

embotech 



# Design Simulation and Software Validation for On-Board and Real-Time Optimal Guidance

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Samir Bennani, Jean-Philippe Preaud, Jorgen Bru

# WHY DO WE NEED REAL-TIME OPTIMAL GUIDANCE?

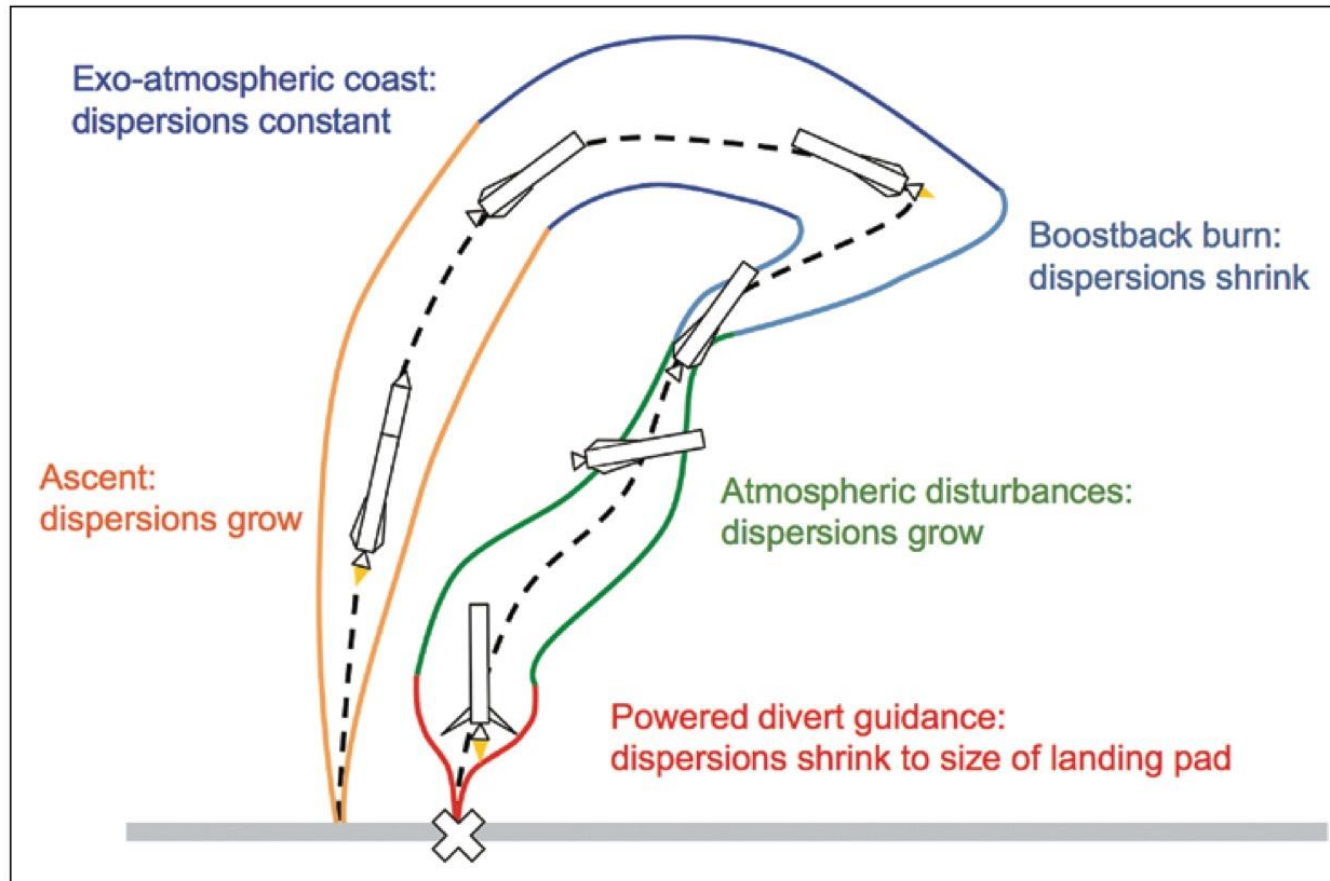


FIGURE 4 Phases of an F9R return-to-launch-site mission. The colored lines represent the largest possible variations in the trajectory, known as dispersions.

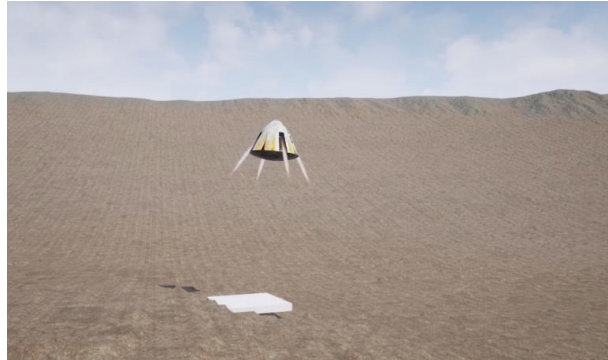
- Trajectory optimality under actual flight conditions
- Ensure mission completion under constraints and actual flight conditions
- Reduce missionization time
- Mid-flight replanning (mission flexibility)

On-line optimization enables autonomous space operations

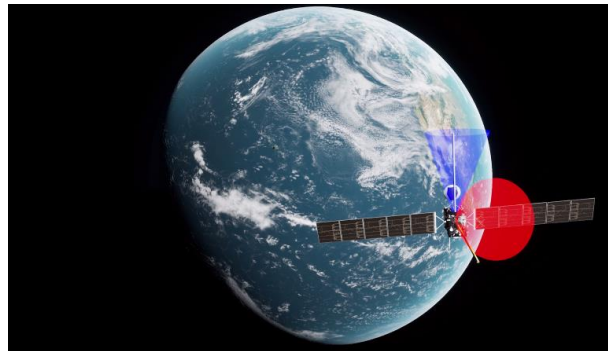
# PROJECT TIMELINE

Phase 1  
Feasibility study

2016 - 2017



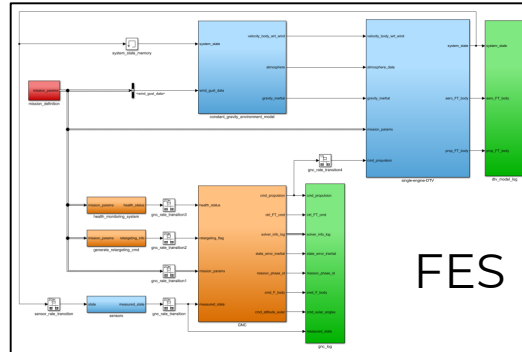
Constrained Powered Descent



Constrained Attitude Guidance

Phase 2.1  
Maturation and  
flight test plan

2018 - 2019



Continuous  
integration  
testing

SVF



Phase 2.2  
Flight testing

2019 - 2020



**Problem 1** : 3-DoF, Non-Convex, Continuous-Time, Free-Final-Time, Minimum-Fuel Problem

Cost Function

$$\underset{t_f, \mathbf{T}_B(\cdot)}{\text{minimize}} \int_{t_0}^{t_f} \|\mathbf{T}_B(t)\| + \lambda_1 \|\dot{\mathbf{T}}_B(t)\|^2 + \lambda_2 \eta(t)^2 dt \quad (1)$$

subject to:

Boundary Conditions

$$m(t_0) = m_0 \quad (2)$$

$$\mathbf{r}_X(t_0) = \mathbf{r}_{X,0} \quad \|\mathbf{r}_X(t_f) - \mathbf{r}_{X,f}\| \leq r_{tol} \quad (3)$$

$$\dot{\mathbf{r}}_X(t_0) = \dot{\mathbf{r}}_{X,0} \quad \|\dot{\mathbf{r}}_X(t_f) - \dot{\mathbf{r}}_{X,f}\| \leq \dot{r}_{tol} \quad (4)$$

Point-mass Dynamics

$$\dot{m}(t) = -\alpha \|\mathbf{T}_B(t)\| \quad (5)$$

$$\ddot{\mathbf{r}}_X(t) = \frac{1}{m(t)} \mathbf{F}_X(t) + \mathbf{g}_X \quad (6)$$

