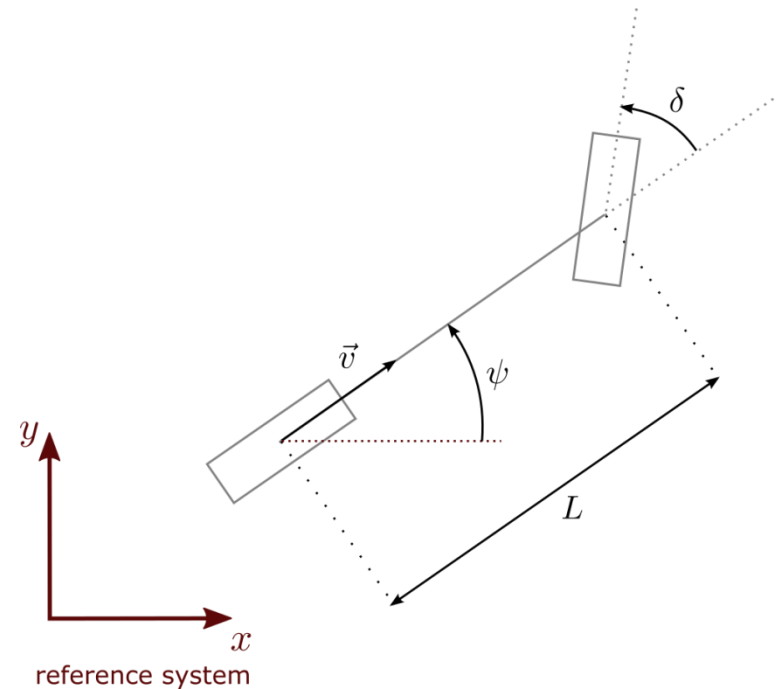
$$\dot{v} = a, \quad \dot{\omega}_{\delta} = a_{\delta},$$

$$\dot{a} = j.$$

Physical limits and limitations
due to comfort reasons:

$$v_{\min} \leq v \leq v_{\max}, \quad \delta_{\min} \leq \delta \leq \delta_{\max},$$

$$a_{\min} \leq a \leq a_{\max}, \quad \omega_{\delta_{\min}} \leq \omega_{\delta} \leq \omega_{\delta_{\max}}.$$





Optimization criteria

$$\begin{aligned}\tilde{J}(z, u, T) := & w_0 T \\ & + \int_0^T w_1 \omega_\delta^2 + w_2 a^2 + w_3 \dot{j}^2 + w_4 a_\delta^2 dt \\ & + \int_0^T w_5 (v - v_{\text{set}})^2 dt.\end{aligned}$$

Process time

Energy & comfort

Keep desired speed



Optimization criteria

$$\begin{aligned}\tilde{J}(z, u, T) := & w_0 T \\ & + \int_0^T w_1 \omega_\delta^2 + w_2 a^2 + w_3 j^2 + w_4 a_\delta^2 dt \\ & + \int_0^T w_5 (v - v_{\text{set}})^2 dt.\end{aligned}$$

Process time

Energy & comfort

Keep desired speed

Deviation from desired target state:

Case $v_T = 0 \text{ km/h}$:

$$\begin{aligned}J_T(z, u, T) := & w_6 (x(T) - x_T)^2 + w_7 (y(T) - y_T)^2 \\ & + w_8 (\psi(T) - \psi_T)^2 + w_9 (\delta(T) - \delta_T)^2.\end{aligned}$$

$$J(z, u, T) = \tilde{J}(z, u, T) + J_T(z, u, T)$$

Optimization criteria

$$\begin{aligned}\tilde{J}(z, u, T) := & w_0 T \\ & + \int_0^T w_1 \omega_\delta^2 + w_2 a^2 + w_3 j^2 + w_4 a_\delta^2 dt \\ & + \int_0^T w_5 (v - v_{\text{set}})^2 dt.\end{aligned}$$

Deviation from desired target state:

Case $v_T = 0$ km/h:

