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Space Weather Modelling Workshop 2023 ESA/ESOC

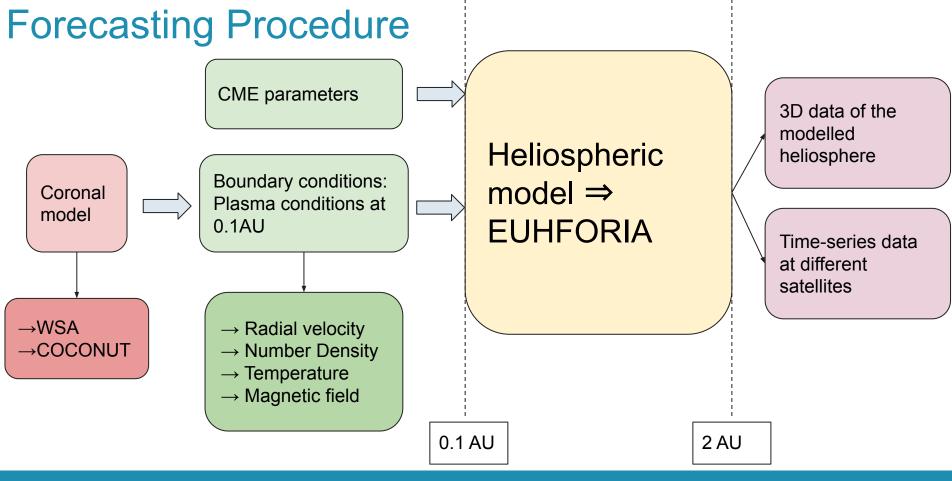










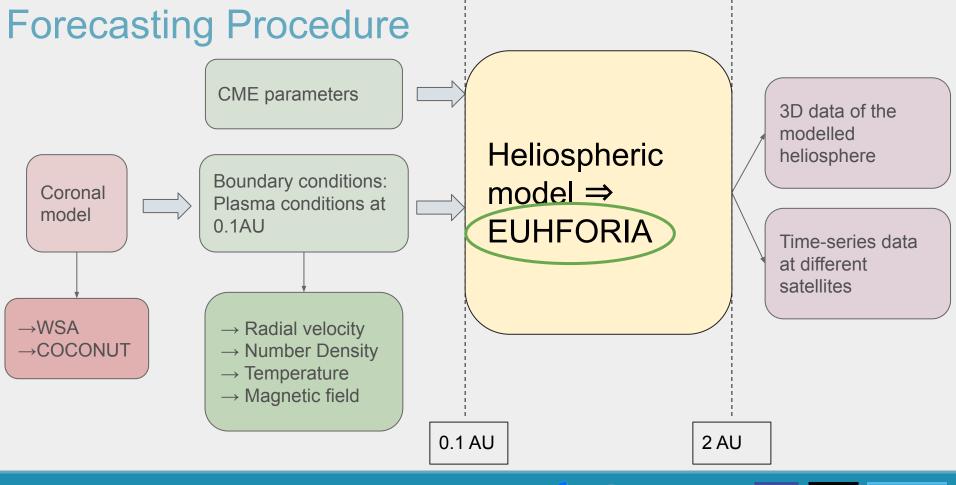














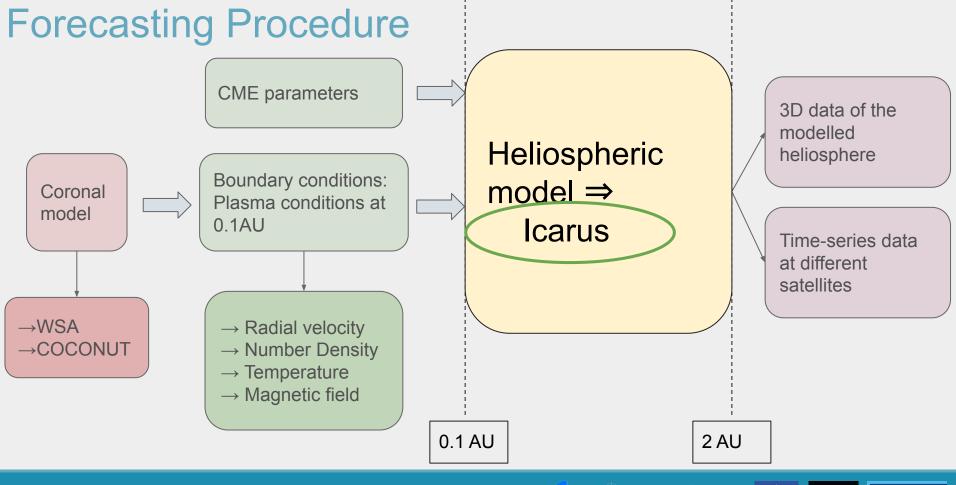


















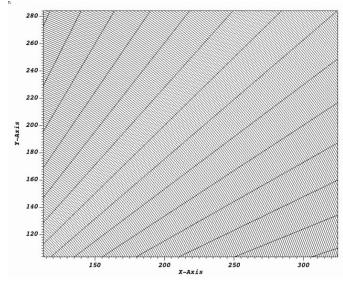




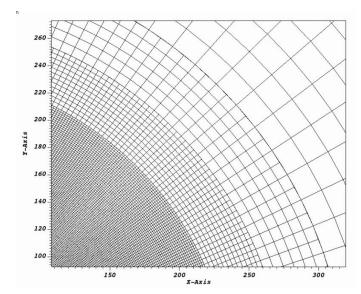


#### Motivation

- Operational perspective
  - Optimization (grid stretching & Adaptive Mesh Refinement) in Icarus ⇒ CPU time
     saved



Equidistant grid



Stretched grid with AMR











#### **Motivation**

- Operational perspective
  - Optimization (grid stretching & Adaptive Mesh Refinement) in Icarus ⇒ CPU time saved
- Physics perspective
  - Better capturing of CIRs or CIR shocks or CMEs or CME shocks (via AMR)











#### Icarus model

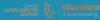
Implemented in the framework of MPI-AMRVAC (Xia et al., 2018)

- MPI-AMRVAC is a parallel adaptive mesh refinement framework (in FORTRAN)
- Solves (primarily hyperbolic) partial differential equations
- Ideal MHD module

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abla \cdot (
ho \mathbf{v}) &= 0, \ rac{\partial (