State Constraints

$$\mathbf{e}_1 \cdot (\mathbf{r}_X(t) - \mathbf{r}_X(t_{0,f})) \geq \tan(\gamma) \|\mathbf{e}_2 \mathbf{e}_3 \cdot (\mathbf{r}_X(t) - \mathbf{r}_X(t_{0,f}))\| \quad (7)$$

$$\|\dot{\mathbf{r}}_X(t)\| \leq v_{max} + \eta(t) \quad (8)$$

$$\eta(t) \geq 0 \quad (9)$$

Control Constraints

$$0 \leq T_{min} \leq \|\mathbf{T}_B(t)\| \leq T_{max} \quad (10)$$

$$\dot{T}_{min} \leq \dot{\mathbf{T}}_B(t) \leq \dot{T}_{max} \quad (11)$$

$$\mathbf{e}_1 \cdot \mathbf{T}_B(t) \geq \cos(\theta_{max}) \|\mathbf{T}_B(t)\| \quad (12)$$

$$\mathbf{e}_1 \cdot \mathbf{T}_B(t)(1 + \nu_D) \leq T_{max}(1 - \mathbf{e}_1 \cdot \mathbf{r}_X(t)\beta) \quad (13)$$

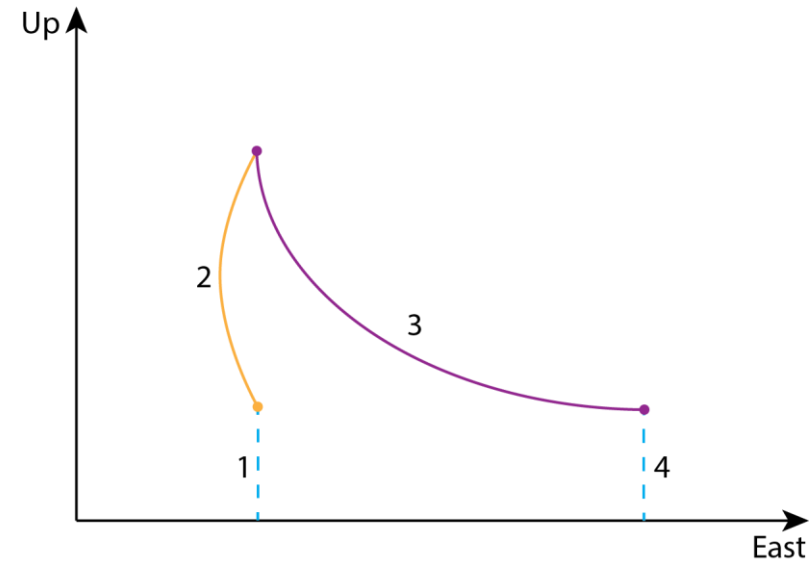
# MISSION PROFILE

INCAS Demonstrator for Technology Validation: DTV



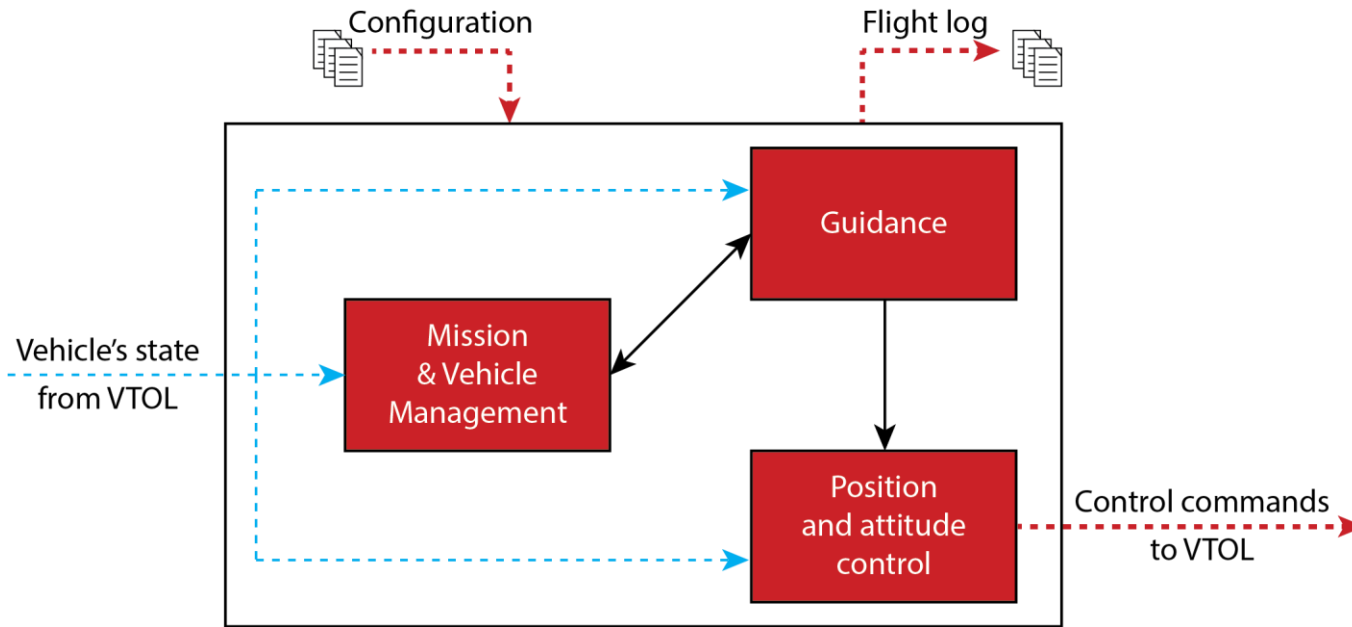
- Jet powered
- Vertical Takeoff and Landing
- Max thrust = 900N
- Weight = 60 - 70 Kg
- Height = 1.2 m

End-to-End mission scenario



1. Vertical takeoff
2. Ascent (Real-Time Optimal Guidance)
3. Descent (Real-Time Optimal Guidance)
4. Vertical landing

# GUIDANCE AND CONTROL ARCHITECTURE



## MVM

- Flight mode selector
- Target manager
- Handle exceptions
- Tracking errors
- Engine faults
- Retargeting
- Emergency landing