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$$J(z, u, T) = \tilde{J}(z, u, T) + J_T(z, u, T)$$

Process time

Energy & comfort

Keep desired speed

Case $v_T > 0$ km/h:

$$\begin{aligned}x(T) & \in [x_T - \varepsilon_x, x_T + \varepsilon_x], \\ y(T) & \in [y_T - \varepsilon_y, y_T + \varepsilon_y], \\ \psi(T) & \in [\psi_T - \varepsilon_\psi, \psi_T + \varepsilon_\psi], \\ \delta(T) & \in [\delta_T - \varepsilon_\delta, \delta_T + \varepsilon_\delta],\end{aligned}$$

$$\varepsilon_x, \varepsilon_y, \varepsilon_\psi, \varepsilon_\delta > 0.$$

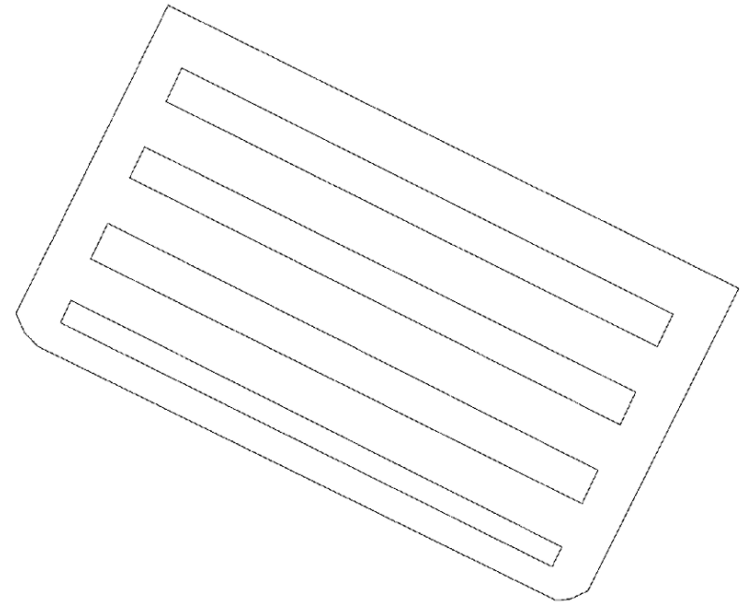
$$J(z, u, T) = \tilde{J}(z, u, T)$$

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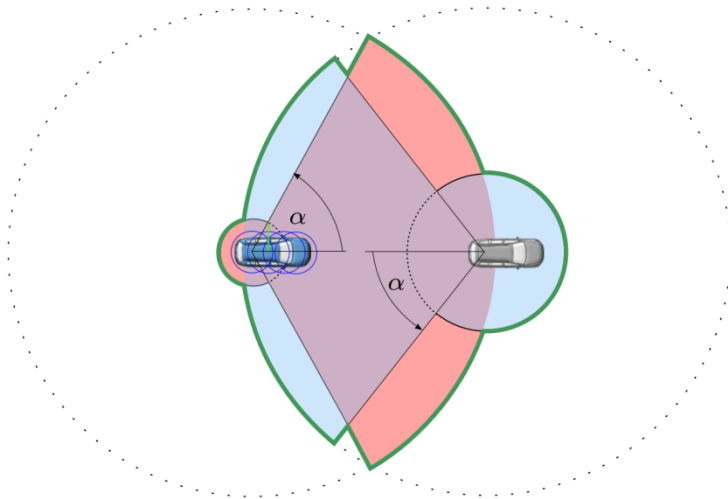
Predefined restrictions of the parking lot



