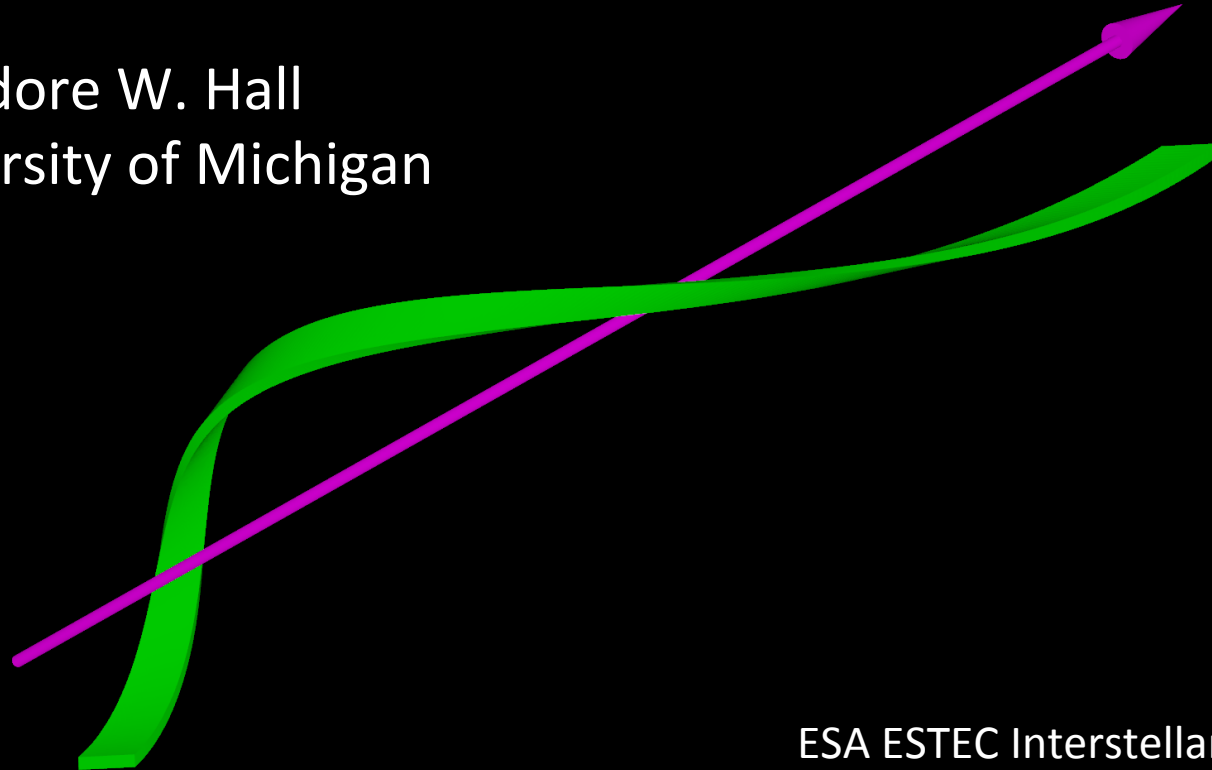


Artificial Gravity in Interstellar Travel

Theodore W. Hall
University of Michigan



Effects of Chronic Weightlessness

- Fluid redistribution
- Fluid loss
- Electrolyte imbalances
- Cardiovascular changes
- Red blood cell loss
- Muscle damage
- Bone damage
- Eye damage
- Hypercalcemia
- Immune suppression.

... and others ... ?

Alternatives to Weight for Preserving Health?


- Suspended animation
- J. D. Bernal,
“three-dimensional, gravitationless way of living”

Weight & Gravity, in Theory ...

Fundamental Forces (Interactions):

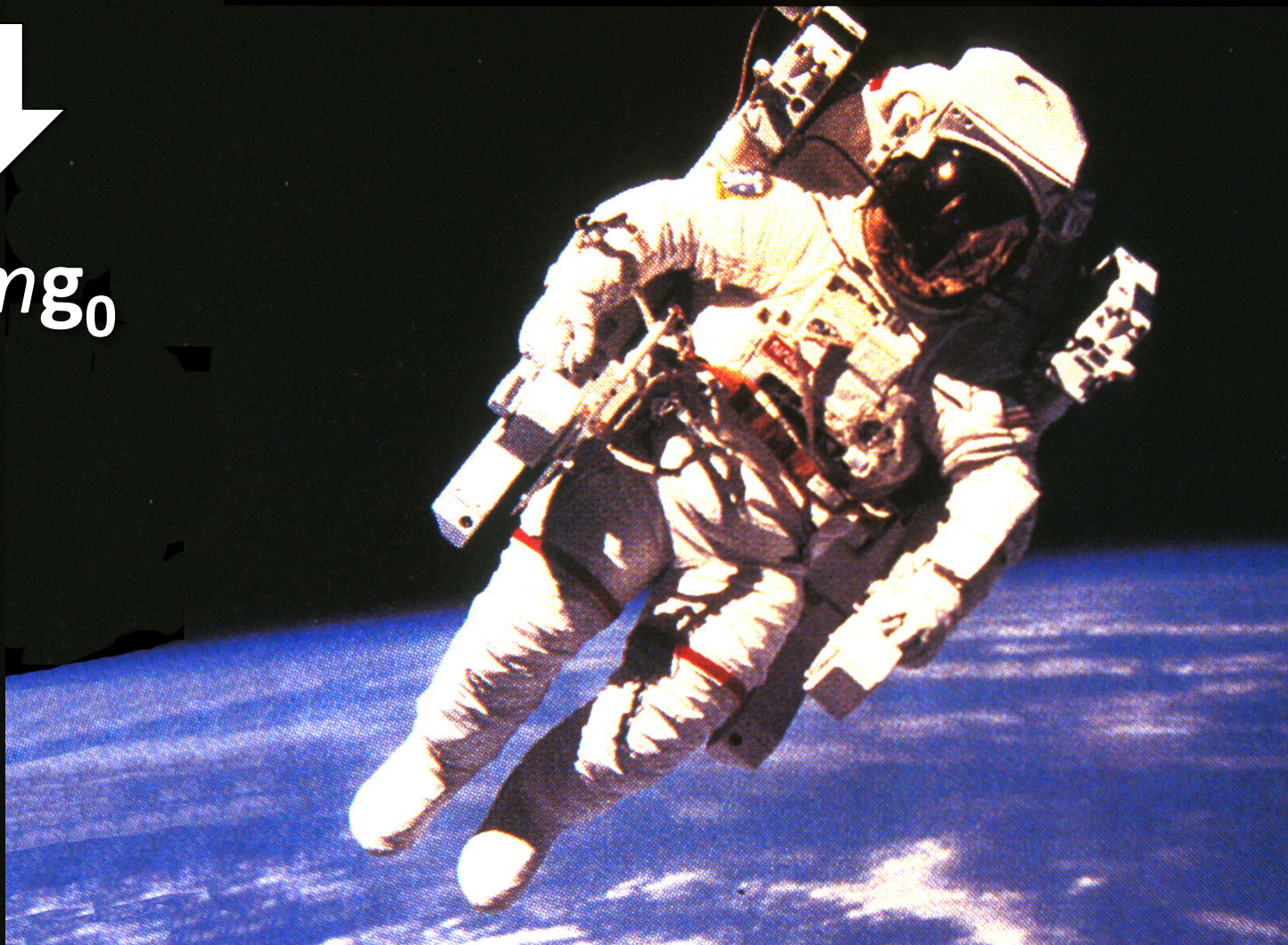
Standard Model of Particle Physics


1. Strong Nuclear (gluons)
2. Weak Nuclear (W & Z bosons)
3. Electromagnetic (photons)
4. Gravitational (?)

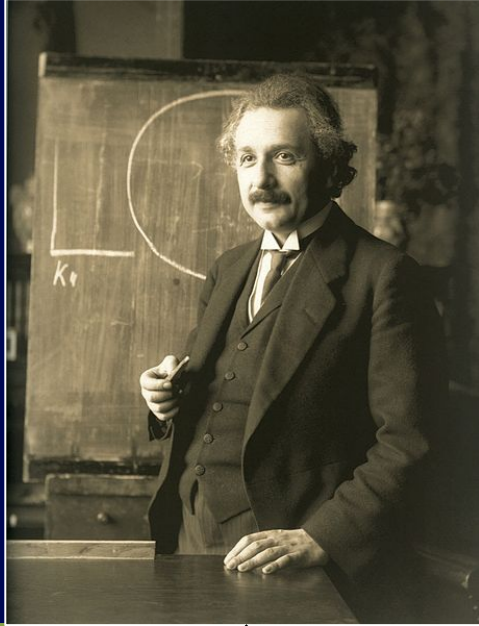
$$F_g = mA$$



$$F_g = 89\% mg_0$$

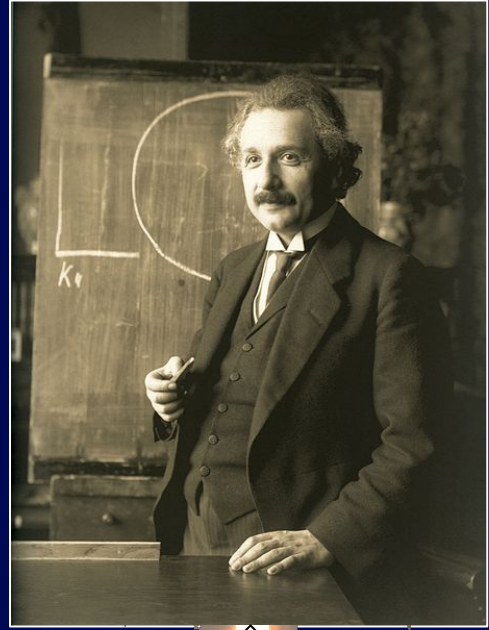
and yet he's
weightless.

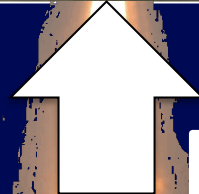


$$F_g = mA$$


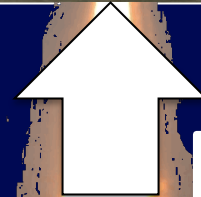
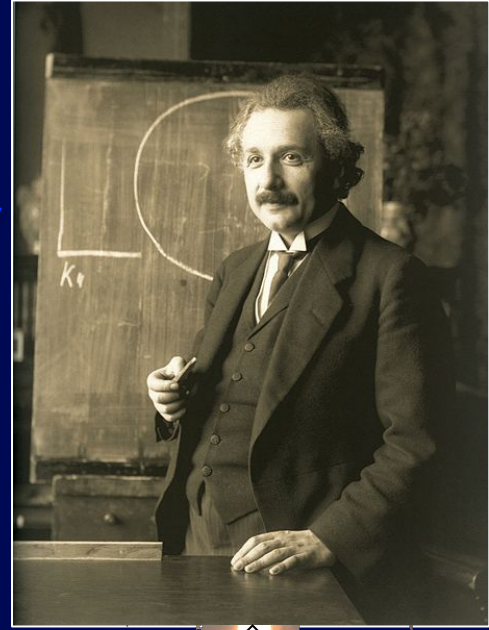



$$F_e = mA$$




$$F_e = mA$$

“a gravitational field exists for the man in the chest, despite the fact that there was no such field for the coordinate system first chosen”
– *Einstein*



$$F_e = mA$$

Gravity is Irrelevant:

It's neither necessary nor sufficient
to preserve human health.