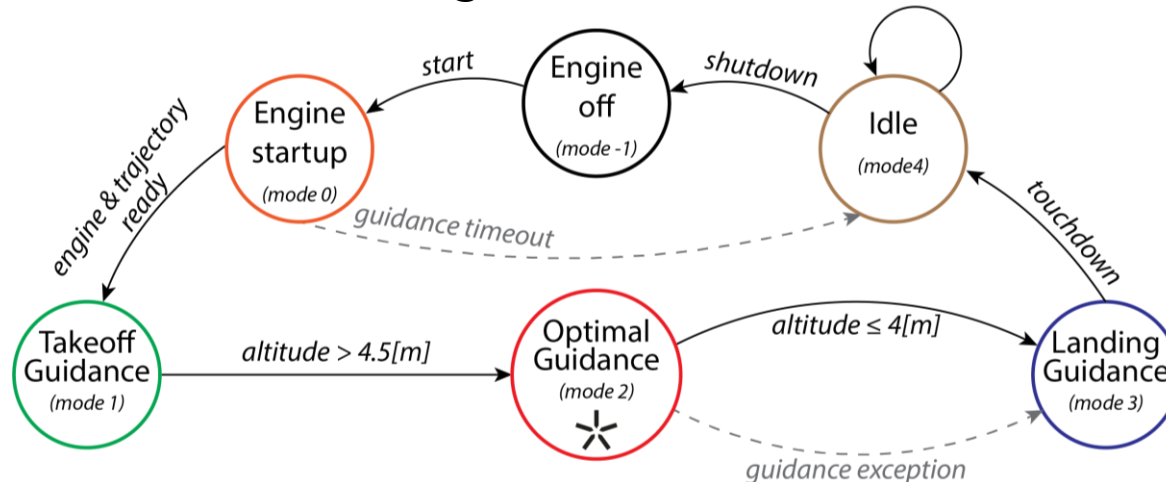
## Guidance

- Constant velocity takeoff
- 3-DoF NLP optimal
- Constant velocity landing

## Control

- LQR on position and attitude
- FF aerodynamics balancing

## Flight mode selector



# OPTIMAL GUIDANCE

- Tested strategies

3-DoF convex

3-DoF convex with ToF lookup table

3-DoF non-convex

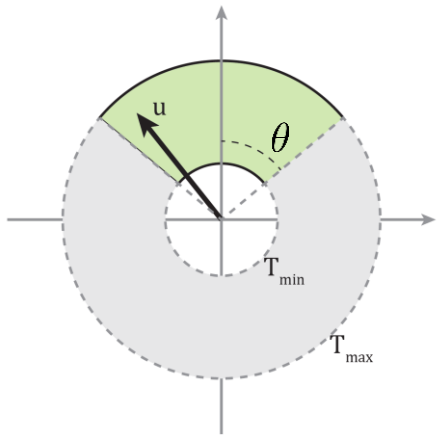
6-DoF non-convex

Minimize fuel consumption

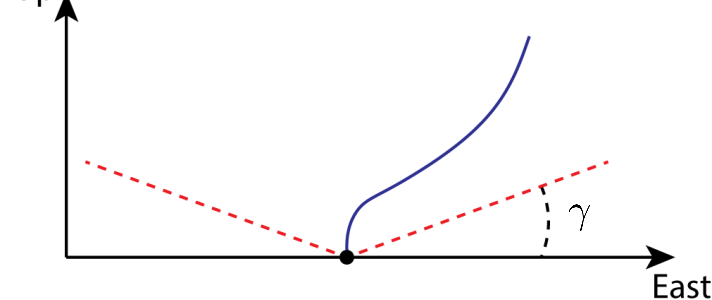
or

Minimize landing error

Thrust constraints



Glideslope constraint



**Problem 1** : 3-DoF, Non-Convex, Continuous-Time, Free-Final-Time, Minimum-Fuel Problem

Cost Function

$$\underset{t_f, \mathbf{T}_B(\cdot)}{\text{minimize}} \int_{t_0}^{t_f} \|\mathbf{T}_B(t)\| + \lambda_1 \|\dot{\mathbf{T}}_B(t)\|^2 + \lambda_2 \eta(t)^2 dt \quad (1)$$

subject to:

Boundary Conditions

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Point-mass Dynamics

$$\dot{m}(t) = -\alpha \|\mathbf{T}_B(t)\| \quad (5)$$

$$\ddot{\mathbf{r}}_I(t) = \frac{1}{m(t)} \mathbf{F}_I(t) + \mathbf{g}_I \quad (6)$$

State Constraints

$$\mathbf{e}_1 \cdot (\mathbf{r}_I(t) - \mathbf{r}_I(t_{0,f})) \geq \tan(\gamma) \|\mathbf{e}_2 \ \mathbf{e}_3\| \cdot (\mathbf{r}_I(t) - \mathbf{r}_I(t_{0,f})) \quad (7)$$

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Control Constraints

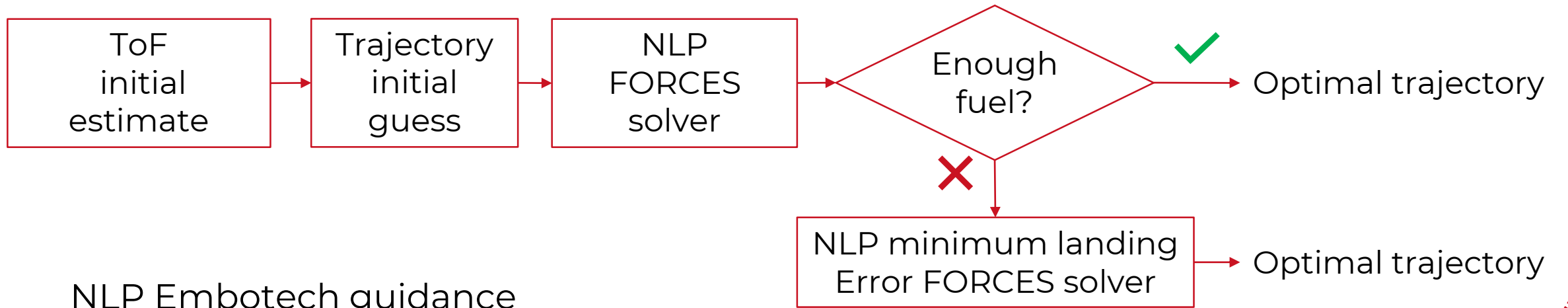
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$$\dot{T}_{min} \leq \dot{\mathbf{T}}_B(t) \leq \dot{T}_{max} \quad (11)$$

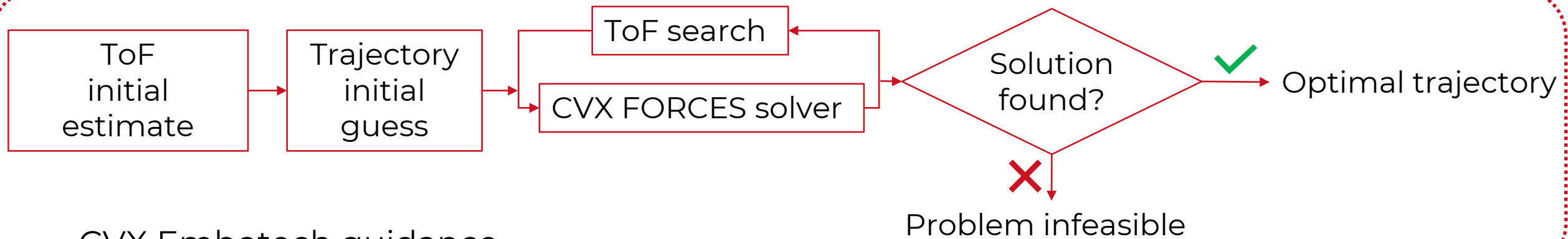
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# OPTIMAL GUIDANCE GUIDANCE



NLP Embotech guidance

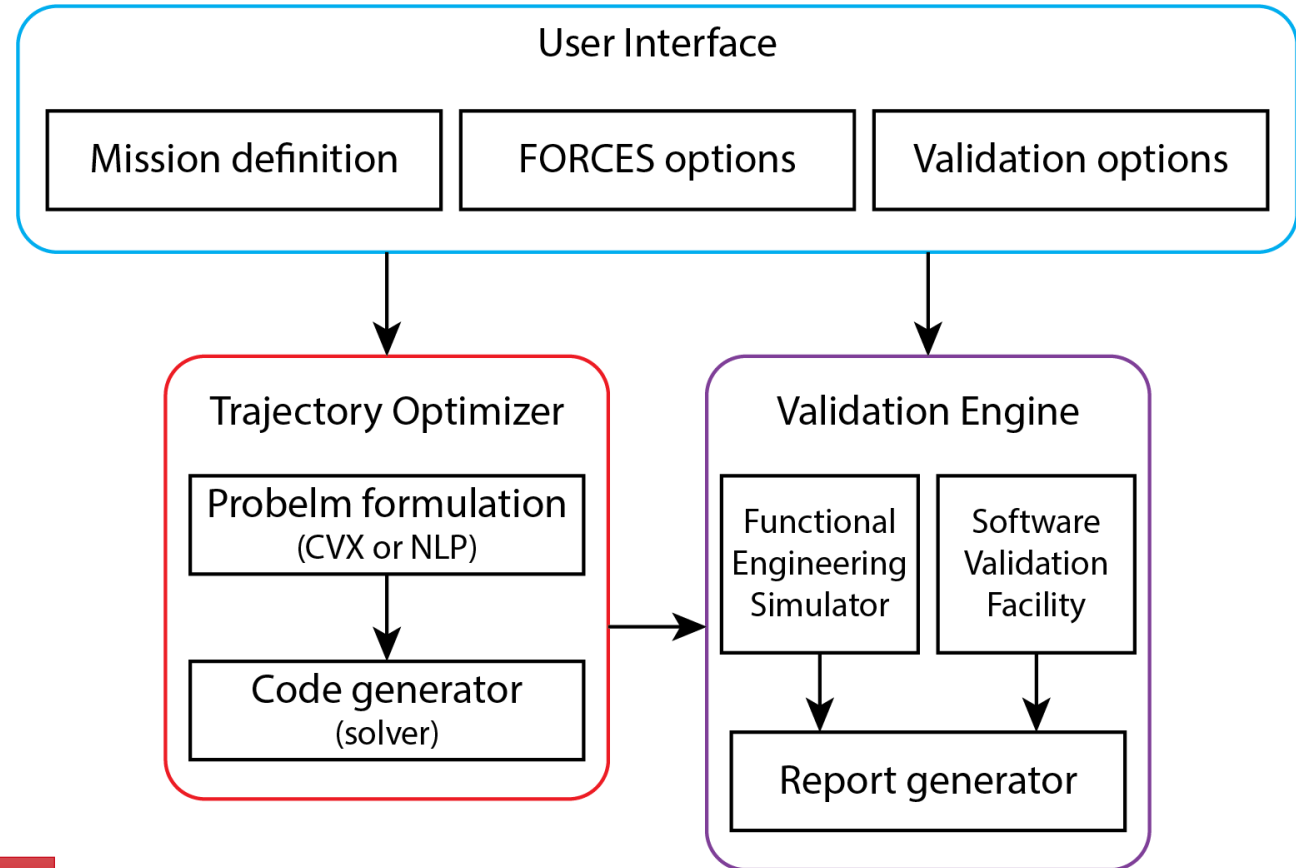


CVX Embotech guidance



# SOFTWARE FRAMEWORK

- A unifying framework designed to extensively evaluate and analyze the guidance and control performance
- Completely modular and extendable architecture
- Matlab/Simulink interface
- Support for automatic code generation and deployment on embedded platforms.