ho \mathbf{v})}{\partial t} + 
abla \cdot \left( 
ho \mathbf{v} \mathbf{v} + p_{tot} \mathbf{I} - \mathbf{B} \mathbf{B} 
ight) - 
ho \mathbf{g} &= \mathbf{F}, \ rac{\partial e}{\partial t} + 
abla \cdot \left( e \mathbf{v} + p_{tot} \mathbf{v} - \mathbf{B} (\mathbf{B} \cdot \mathbf{v}) 
ight) &= \mathbf{v} \cdot \mathbf{F} + 
ho \mathbf{v} \cdot \mathbf{g}, \ rac{\partial \mathbf{B}}{\partial t} + 
abla \cdot \left( \mathbf{v} \mathbf{B} - \mathbf{B} \mathbf{v} 
ight) &= 0, \ 
abla \cdot \mathbf{B} &= 0, \end{aligned}$$

Equidistant grid	$\begin{array}{c} \textbf{Resolution} \\ [\textbf{R}_{\odot},  \textbf{DEG},  \textbf{DEG}] \end{array}$	
Low	[1.37, 3.75, 3.75]	
Middle	[0.685, 1.875, 1.875]	
High	[0.3425, 0.9375, 0.9375]	











#### Icarus vs. EUHFORIA

	Icarus	EUHFORIA
Numerical Domain	R: $0.1AU \rightarrow 2AU$ $\phi: 0^{\circ} \rightarrow 360^{\circ}$ $\theta: -60^{\circ} \rightarrow 60^{\circ}$	R: $0.1AU \rightarrow 2AU$ $\phi: 0^{\circ} \rightarrow 360^{\circ}$ $\theta: -60^{\circ} \rightarrow 60^{\circ}$
Coordinate system	Co-rotating	HEEQ
Computational Grid	Uniform; Radially Stretched; Adaptive Mesh Refinement (AMR)	
MHD Solver	Finite Volume	FV with Constrained transport