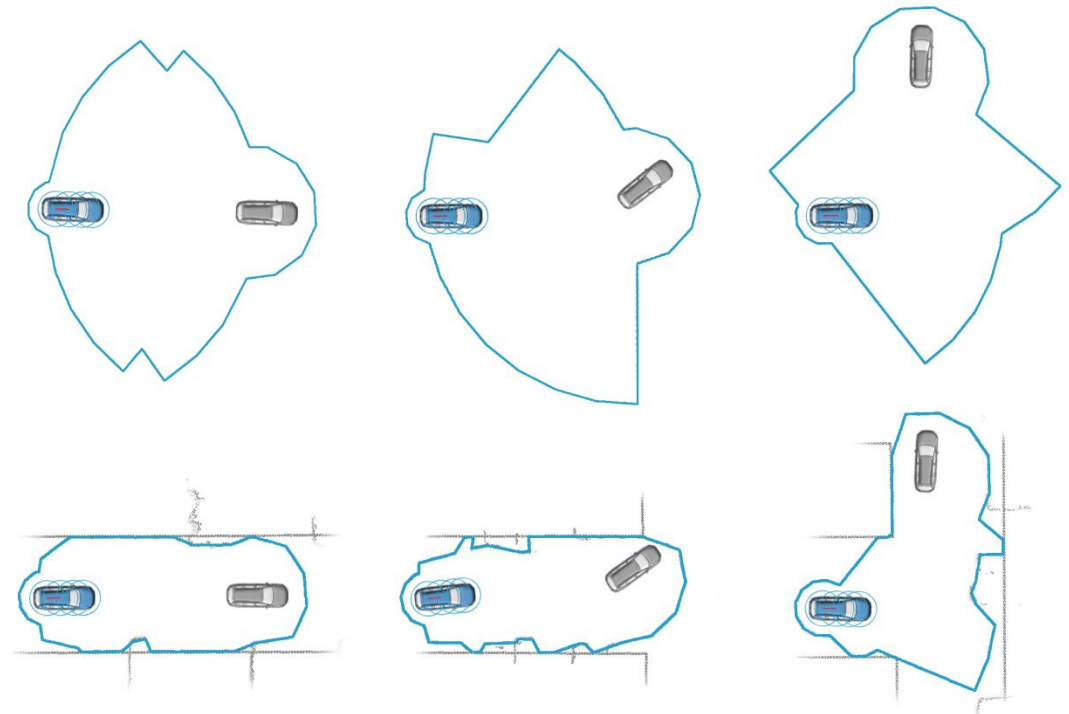
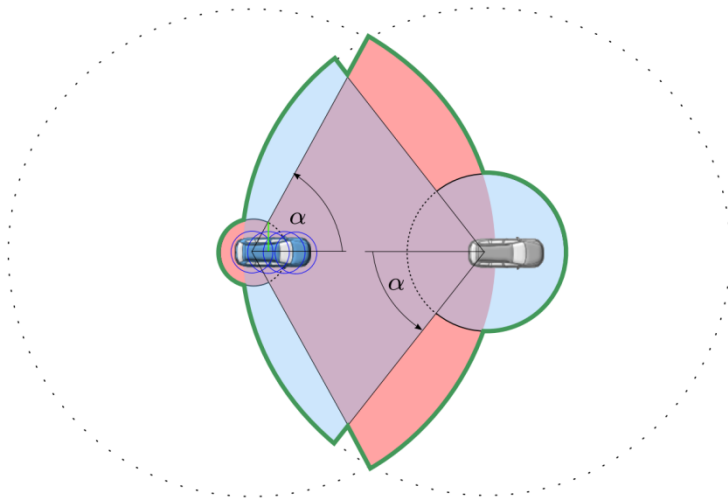
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Construction of feasibility polygons