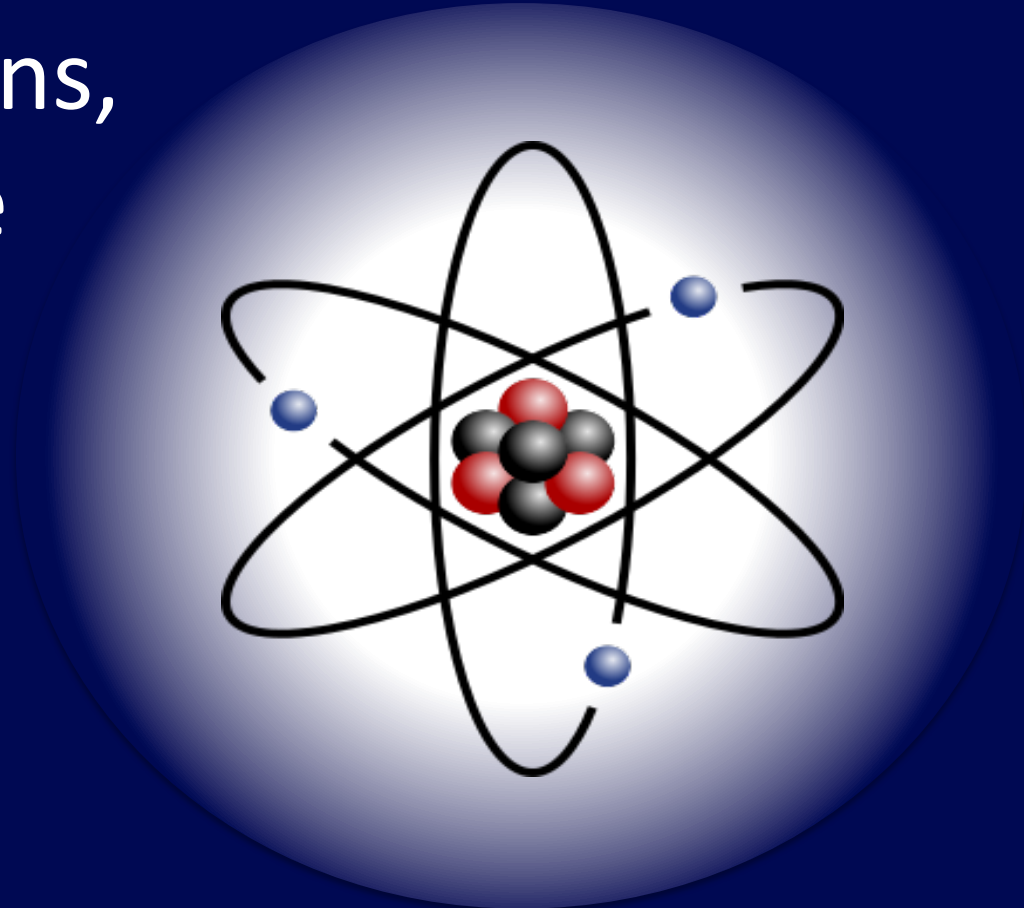
planetary

mostly

Gravity is Irrelevant:

It's neither necessary nor sufficient
to preserve human health.

All mechanical and
chemical interactions,
including *bio*—, are
Electromagnetic.



If weightlessness
is the problem,

then mechanical acceleration
is the solution.

If weightlessness
is the problem,

maybe
then mechanical acceleration
is the solution.

Linear Acceleration:

± 1 g to Proxima Centauri (4.244 ly):

Naive, non-relativistic calculations:

$$t_{total} = 4.055 \text{ yr}$$

$$V_{max} = 2.093 \text{ c}$$

→ A_1

→ A_2

→ A_3

→ V_1

→ V_2

→ V_3

Space travel calculator [N. Geffen]

| | | | |
|-----------------------------------------------|-------------------------------------------------|---------------------------------------------|----|
| Distance | <input type="text" value="4.244"/> | <input type="text" value="light-years"/> | ?+ |
| Acceleration | <input type="text" value="9.80665"/> | <input type="text" value="m/s^2"/> | ?+ |
| Maximum velocity | <input type="text" value="0.9496121347735087"/> | <input type="text" value="speed of light"/> | ?+ |
| Observer time elapsed during journey | <input type="text" value="5.869961089378631"/> | <input type="text" value="years"/> | ?+ |
| Traveler time elapsed during journey | <input type="text" value="3.5412690887271987"/> | <input type="text" value="years"/> | ?+ |
| Payload (spacecraft mass without fuel) | <input type="text" value="25000"/> | <input type="text" value="kilograms"/> | ?+ |
| Fuel conversion rate | <input type="text" value="0.008"/> | <input type="text" value="kg x m x m"/> | ?+ |
| Fuel mass | <input type="text" value="117787801.00439891"/> | <input type="text" value="kg"/> | ?+ |
| Length of spacecraft at start of journey | <input type="text" value="1"/> | <input type="text" value="meters"/> | ?+ |
| Shortest length of spacecraft for observer | <input type="text" value="0.3134274931956345"/> | <input type="text" value="meters"/> | ?+ |
| <input type="button" value="Calculate"/> | | <input type="button" value="Clear"/> | |

Linear Acceleration:

± 1 g to Proxima Centauri (4.244 ly):

Relativistic calculations:

$$t_{total_craft} = 3.541 \text{ yr}$$

$$t_{total_earth} = 5.870 \text{ yr}$$

$$V_{max_earth} = 0.9496 c$$

→ A_1

→ A_2

→ A_3

→ V_1

→ V_2

→ V_3

Linear Acceleration:

Not sustainable:

$$P = m\mathbf{A} \cdot \mathbf{V} \rightarrow \infty$$

→ \mathbf{A}_1

→ \mathbf{A}_2

→ \mathbf{A}_3

→ \mathbf{V}_1

→ \mathbf{V}_2

→ \mathbf{V}_3

Linear Acceleration:

$\pm a \ll 1 \text{ g}$ to Proxima Centauri (4.244 ly):

| A_{craft} | t_{total_craft} | V_{max_earth} |
|-------------------|--------------------|------------------|
| 0.001000 g | 128.2 yr | 0.06608 c |
| 0.001643 g | 100.0 yr | 0.08461 c |
| 0.000572 g | 169.6 yr | 0.05000 c |

—————→ A_1

—————→ A_2

—————→ A_3

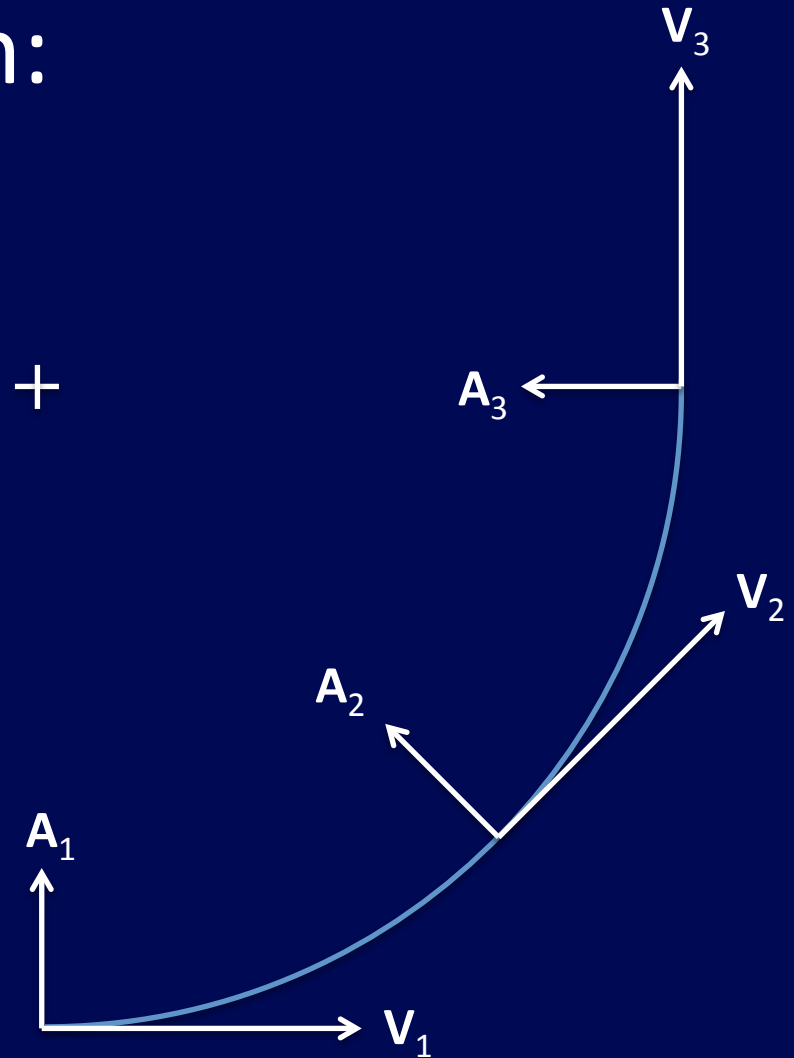
—————→ V_1

—————→ V_2

—————→ V_3

Centripetal Acceleration: Sustainable

$$P = m\mathbf{A} \cdot \mathbf{V} = 0$$



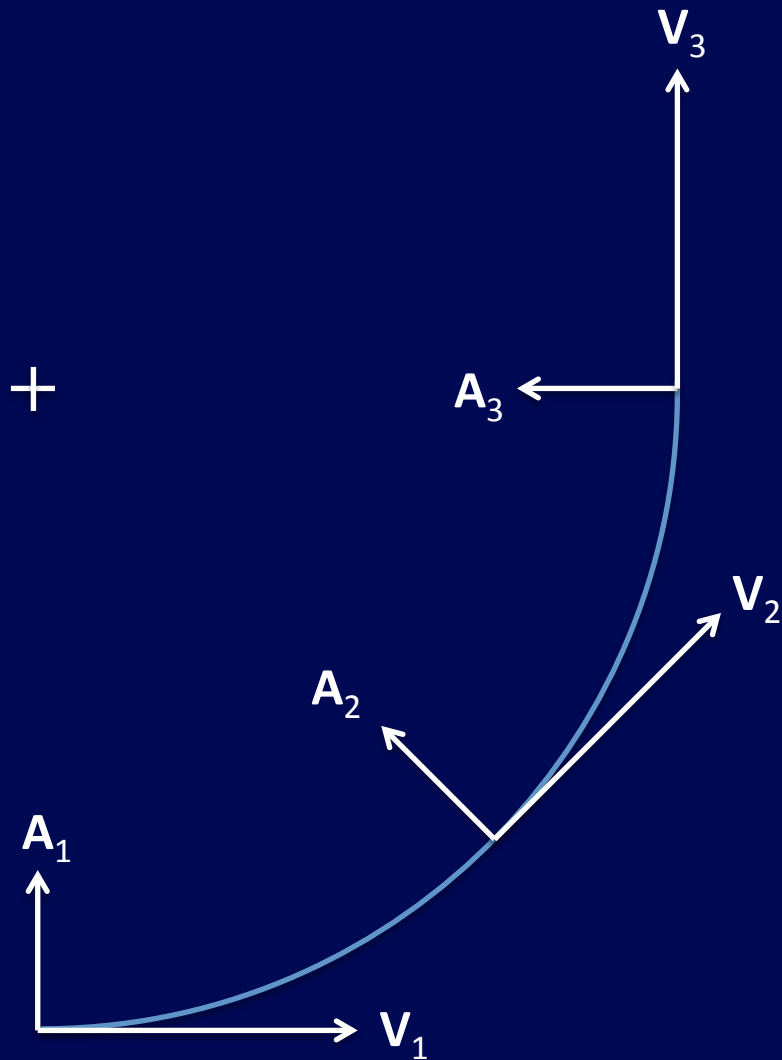
$$\mathbf{V}_{tan} = \boldsymbol{\Omega} \times \mathbf{R}$$

$$\mathbf{A}_{cent} = \boldsymbol{\Omega} \times \mathbf{V}$$

$$= \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{R})$$

$$\mathbf{A}_{Cor} = 2\boldsymbol{\Omega} \times \mathbf{v}_{rel}$$

$$\frac{A_{Cor}}{A_{cent}} = 2 \frac{v_{rel}}{V_{tan}}$$



SpinCalc artificial-gravity calculator

Radius (R)