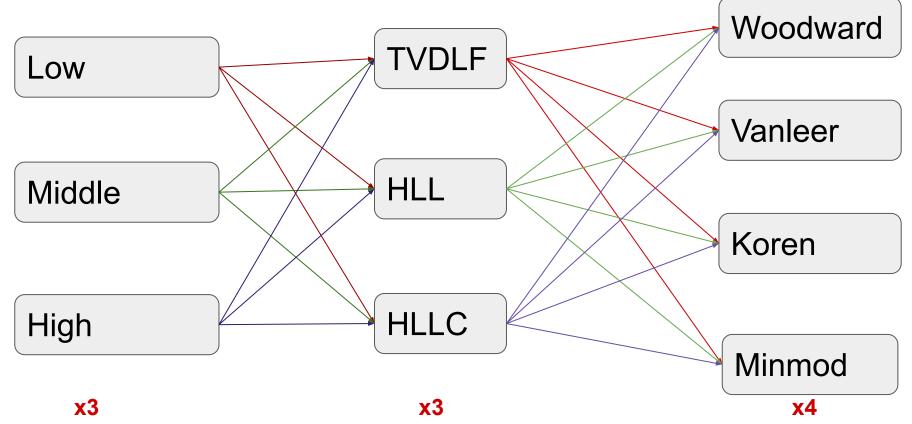








#### **Schemes and Limiters**









#### **Schemes and Limiters** Woodward **TVDLF** Low Vanleer 36 simulations Middle Koren HLLC High Minmod **x3 x3 x4**











#### **Schemes and Limiters** Woodward **TVDLF** Low **TVDLF + WOODWARD:** Vanleer Middle **Sharpest Fastest** Koren HLLC High Minmod

**x3** 







**x4** 

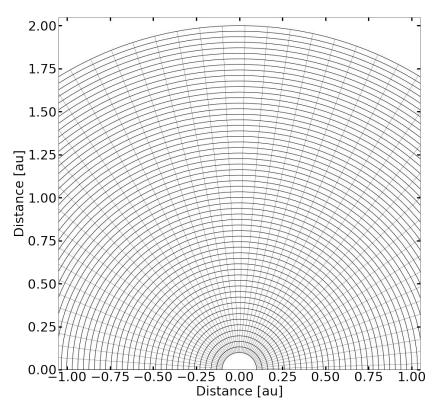




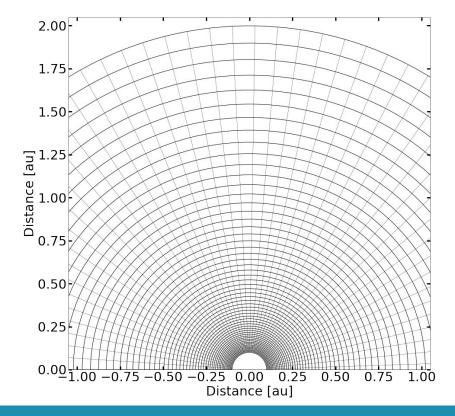
**x3** 

#### Advanced techniques: Grid Stretching

Non-stretched grid N=60.



#### Stretched grid N=60.













## Advanced techniques: Adaptive Mesh Refinement

- Refinement applied to the blocks of cells
- 1 level of refinement difference between the adjacent blocks
- Implemented condition controls the refinement in the domain

Higher resolution in the domain only where necessary.





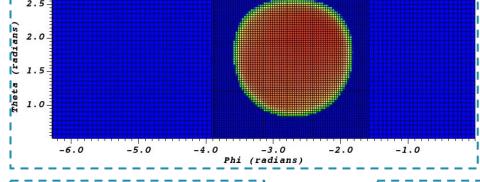




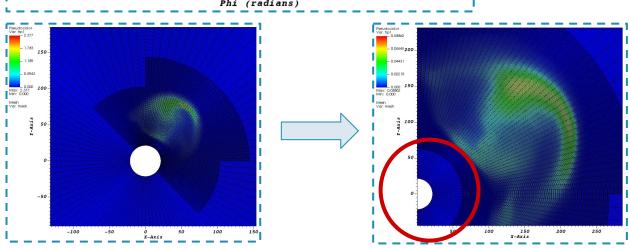


#### Advanced techniques: AMR

Inner boundary slice



**Equatorial plane** 













#### AMR (uniform) - CIR refinement

$$\phi = \phi_0 + rac{r-r_i}{U} st \Omega$$

φ - the longitude that needs to be refined,

 $\phi_0$  and  $\mathbf{r}$  - the coordinates of a point

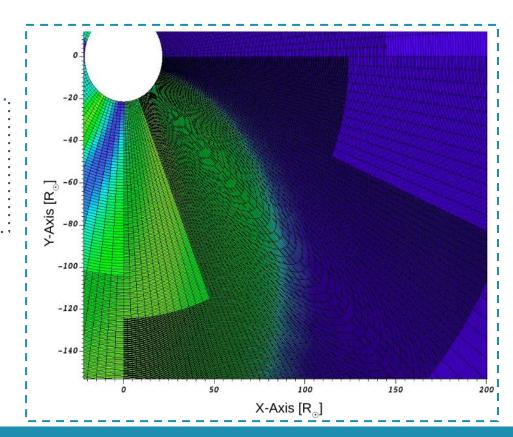
 $\mathbf{r}_1 = 0.1 \mathrm{AU}$ 

**U** - the characteristic speed of the fast stream

 $\Omega$  - the rotation rate of the Sun.