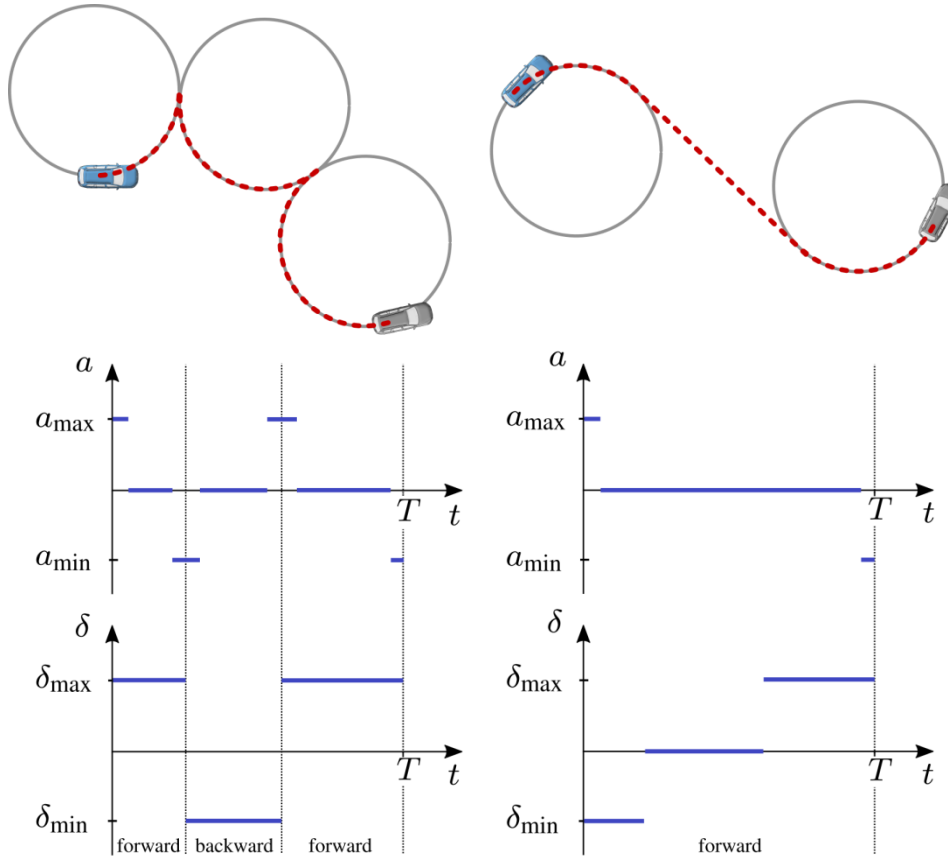


Construction of feasibility polygons



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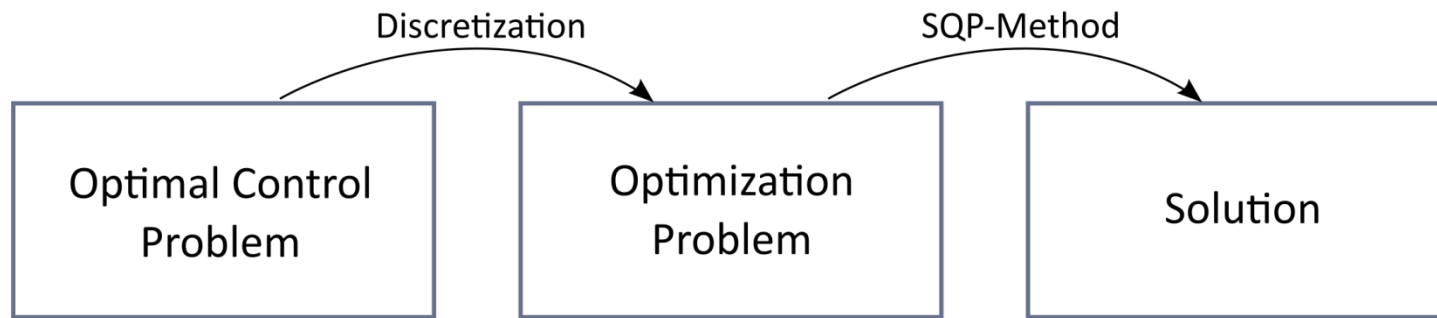
Initial guess based on Reeds-Shepp paths