9.439403162878252

meters

$$R \propto A/\Omega^2$$

Angular Velocity (Ω)



6

rotations/minute

input

Tangential Velocity (V)



5.930951926154115

meters/second

$$V \propto A/\Omega$$

Centripetal Acceleration (A)



0.38

g

input

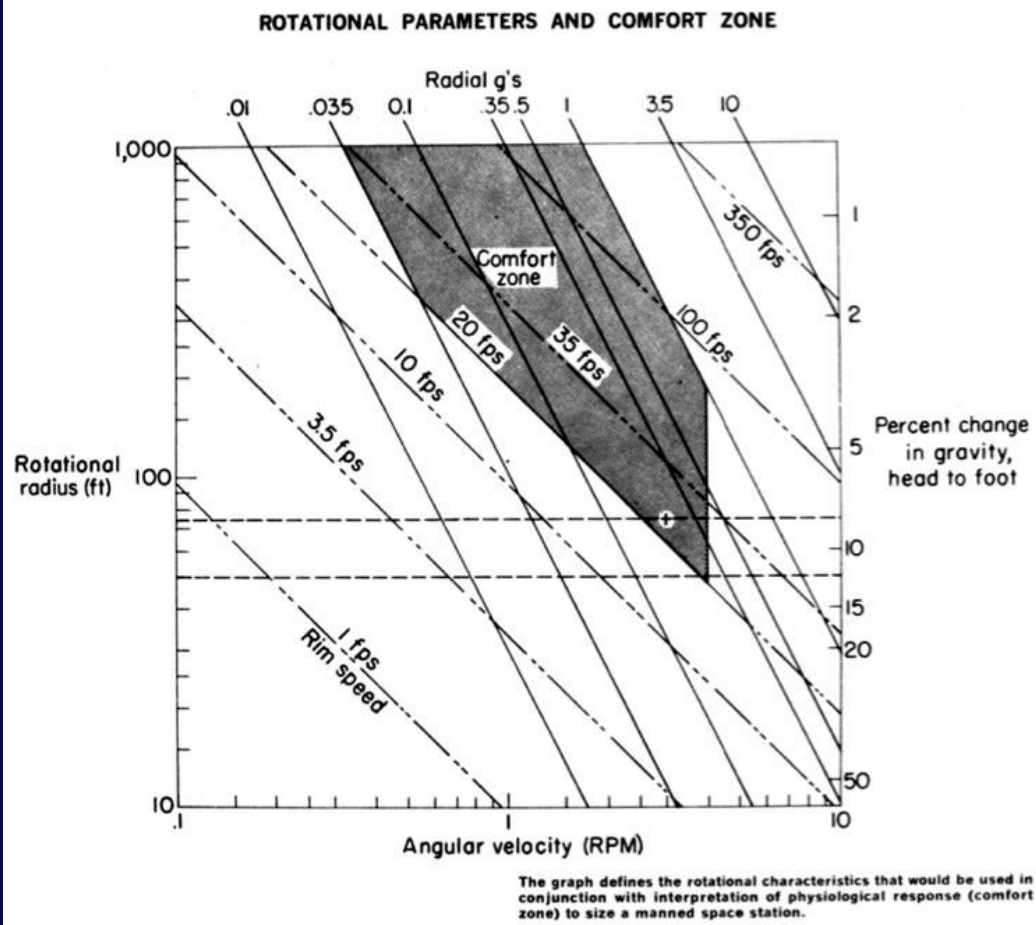
NASA Langley Research Center Rotating Space Station Simulator, 1960s



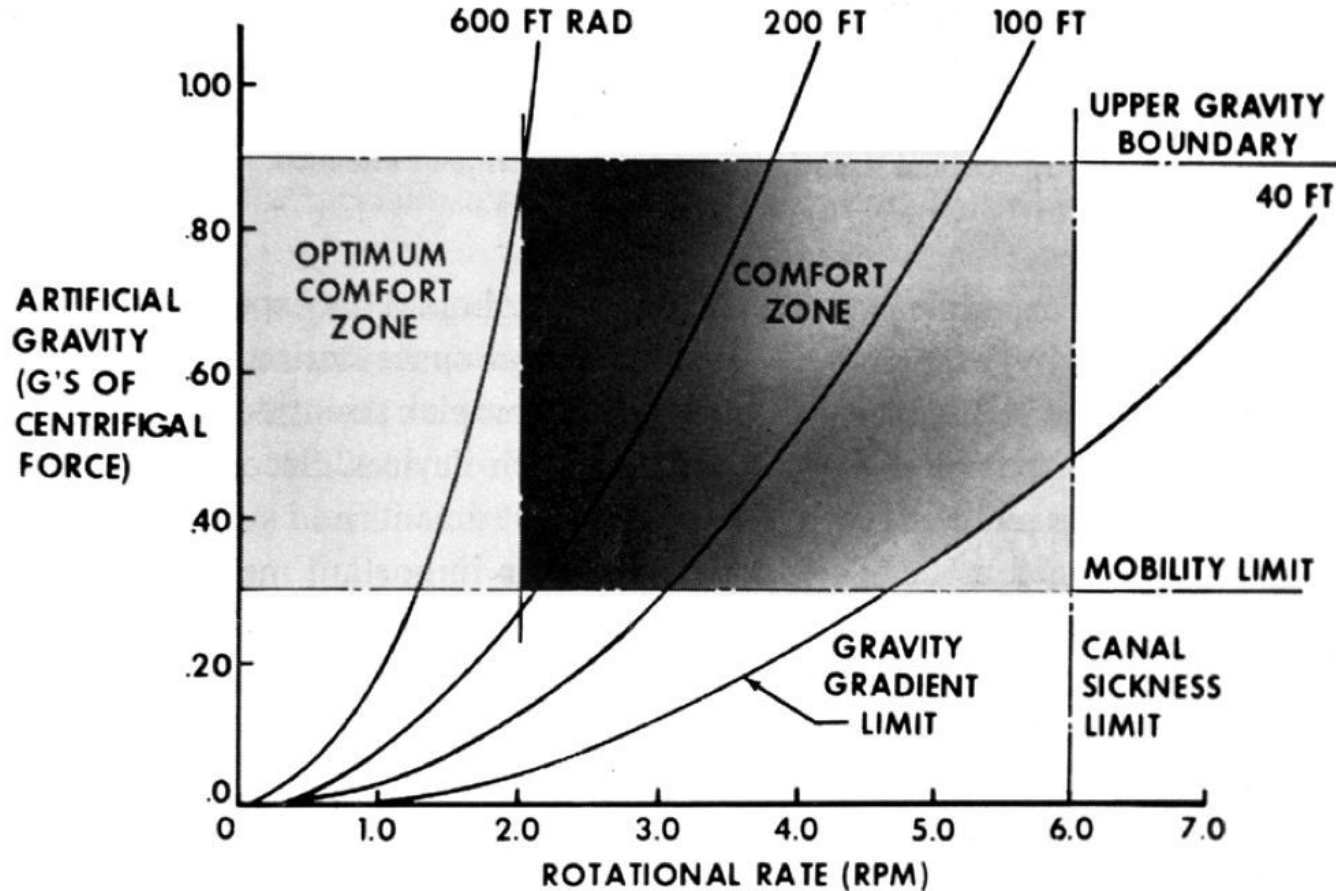
NASA Langley Research Center Rotating Space Station Simulator, 1960s