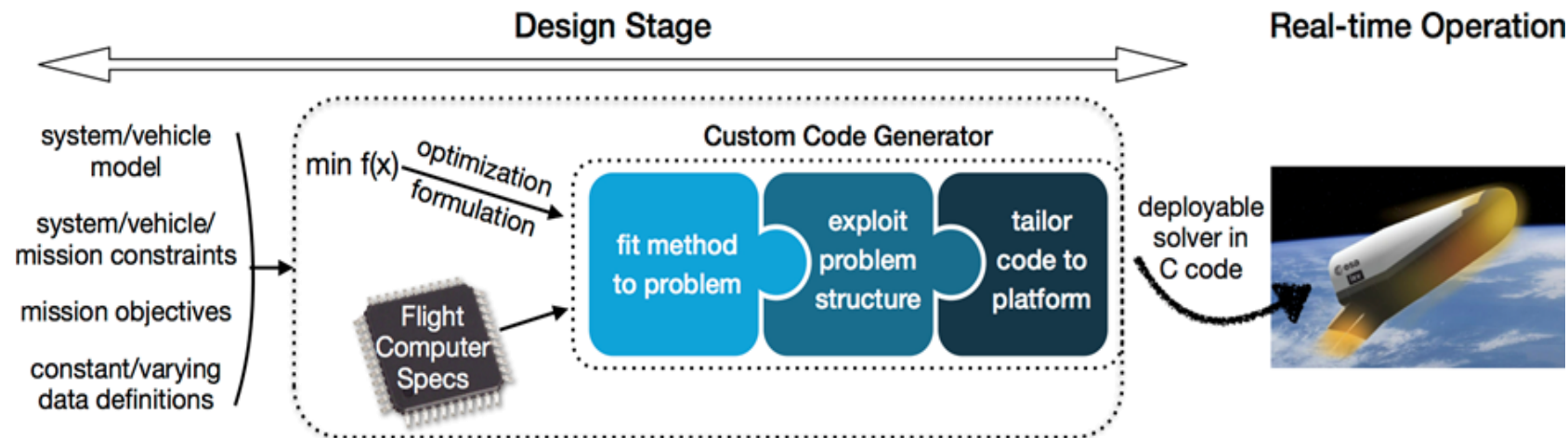


The generated C is embeddable on-board as part of the real-time flight code

# FORCES PRO

## Concept

- State-of-the-art client/server code generation system for optimization solvers
- C code tailored for deployment on embedded systems
- Uses only static memory allocation
- No dependency on external libraries
- MISRA C compliant
- Wide range of algorithmic options for LPs, QPs, QCQPs, SOCPs, NLPs and MI-NLPs
- Developed and professionally maintained by embotech AG



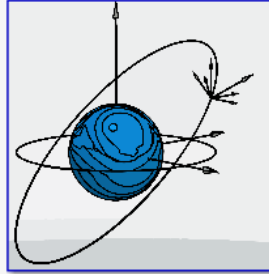
# FUNCTIONAL ENGINEERING SIMULATOR (DTV)



Physical\_Subsystems



Software\_Subsystems



Axes\_Transformations



Utility

## Legend

Light Blue	Physical Subsystem
Orange	Software Subsystem
Red	Input
Green	Output
Yellow	Constant
Dark Green	Mathematical Operation
Blue	Frame Conversion
Magenta	Logic Operation
Orange	WCA gain

An expandable simulation library built for INCAS' DTV

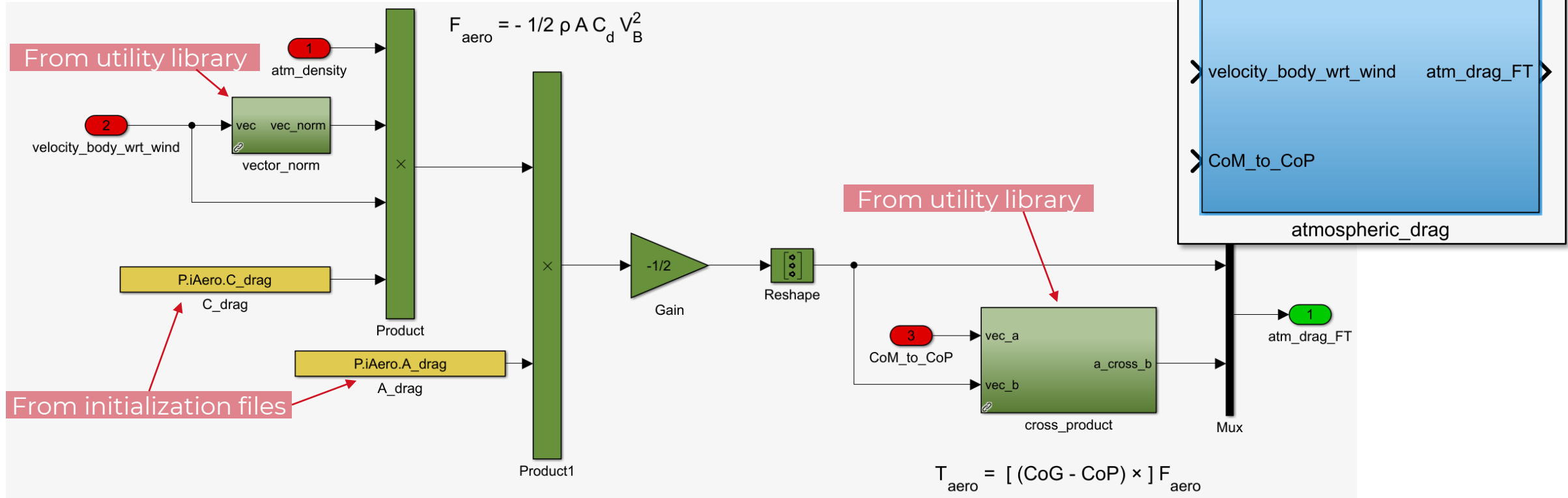
## Initialization files:

- mass properties
- propulsion system
- environment
- 

## Library blocks

## Simulators

# LIBRARY BLOCK EXAMPLE

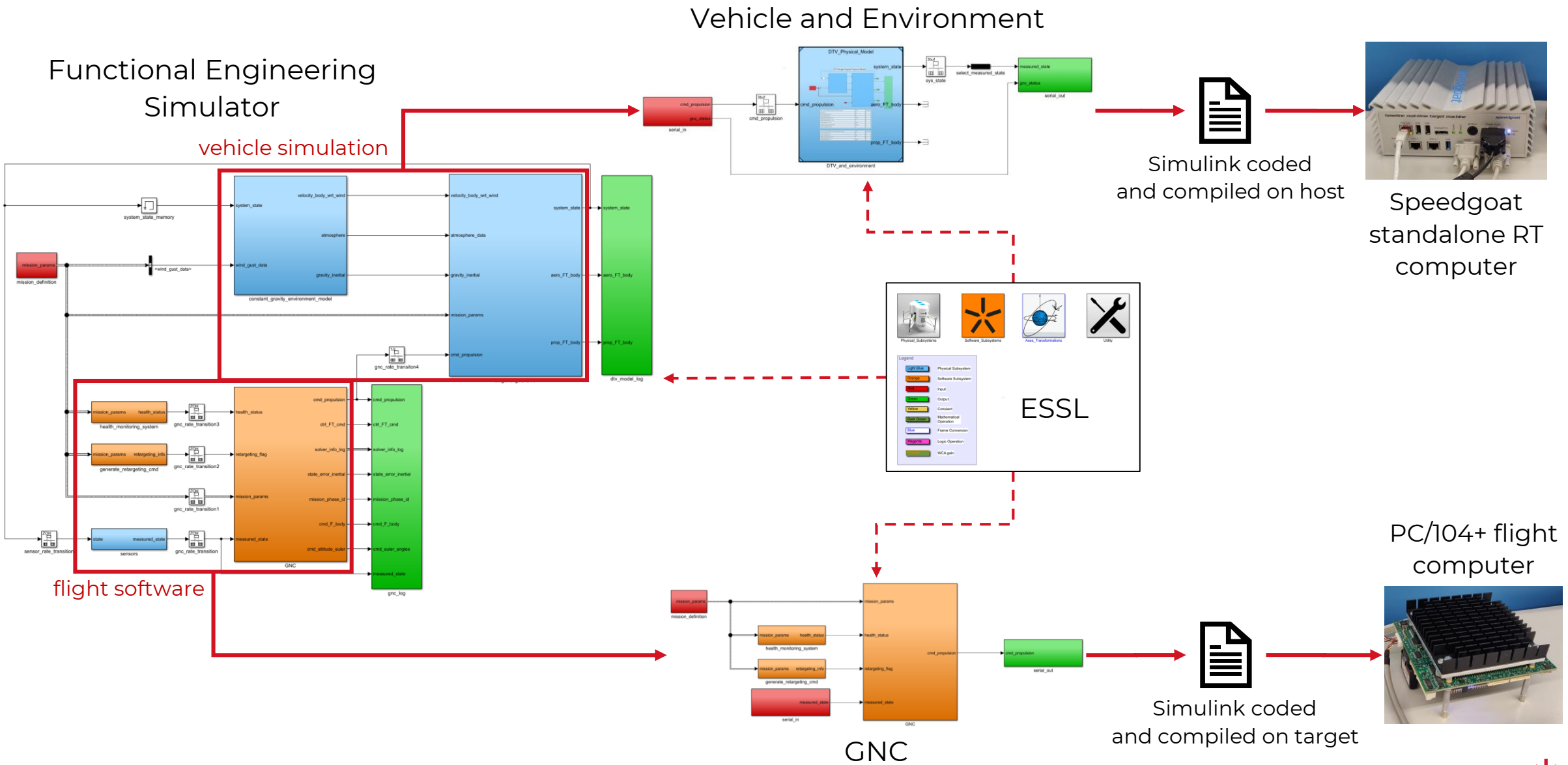


Input	Units	Dimension
Atmosphere Density	kg/m^3	1
Velocity wrt Wind (body)	m/s	3
Attitude Quaternion	-	4
Lever Arm (CoG - CoP)	m	3

Output	Units	Dimension
Aerodynamic Drag Force (body)	N	3
Aerodynamic Torques (body)	N*m	3

Parameters	Units	Dimension
Drag Coefficient	-	1
Cross Sectional Area	m^2	1

# SIMULATION ENVIRONMENTS

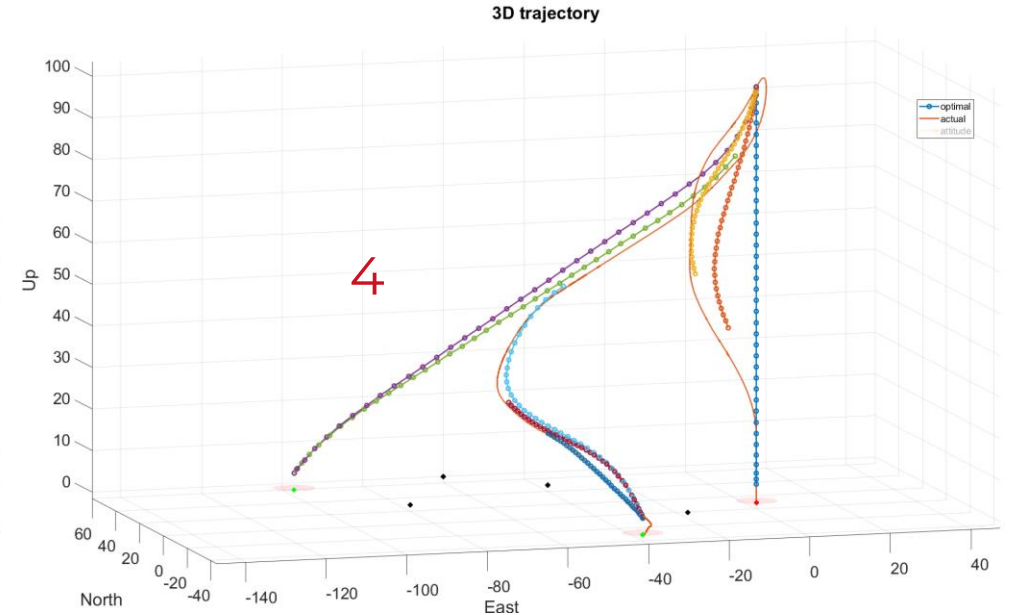
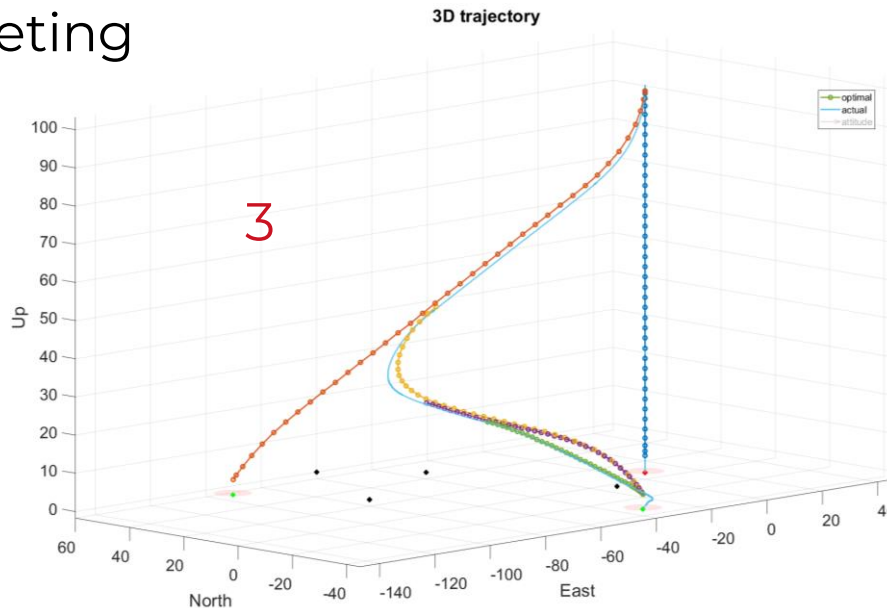
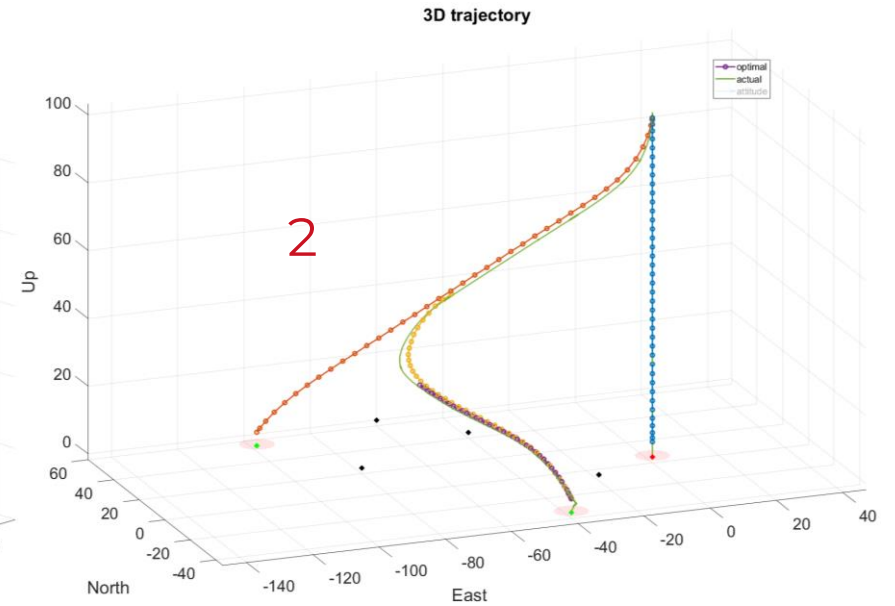
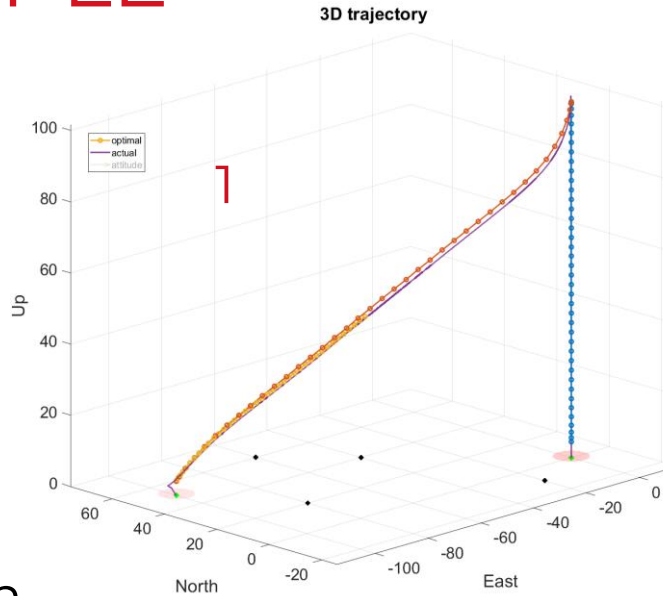