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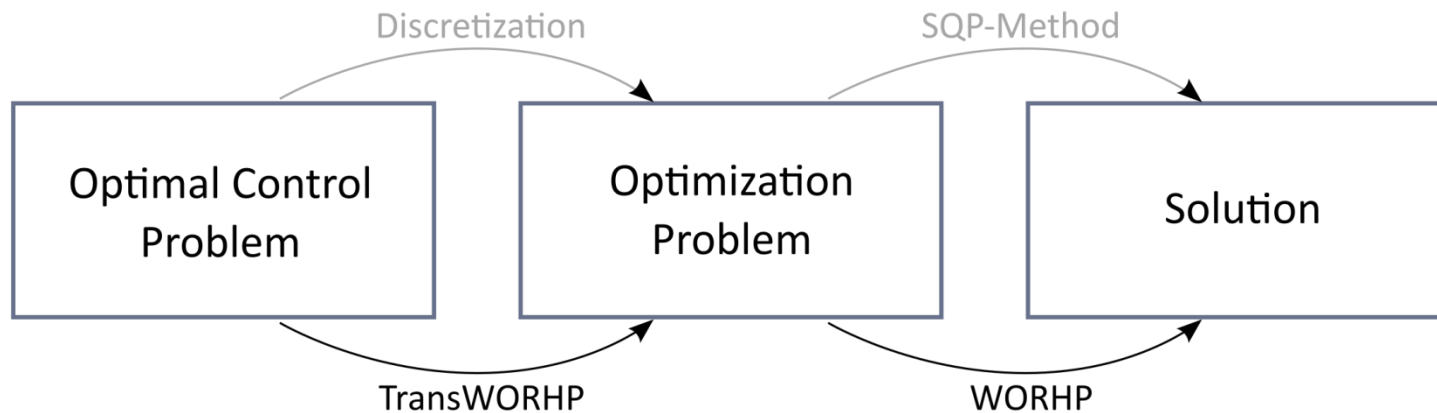