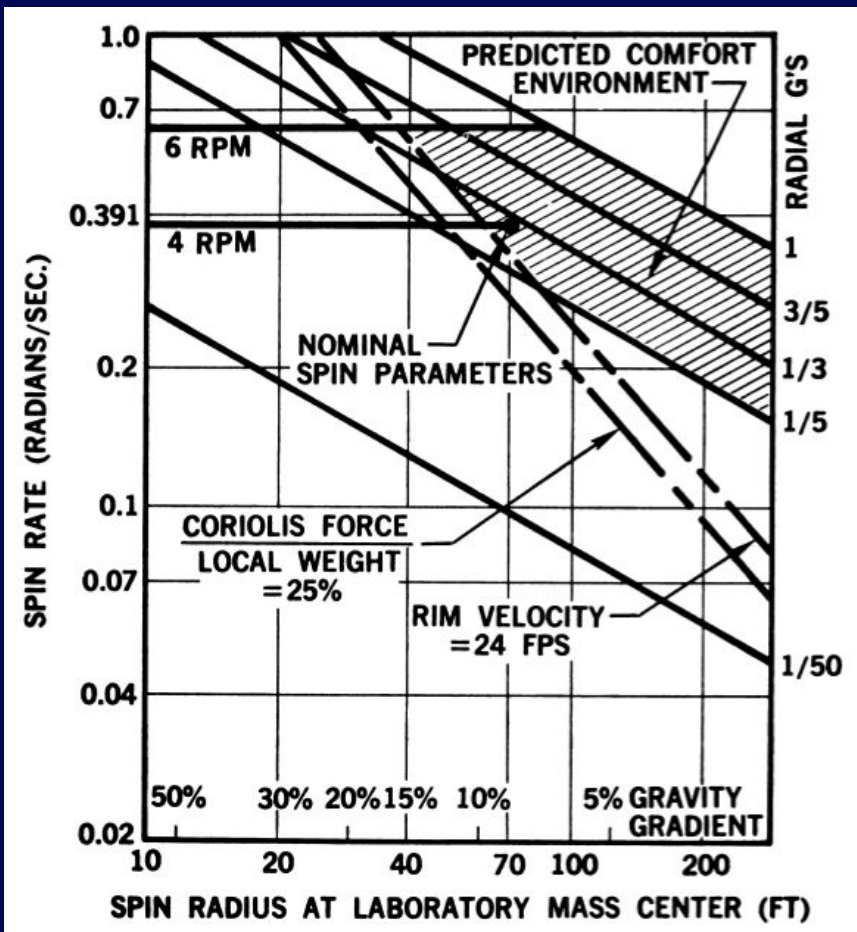
Comfort chart, Hill and Schnitzer, 1962



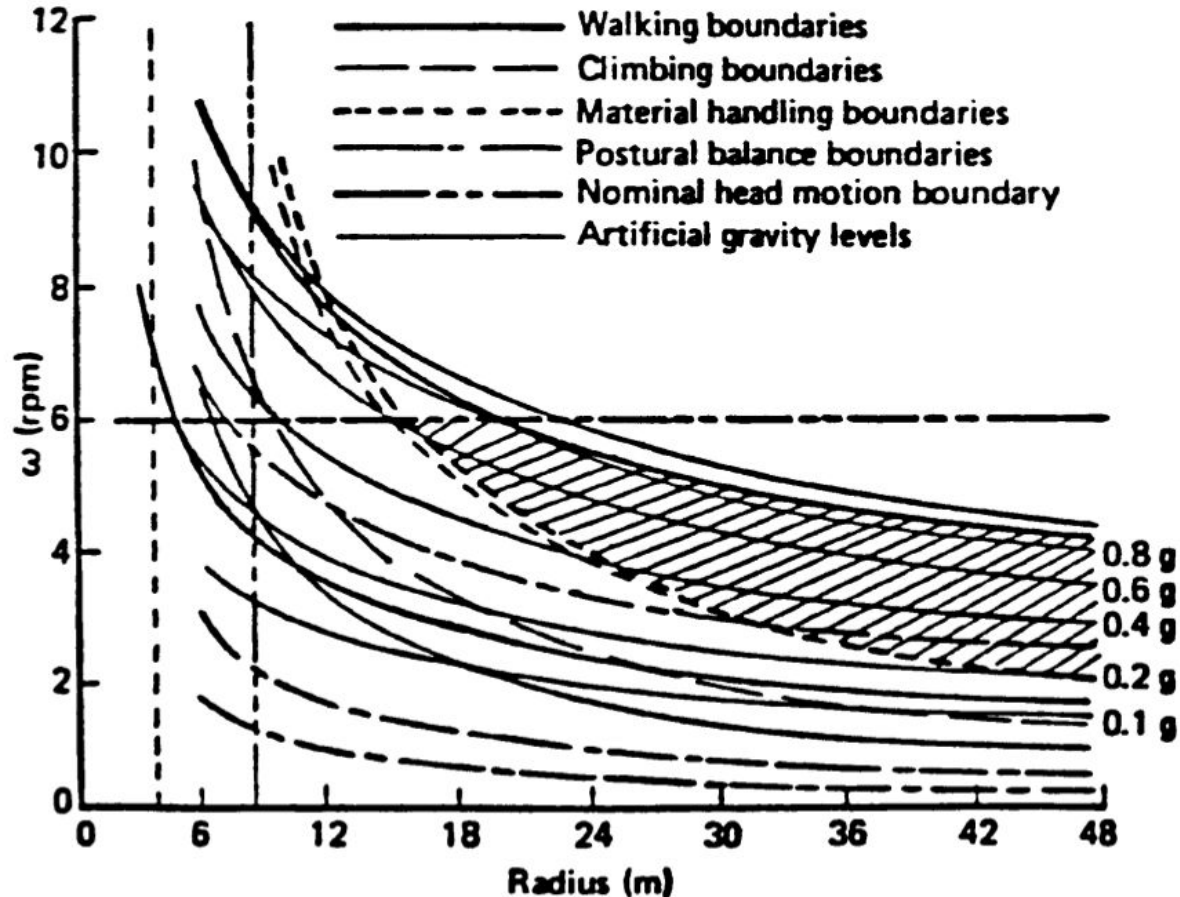
Comfort chart, Gilruth, 1969



Comfort chart, Gordon and Gervais, 1969

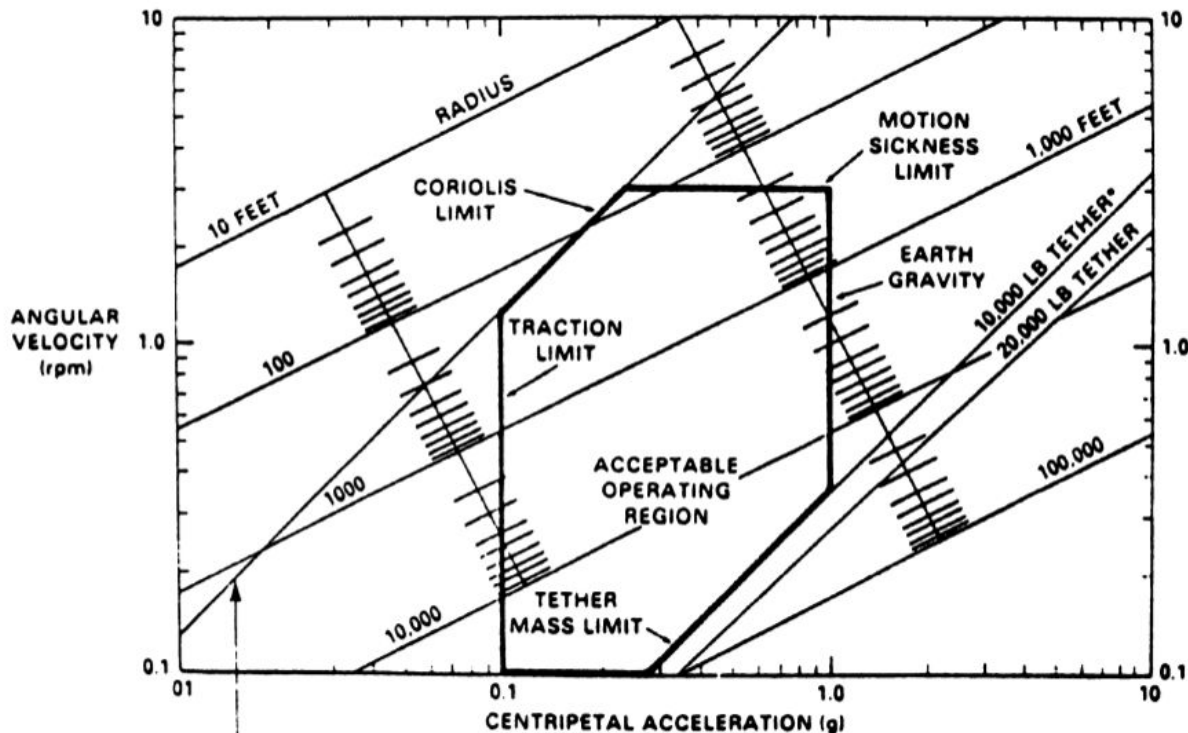


Comfort chart, Stone, 1973



Comfort chart, Cramer, 1985

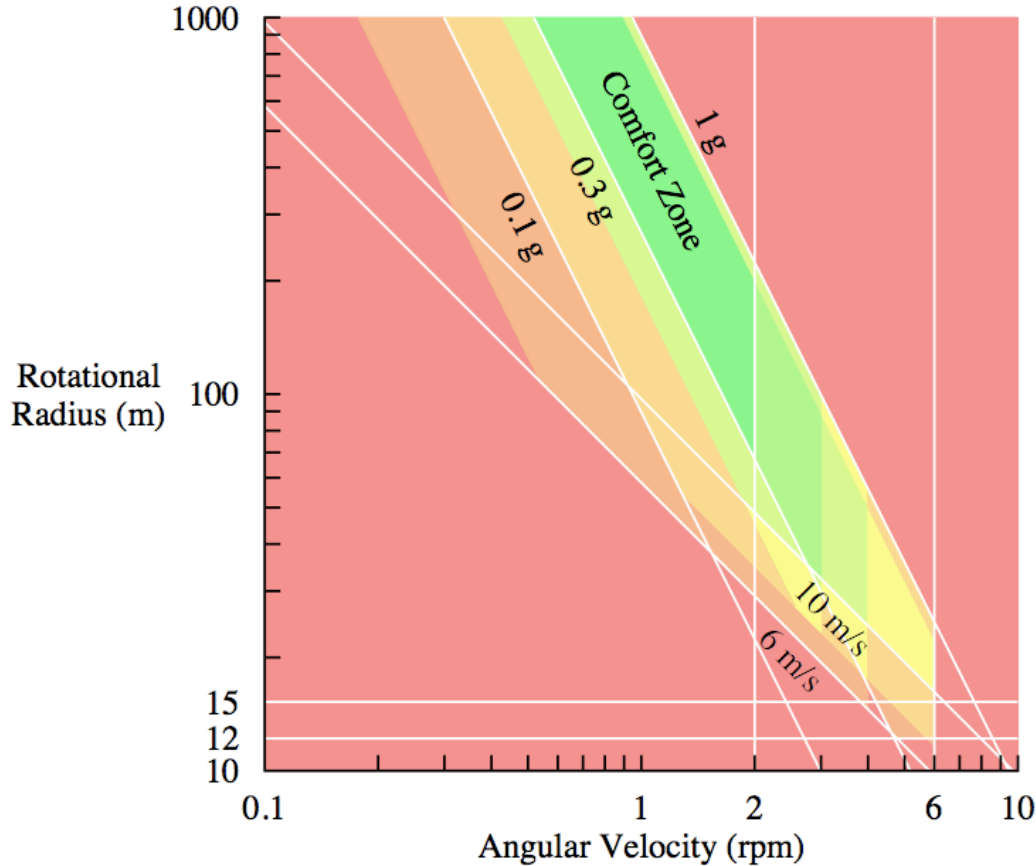
ARTIFICIAL GRAVITY PARAMETERS



CORIOLIS ACCELERATION = 0.25 CENTRIPETAL ACCELERATION
FOR 3 FT SEC⁻¹ RADIAL VELOCITY

* TETHER MASS LIMIT:
100,000 LB MODULE AT EACH END,
KEVLAR, CYLINDRICAL TETHER

Comfort chart – composite



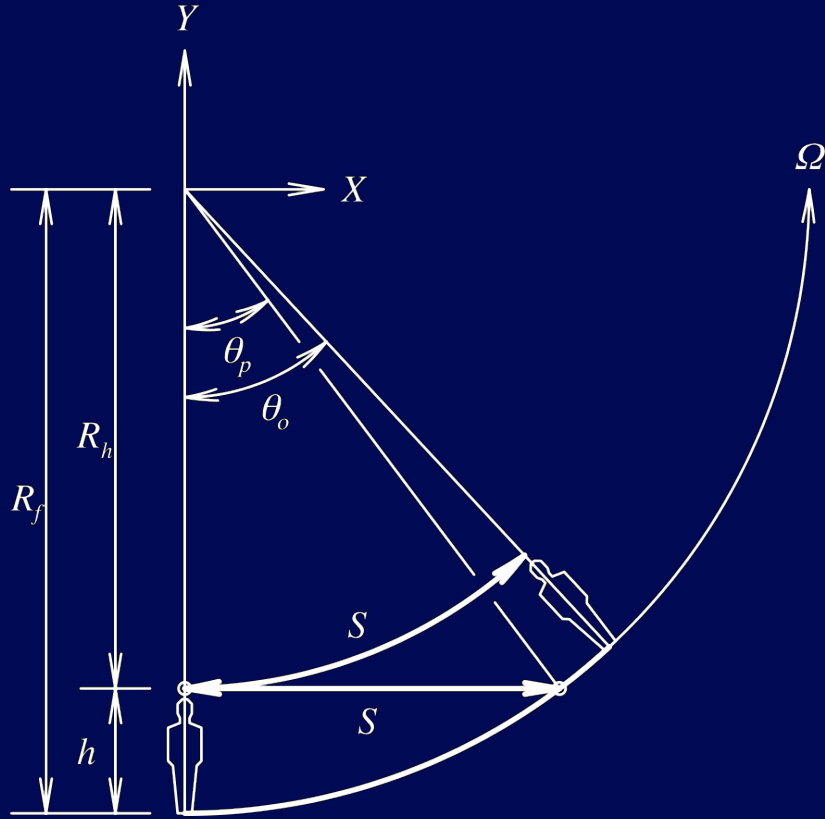
Starship population estimates:

| | | | |
|-------------|---------------------|------------|---------------|
| Birdsell | 10 – 100s | Marotta | 1,000 – 8,000 |
| Hodges | $10/ss \times \#ss$ | & Globus | |
| Cohen & al. | 100 - 500 | Smith | 40,000 |
| Wachter | 100s | Hein & al. | 100,000 |