# SIMULATION EXAMPLE

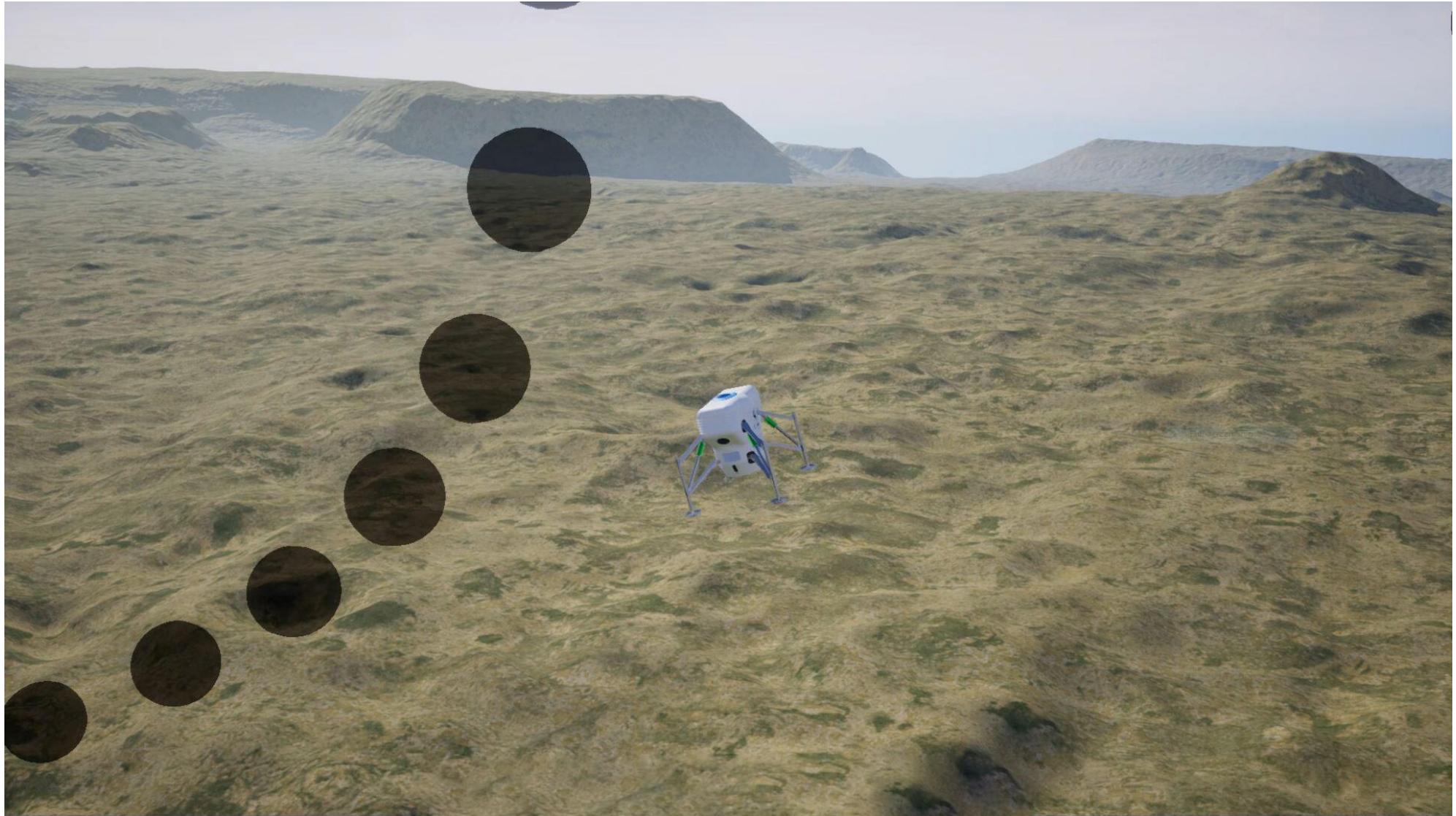
CPU	Median [s]	Max [s]	Min [s]
i7 8550U @ 1.8	0.07	0.15	0.04
Atom E3845 @ 1.9	0.25	0.55	0.19

1. Nominal end-to-end mission
2. Mid-flight retargeting
3. Engine fault
4. Wind on ascent

- Takeoff pad
- Landing pad
- Emergency pad

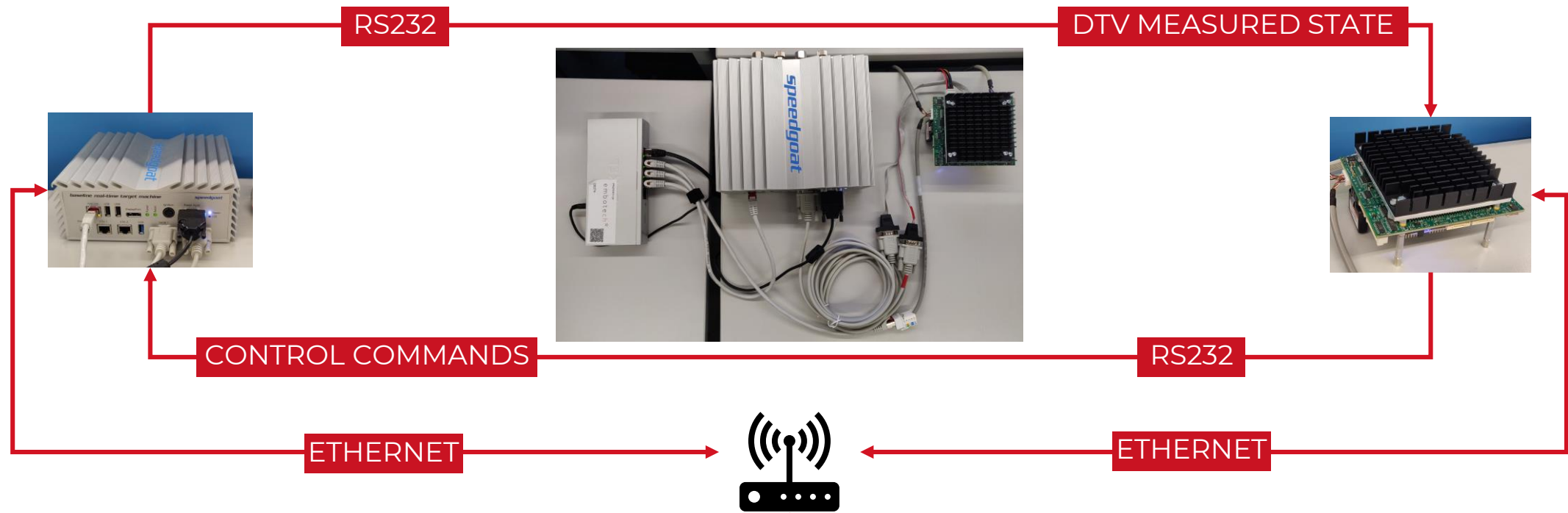


# END-TO-END VTOL MISSION



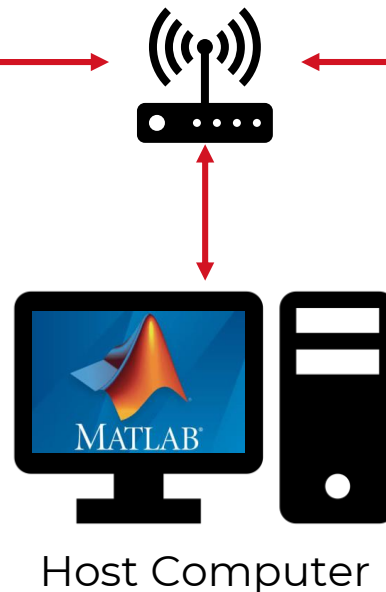
<https://youtu.be/srjEs1iFxl8>

# SOFTWARE VALIDATION FACILITY



## Key Features:

- PC/104+ & Speedgoat connected using two different serial cables;
- Communication between PC/104+ & Speedgoat at 25 Hz;
- Speedgoat & PC/104+ connected to the local embotech's network via Ethernet;
- Host computer accesses PC/104+ via SSH;
- Host computer accesses Speedgoat via Simulink Real-Time Explorer.