Solution of the OCP



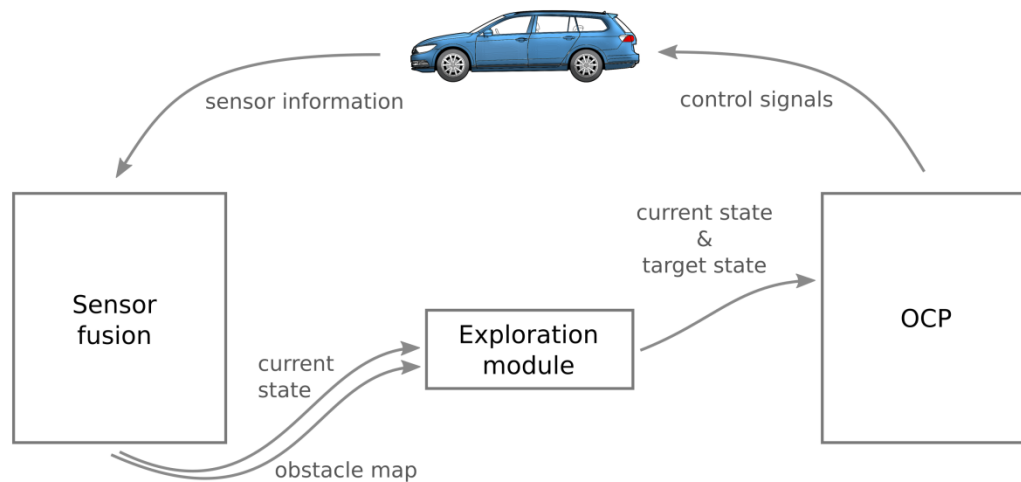


Solution of the OCP



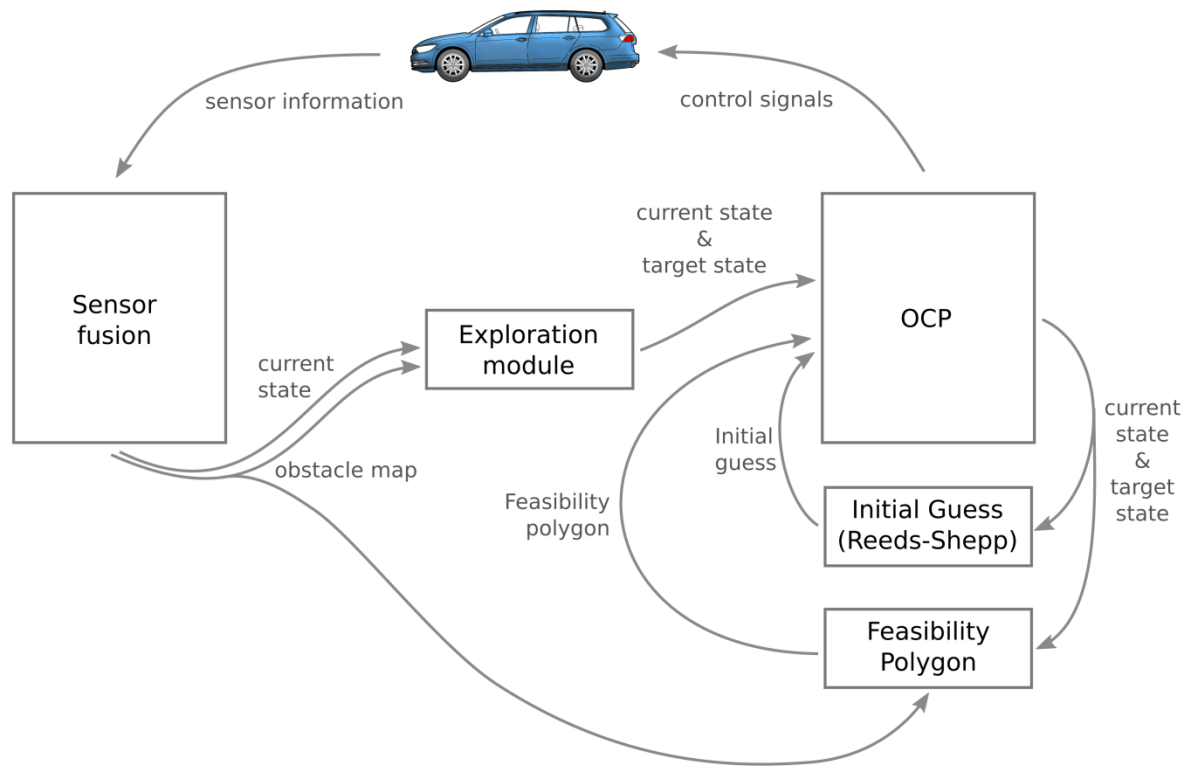
Control loop (simplified)

Nonlinear model predictive control



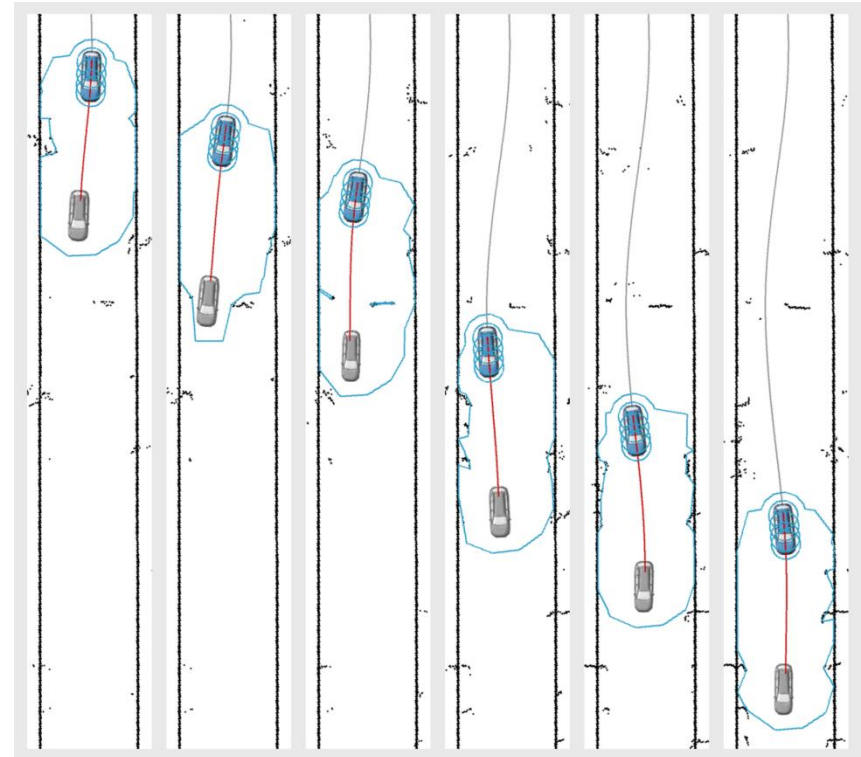
Control loop (simplified)