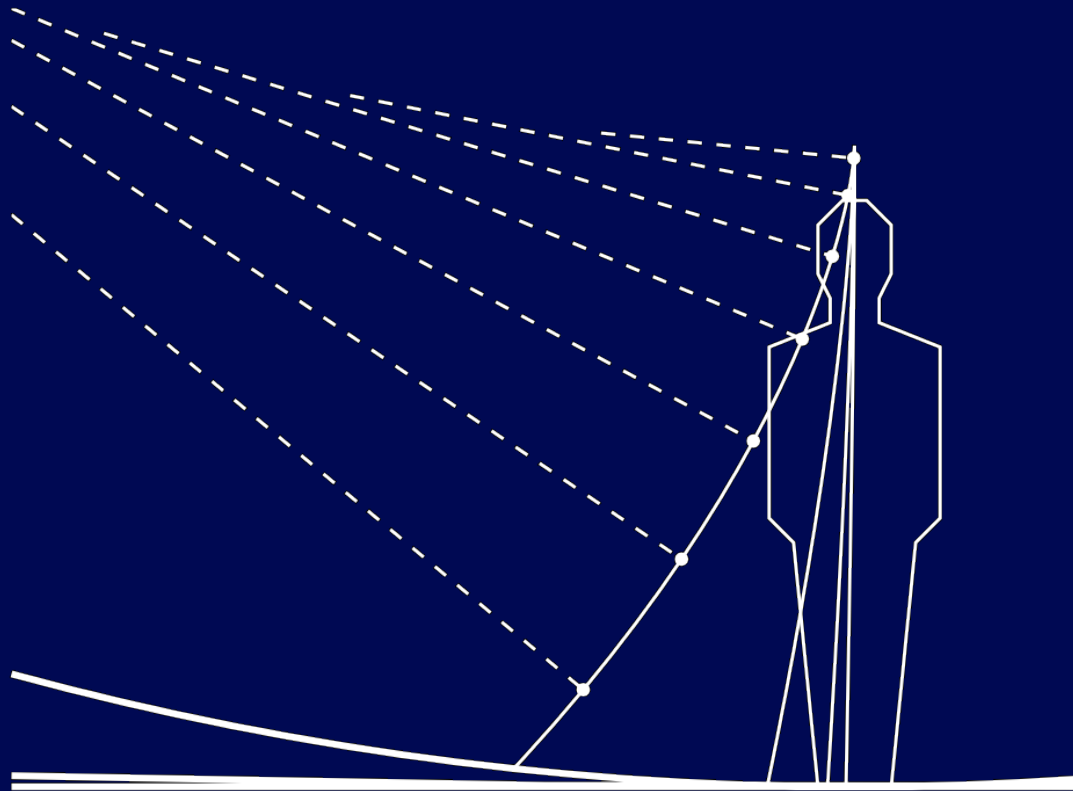
Starship size will be dictated
by population size,

not by rotational tolerance.

Dropping particles, inertial view: h/R_f



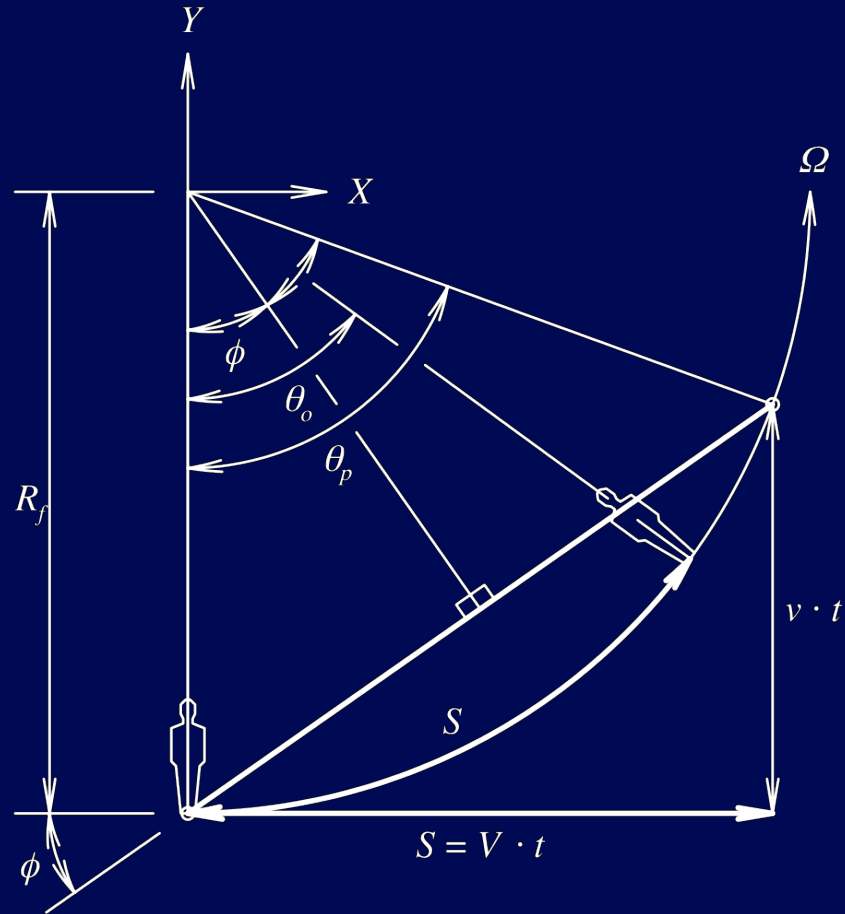
Dropping particles, rotating view: h/R_f



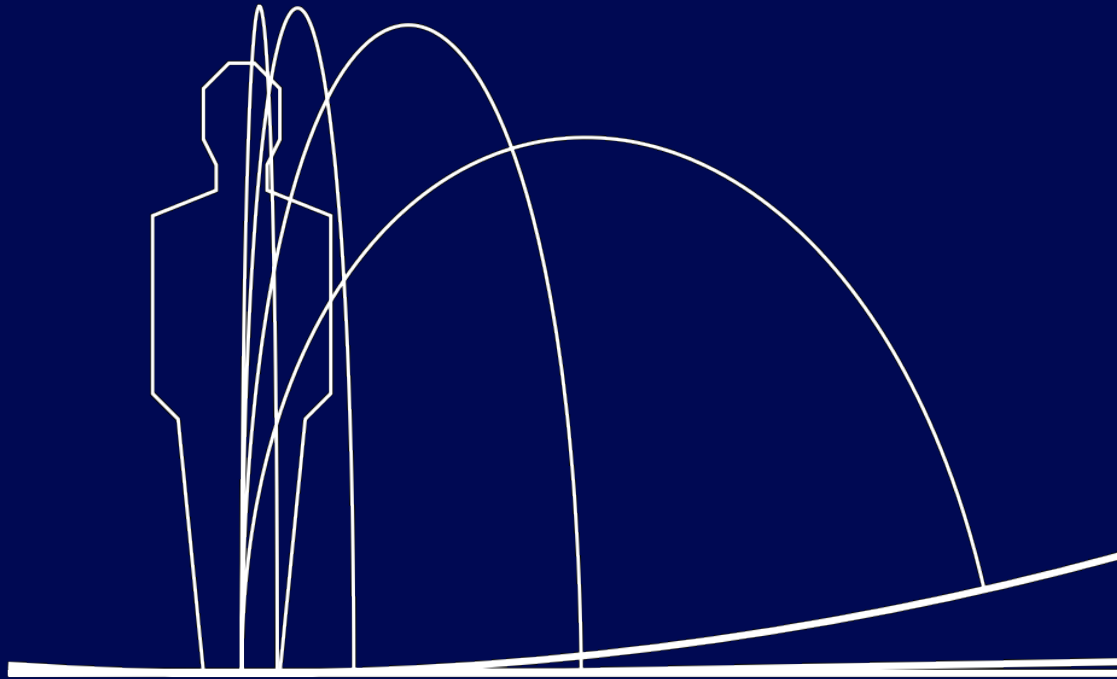
$$h = 2 \text{ m}$$

$$R_f = 10 \text{ m} \quad 100 \text{ m} \quad 1000 \text{ m} \quad 10000 \text{ m}$$

Hopping particles, inertial view: v/V



Hopping particles, rotating view: v/V



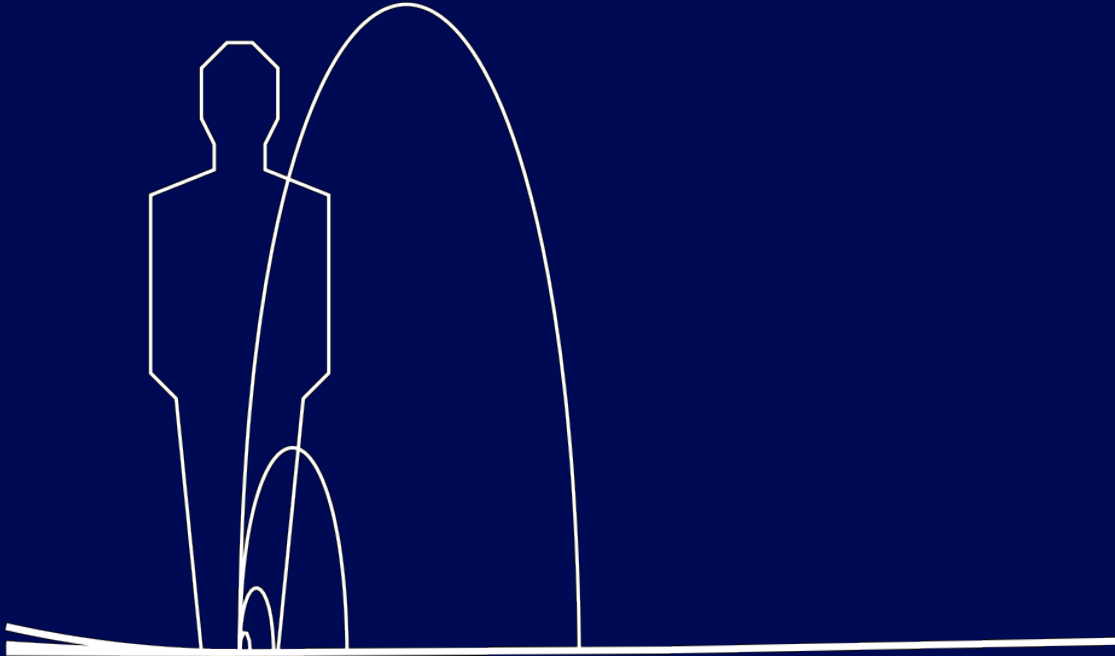
$$A_{cent} = 1 \text{ m/s}^2$$

$$v = 2 \text{ m/s}$$

$$V = 100 \text{ m/s} \quad 32 \text{ m/s} \quad 10 \text{ m/s} \quad 3.2 \text{ m/s}$$

$$R_f = 10000 \text{ m} \quad 1000 \text{ m} \quad 100 \text{ m} \quad 10 \text{ m}$$