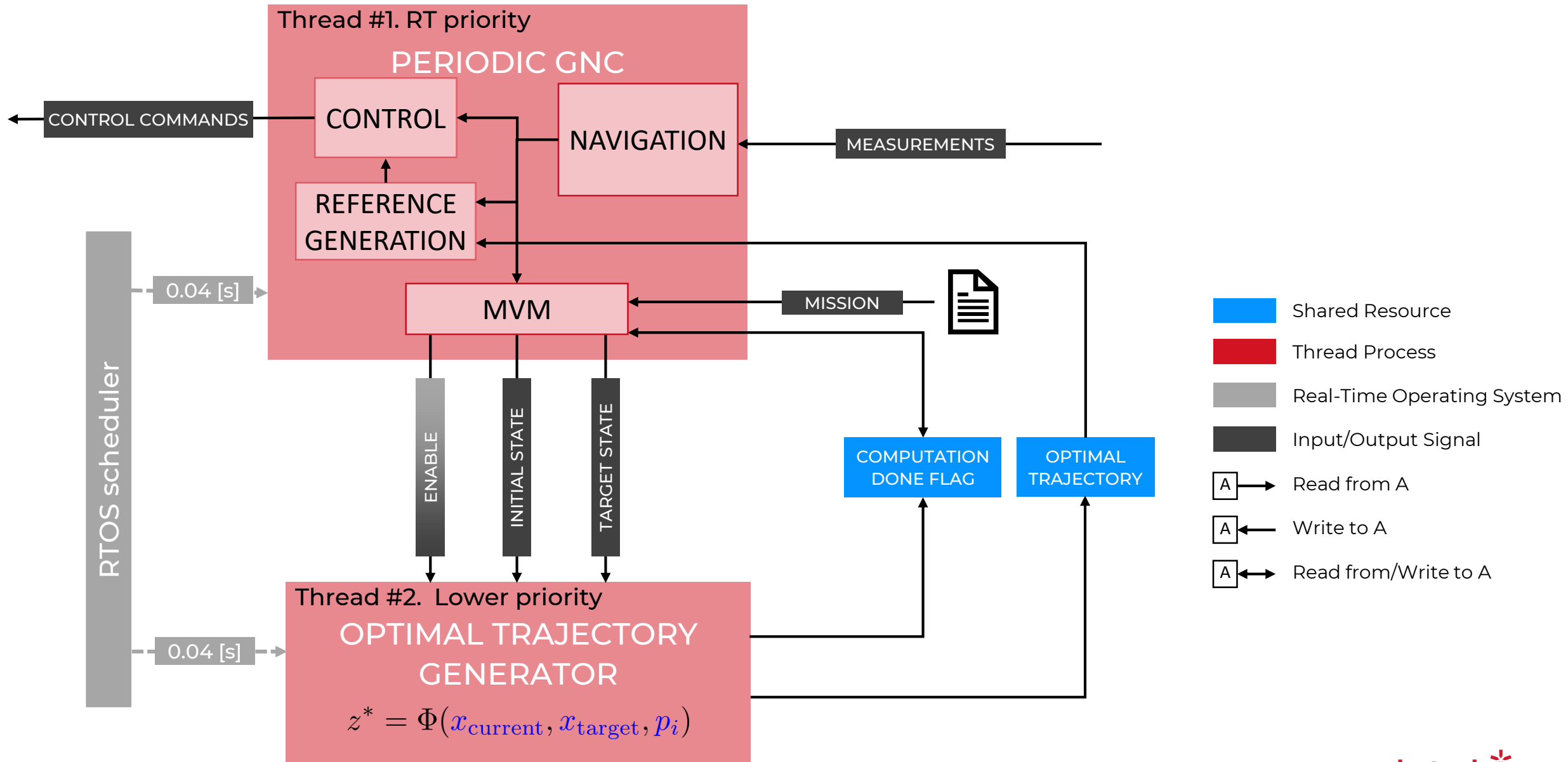


## Host Computer Tasks:

- Code generation;
- Code loading into Speedgoat & PC/104+;
- Processes launch;
- Data log recovery;
- Results plotting & analysis.

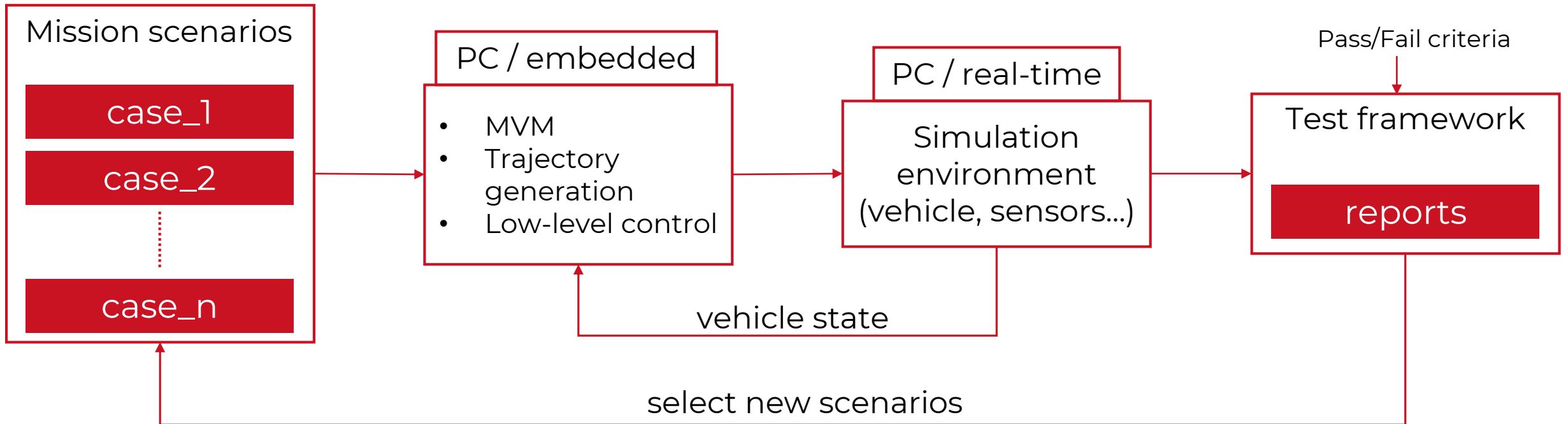


# REAL-TIME FLIGHT SOFTWARE



# FLIGHT SOFTWARE QUALIFICATION

- Functional validation campaign
  - 2576 scenarios simulated under *nominal*, *robust* and *fault* conditions
  - Sensitivity analysis w.r.t. noise and dispersion
- Software validation campaign
  - Subset of scenarios necessary for full code coverage



# CONTINUOUS INTEGRATION

## Summary Test Data

### Statistical data

- Landing error:
  - Average = 0.33444
  - Median = 0.28023
  - Maximum = 0.87238
  - Minimum = 0.022803
- Vertical velocity at landing:
  - Average = -0.4777
  - Median = -0.48024
  - Maximum = -0.40606
  - Minimum = -0.55762
- Horizontal velocity at landing:
  - Average = 0.12794
  - Median = 0.12671
  - Maximum = 0.28195
  - Minimum = 0.0090332
- Tilt angle at landing:
  - Average = 0.18689
  - Median = 0.20057
  - Maximum = 0.39637
  - Minimum = 0.0226
- Angular rate norm at landing:
  - Average = 0.053015
  - Median = 0.039726
  - Maximum = 0.46695
  - Minimum = 0.0070554