Nonlinear model predictive control

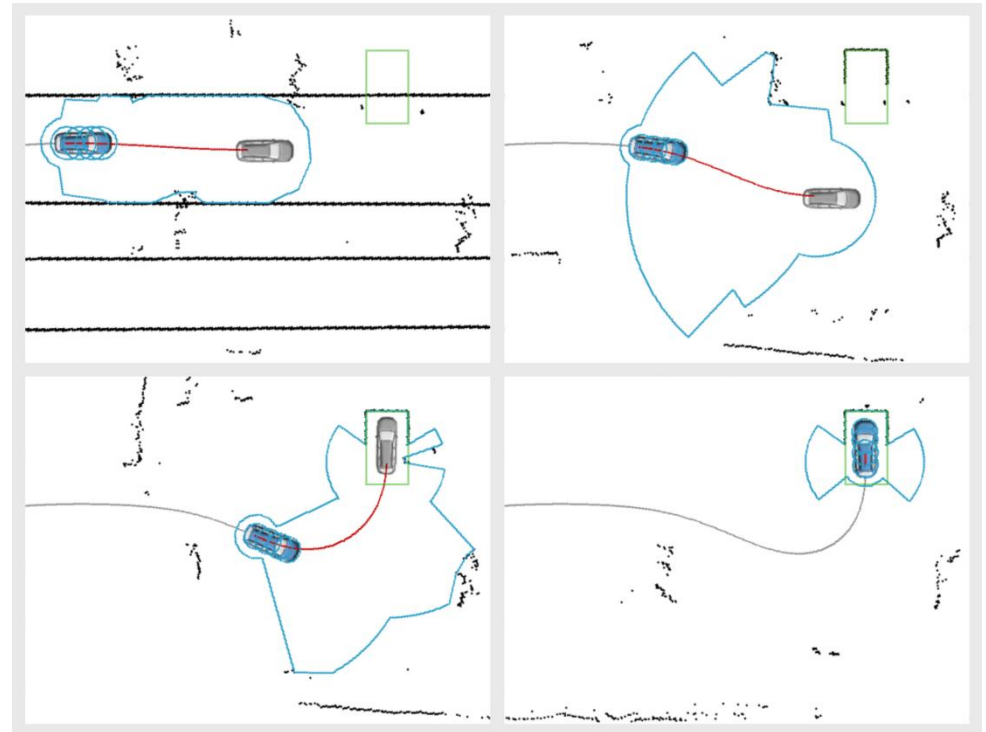


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Experiments – Narrowing of the lane