Hopping particles, rotating view: v/V



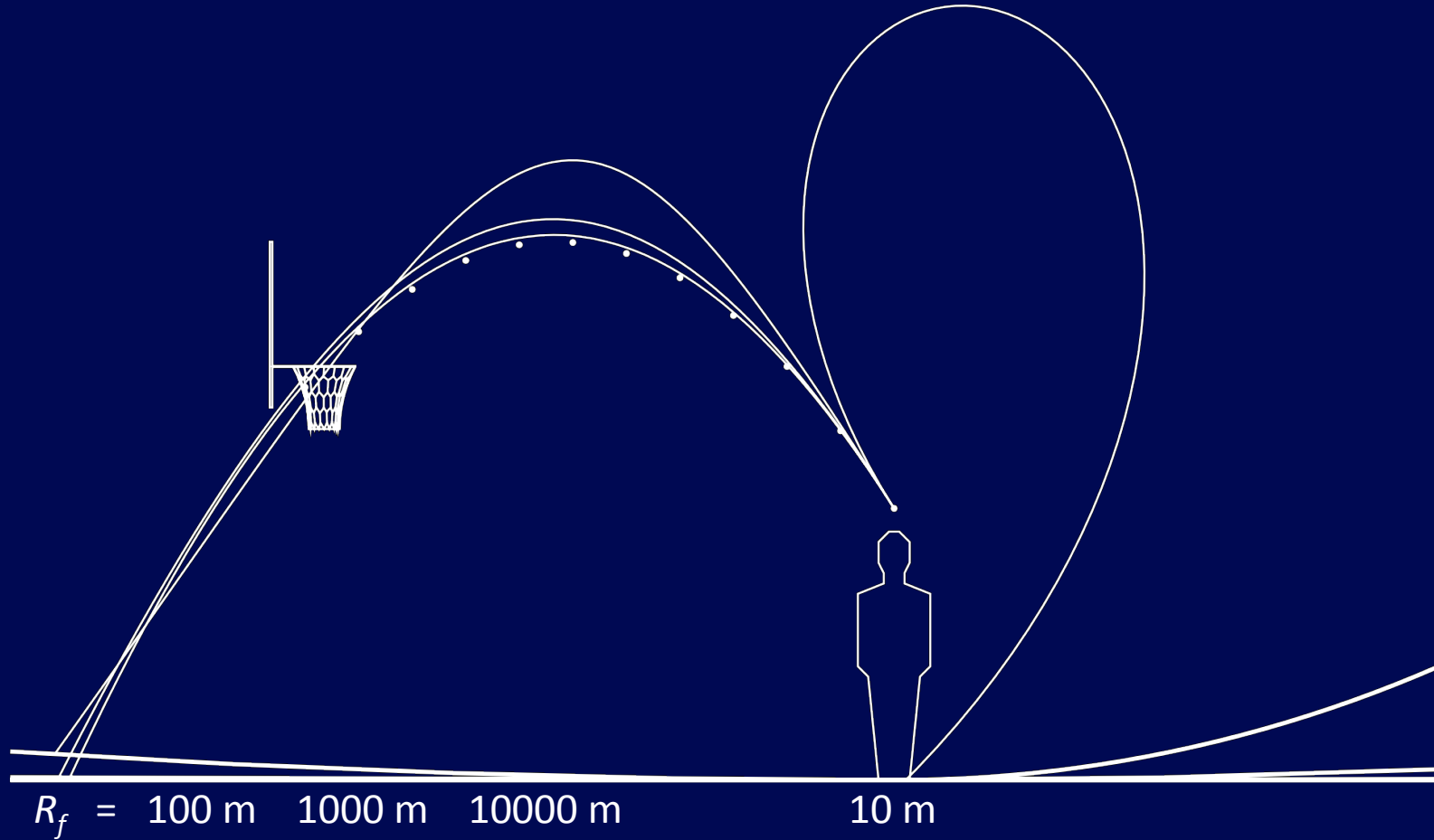
$$v = 2 \text{ m/s}$$

$$V = 10 \text{ m/s}$$

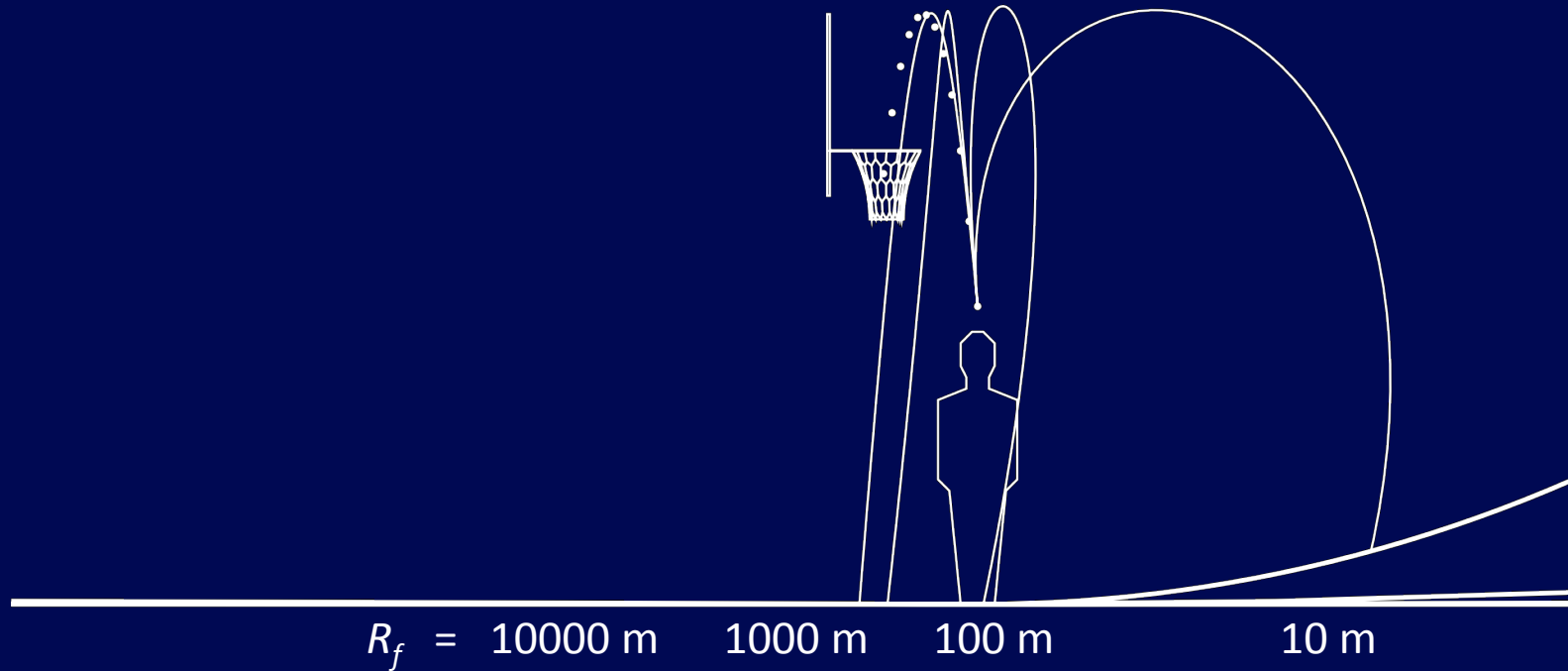
$$A_{cent} = 32 \text{ m/s}^2 \quad 10 \text{ m/s}^2 \quad 3.2 \text{ m/s}^2 \quad 1 \text{ m/s}^2$$

$$R_f = 3.2 \text{ m} \quad 10 \text{ m} \quad 32 \text{ m} \quad 100 \text{ m}$$

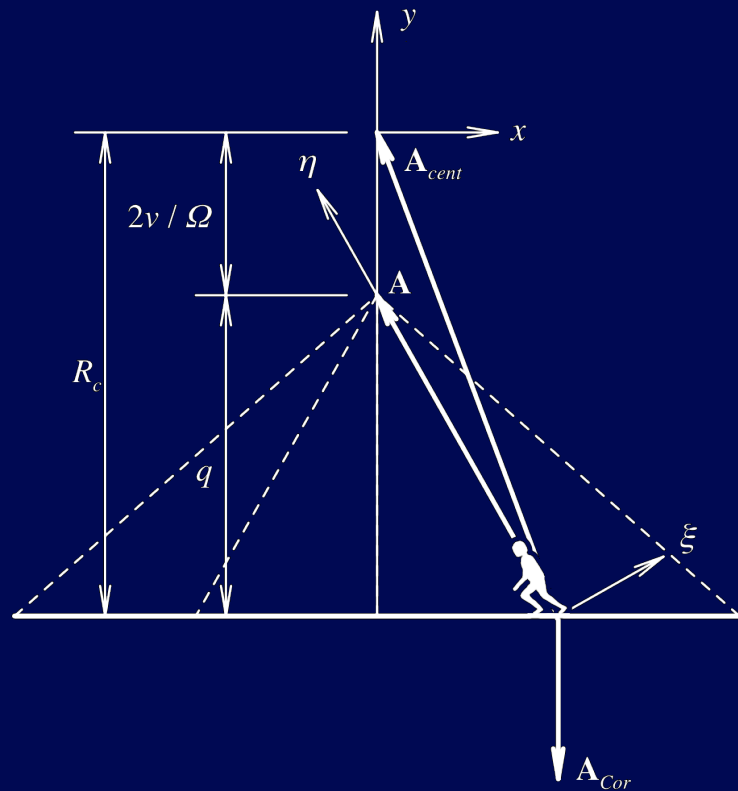
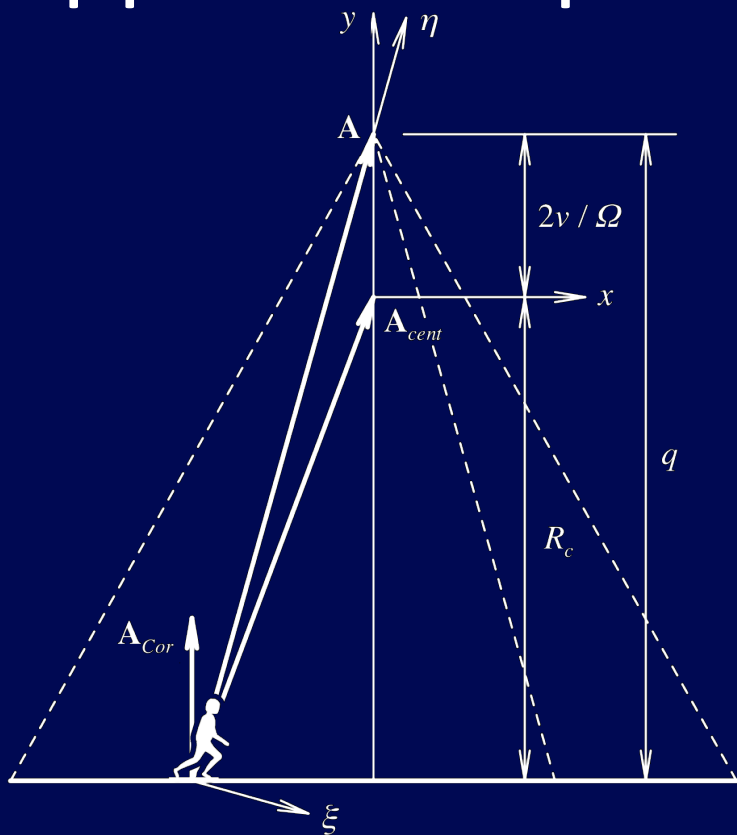
Basketball in 1-g AG: free throw