## MATLAB® Test Report

Timestamp: 06-Jun-2019 08:57:22

Host: Jenkins-ESA

Platform: win64

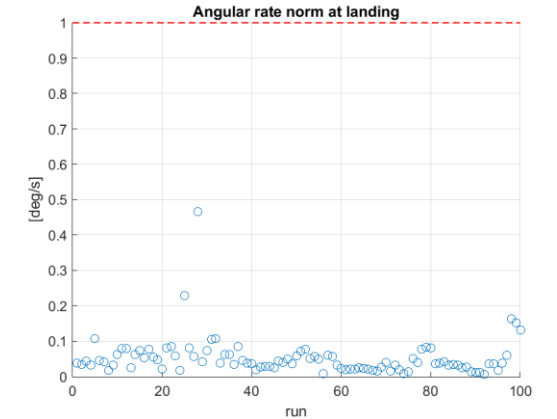
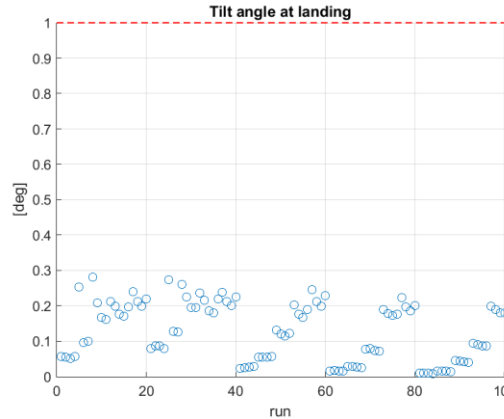
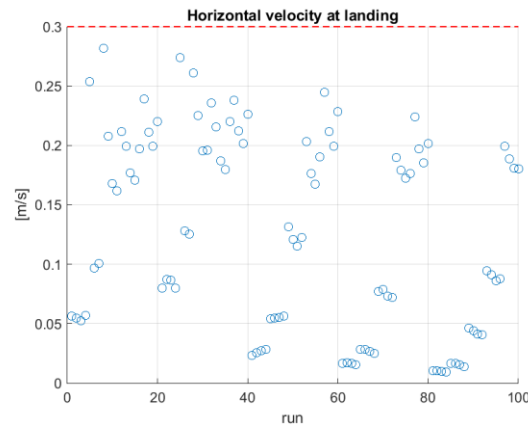
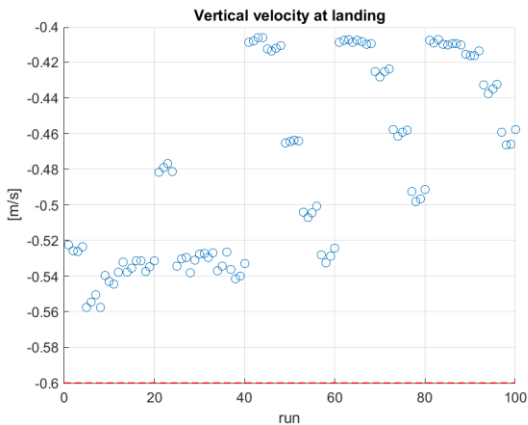
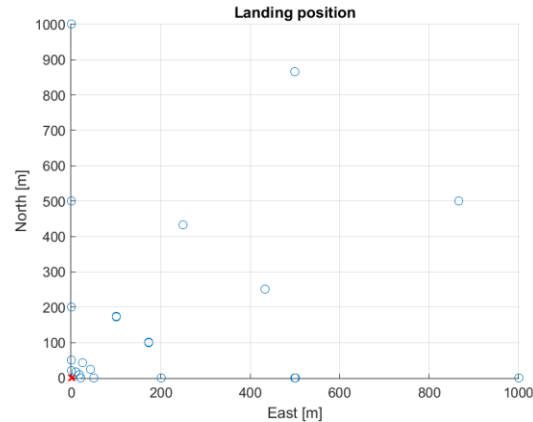
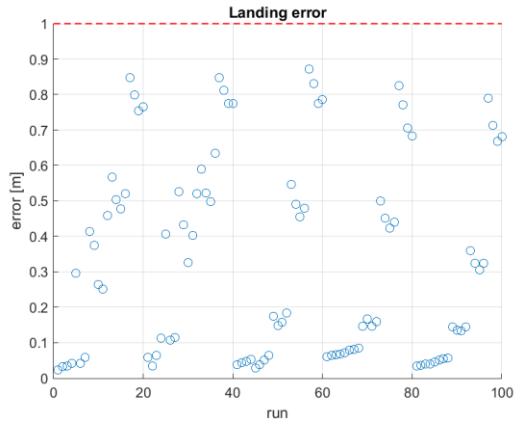
MATLAB Version: 9.4.0.949201 (R2018a) Update 6

Number of Tests: 100

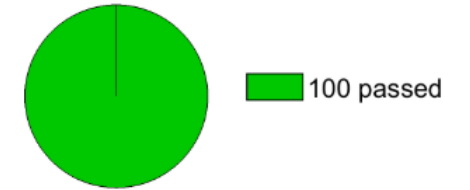
Testing Time: 901.6306 seconds

Overall Result: PASSED

Summary plots



Report generation after every batch of tests



# CONCLUSION



SpaceX

**Problem 1 : 3-DoF, Non-Convex, Continuous-Time, Free-Final-Time Minimum-Fuel Problem**

Cost Function

$$\underset{t_f, \mathbf{T}_B(\cdot)}{\text{minimize}} \int_{t_0}^{t_f} \|\mathbf{T}_B(t)\| + \lambda_1 \|\dot{\mathbf{T}}_B(t)\|^2 + \lambda_2 \eta(t)^2 dt \quad (1)$$

subject to:

Boundary Conditions

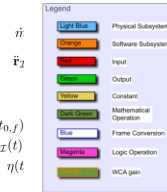
$$m(t_0) = m_0$$

$$\mathbf{r}_Z(t_0) = \mathbf{r}_{Z,0}$$

$$\dot{\mathbf{r}}_Z(t_0) = \dot{\mathbf{r}}_{Z,0}$$



Point-mass Dynamics



State Constraints

$$\mathbf{e}_1 \cdot (\mathbf{r}_Z(t) - \mathbf{r}_Z(t_{a,f}))$$

$$\|\dot{\mathbf{r}}_Z(t)\|$$

$$\eta(t)$$

Control Constraints

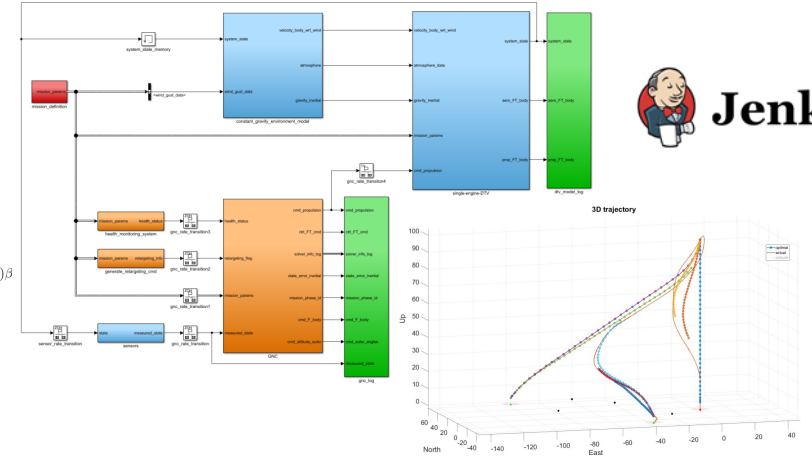
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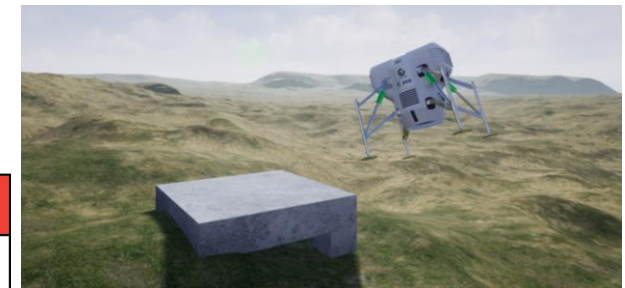
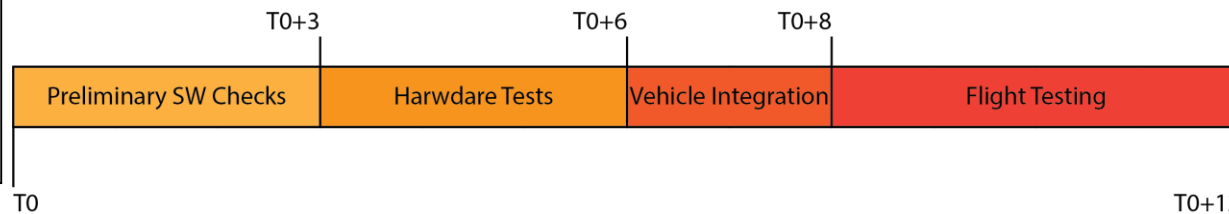
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## Design – Simulation – Validation



## Flight Testing on INCAS DTV, Q3 2019





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