Experiments – Parking



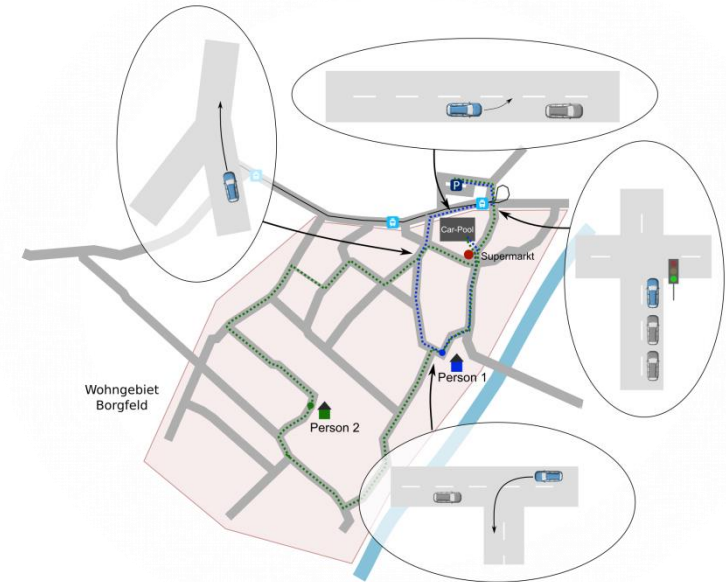
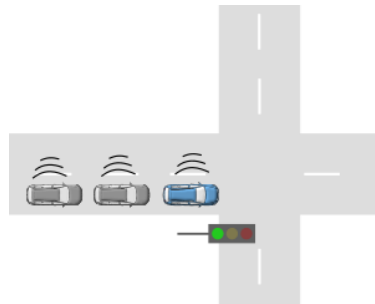
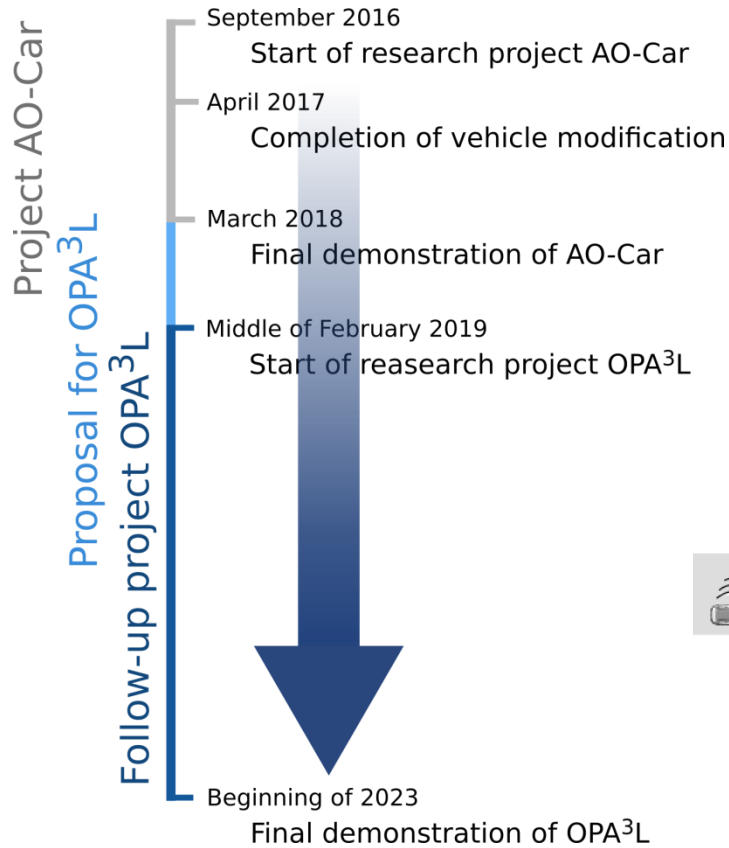


Impressions



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Outlook and future research



Vehicle on demand concept
and cooperative maneuvers



Thank you very much
for your attention!



Performance

	Exploration	Narrowing	Parking
Mean computing time			
optimal	33 ms	35 ms	70 ms
non-optimal	104 ms	251 ms	-
total	33 ms	41 ms	70 ms
Standard deviation			
optimal	11 ms	19 ms	49 ms
non-optimal	121 ms	169 ms	-
total	17 ms	49 ms	49 ms
# Computations	2 486	750	480
# Optimal	2 462	725	468
# Not optimal (feasible)	18	9	12
# Not optimal (unacc.)	6	16	0
Rate of unacc. solutions	0.24 %	2.13 %	0 %
# Relax	2	4	12