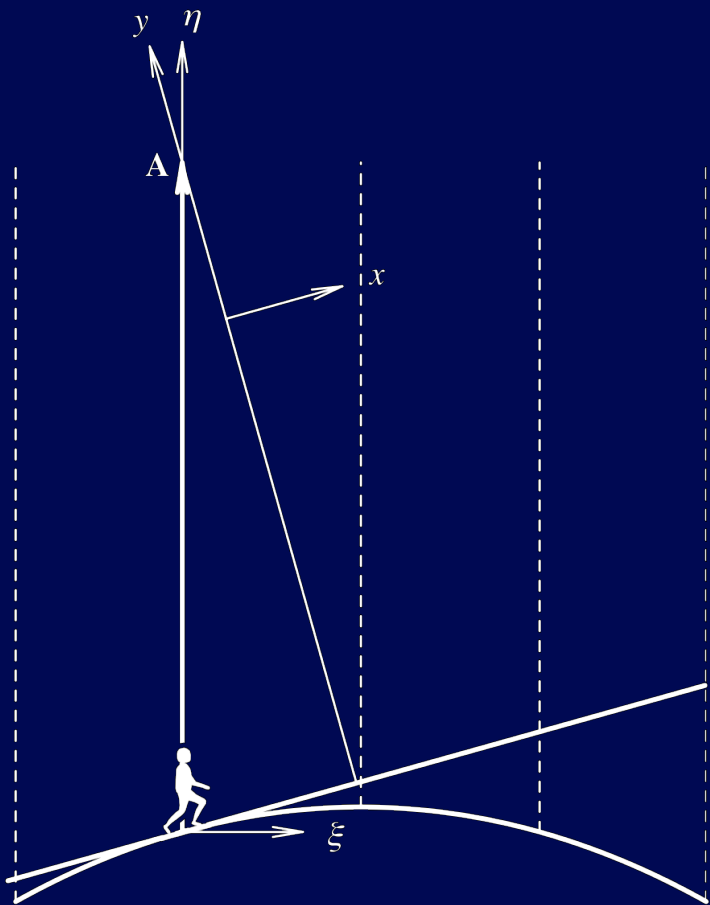
Basketball in 1-g AG: under the net



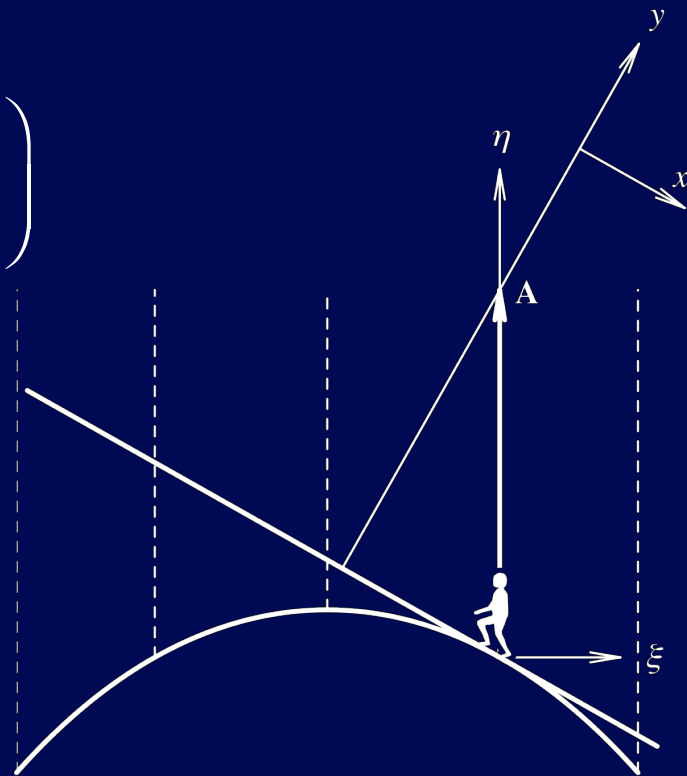
Apparent slope of flat floor



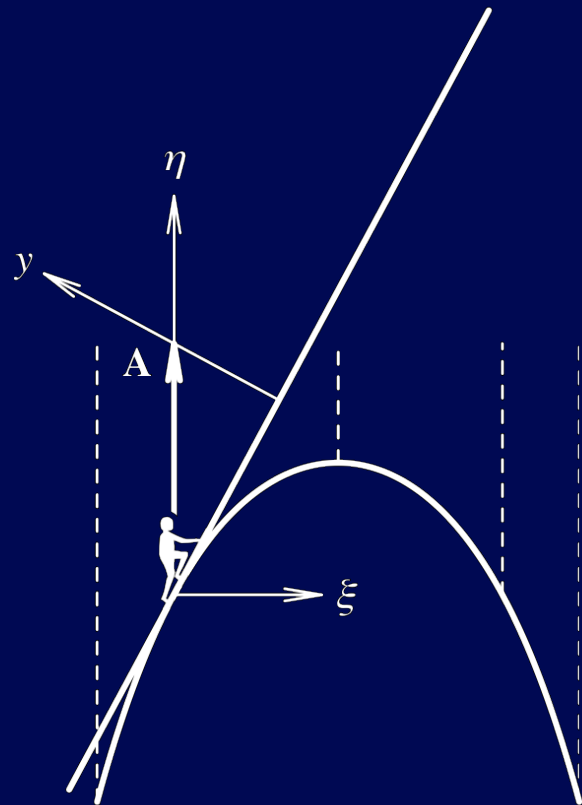
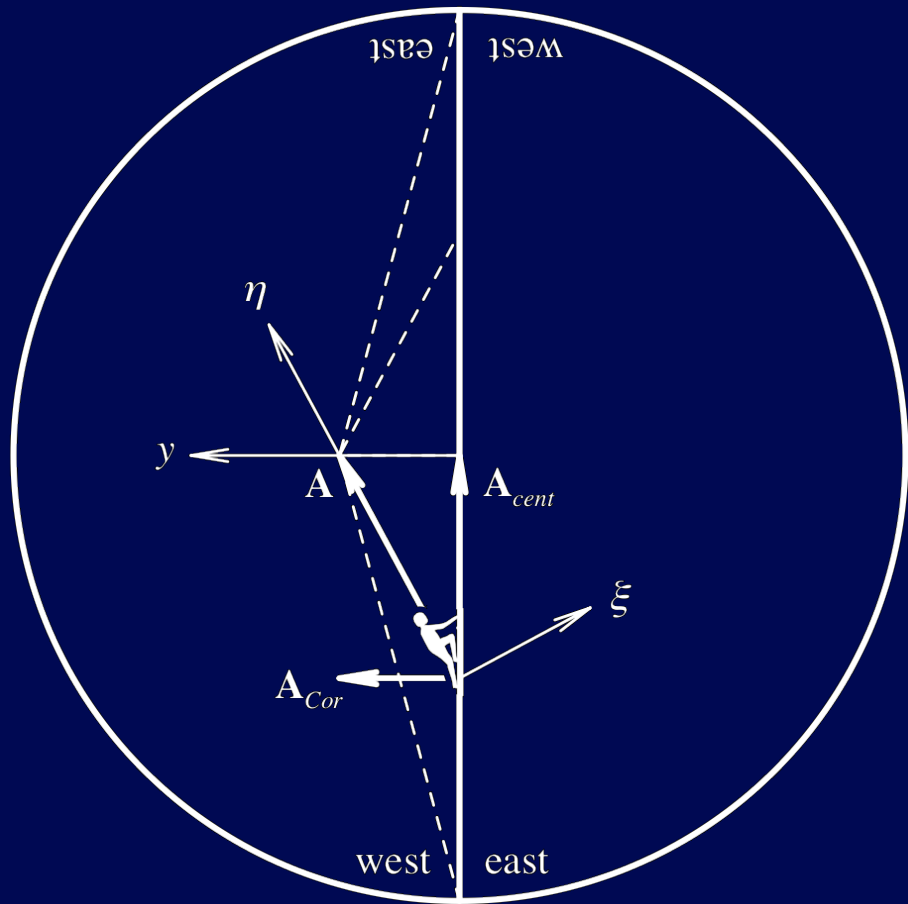
Apparent slope of flat floor: catenary arch



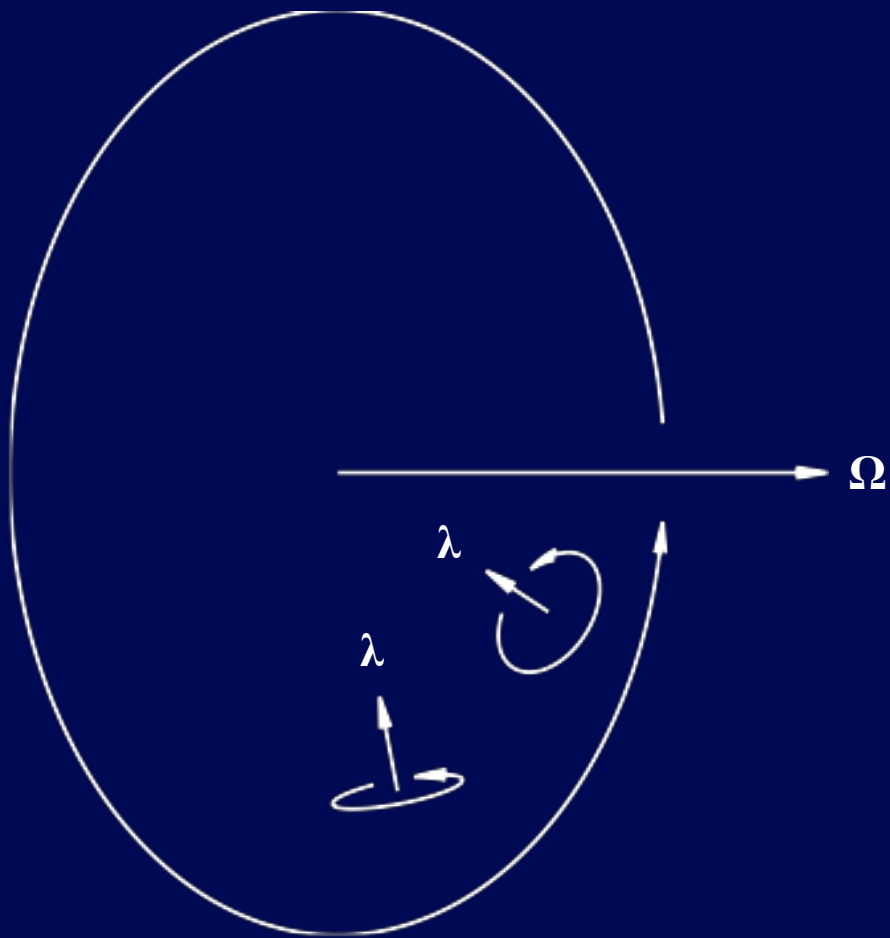
$$\frac{\eta}{q} = -\cosh\left(\frac{\xi}{q}\right)$$
$$\frac{A}{q} = \Omega^2 \cosh\left(\frac{\xi}{q}\right)$$



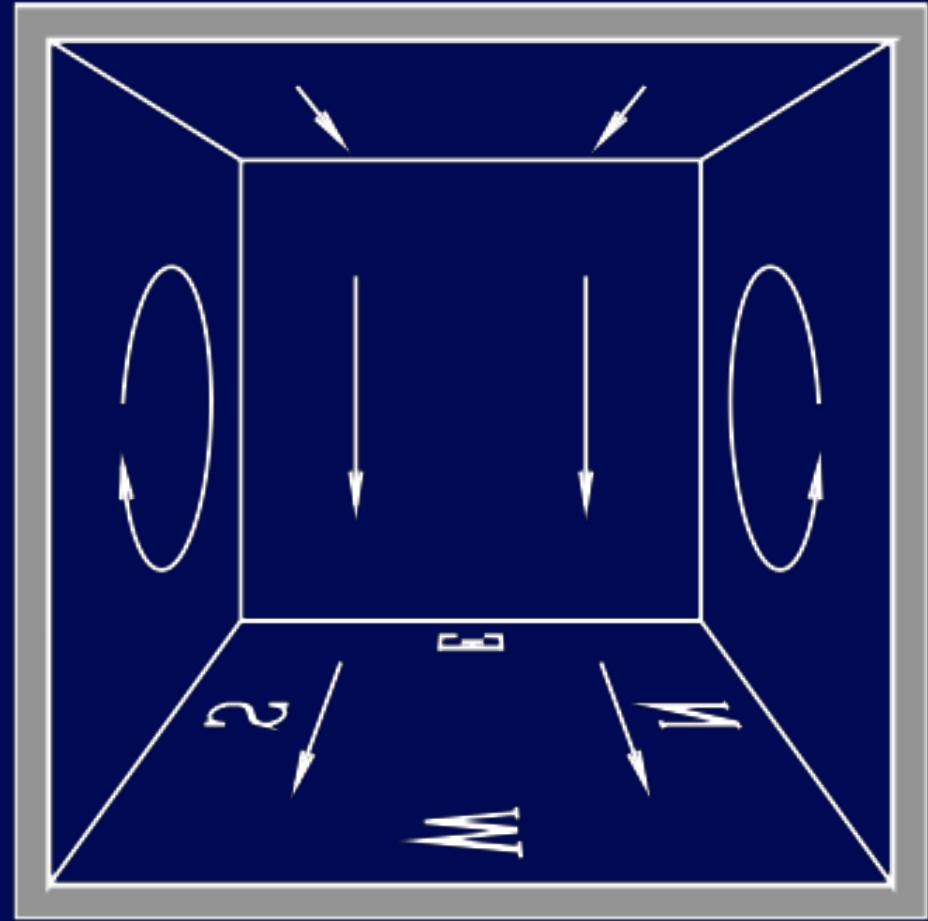
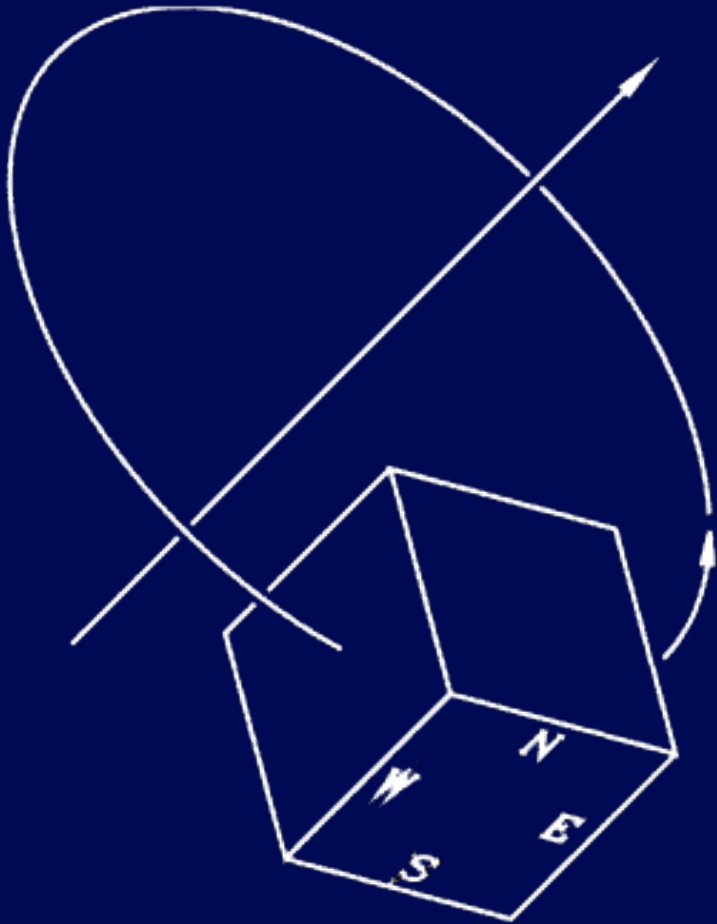
Apparent slope of ladder: catenary arch



Cross-coupled rotations

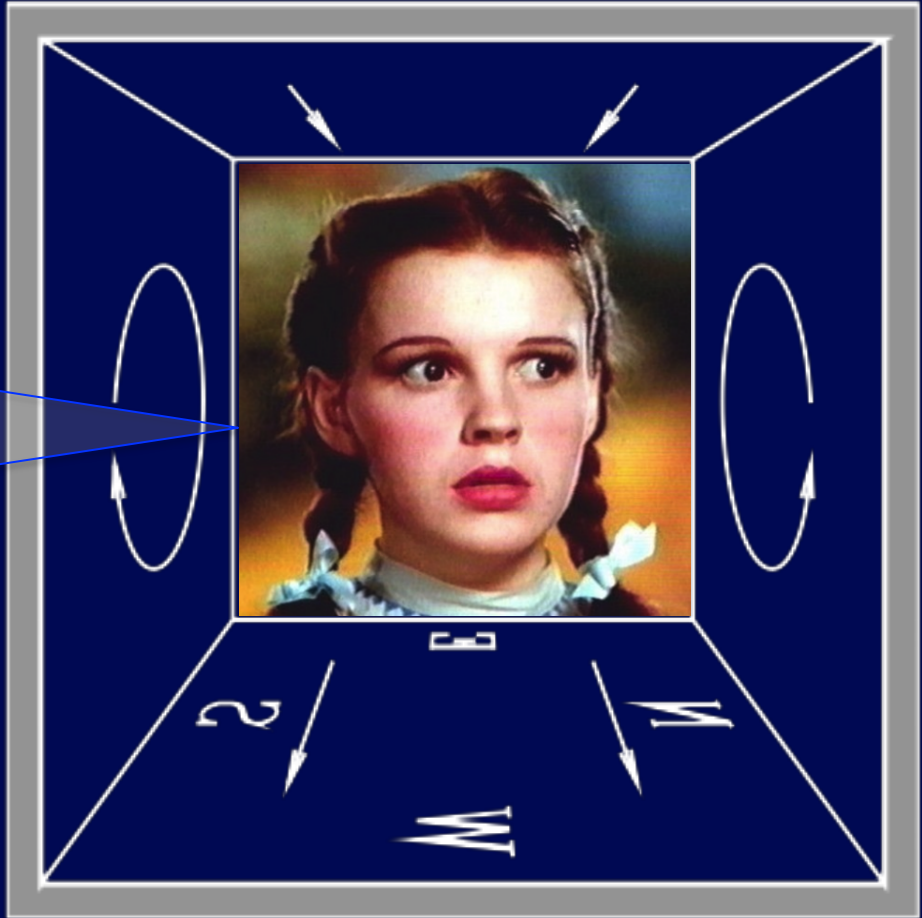


Principal directions: inside-out

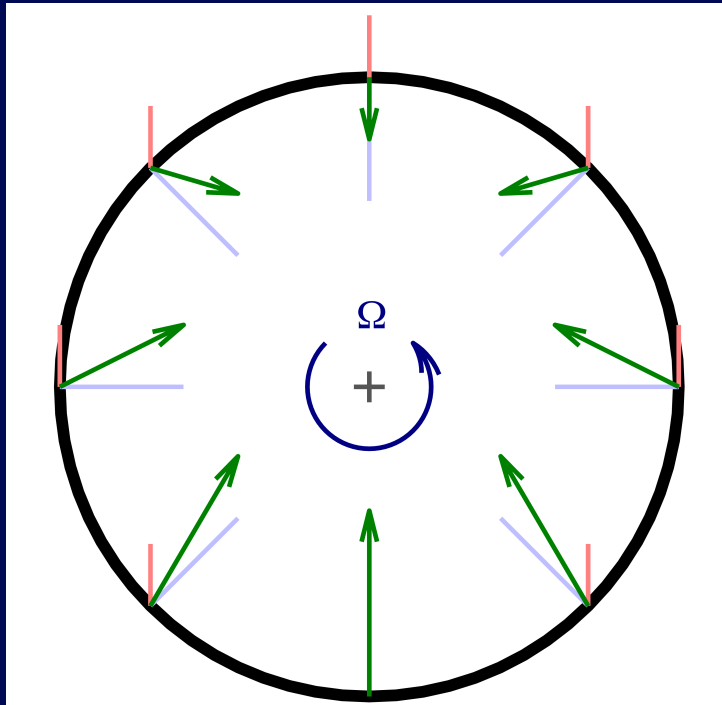


The country and climate in which we build

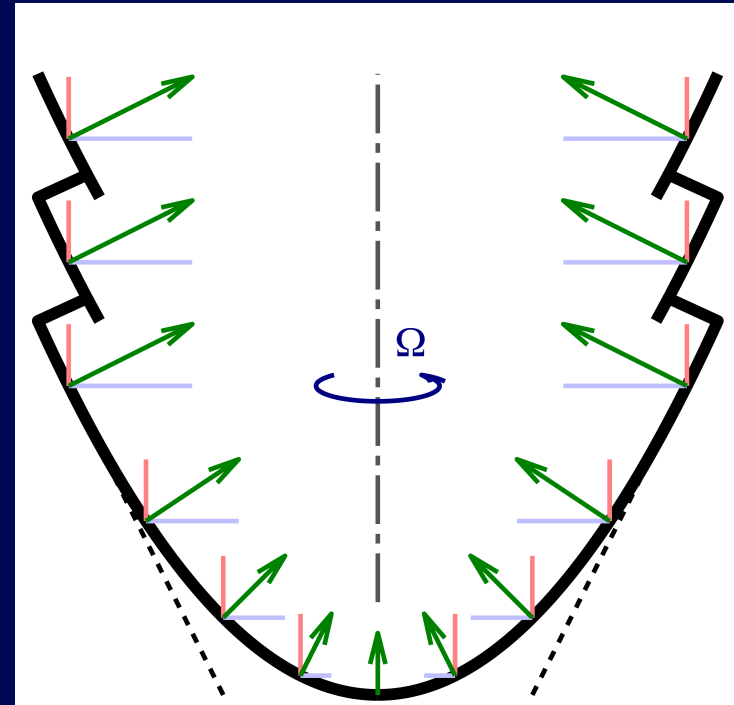
We're not in
Kansas anymore.
– *Gale*



Combined linear + centripetal acceleration



in-plane thrust



on-axis thrust