$$\phi_{lower} < \phi < \phi_{upper}$$

**Aimed for SEPs** → **PARADISE** 













## AMR Equidistant - Tracing function

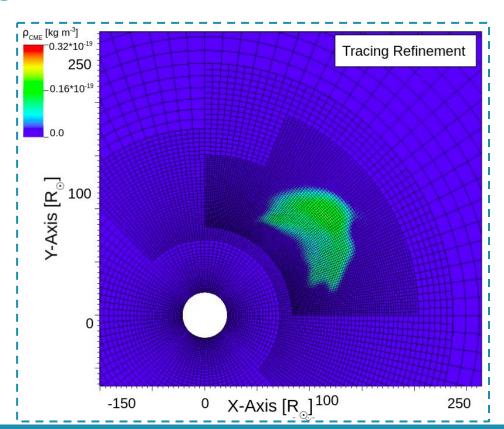
Tracing function  $F_{TR}$ :

If CME is present  $\rightarrow F_{TR} =$ 

 $\rho_{CME}$ If CME is NOT present  $\rightarrow F_{TR} = 0$ 

Criterium:  $F_{TR} > 0$ 

**Aimed for complex CME interior** 



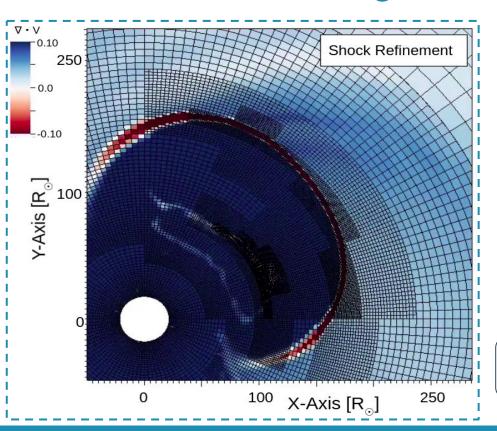








#### AMR on a stretched grid: Shock function



Refinement according to the compressed regions in the domain

Criterium:  $abla \cdot V < 0$ 

Aimed for estimation for arrival time, strength









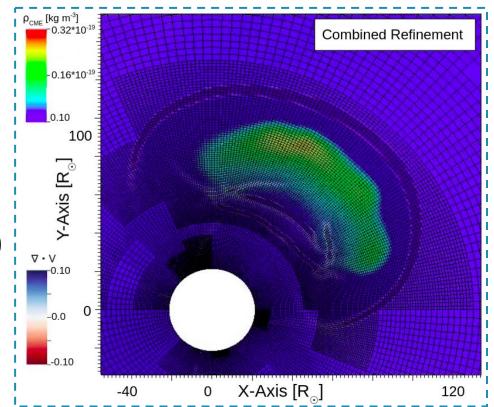


#### AMR Equidistant - Combined criterion

Refinement is applied when the CME or the shock is present in the domain

Criterium: $F_{TR} > 0 \& div(V) < 0$ 

Aimed for full evolution





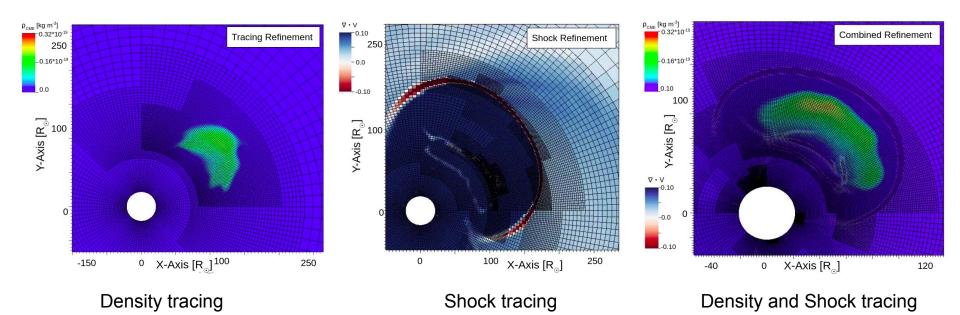








#### Advanced techniques: AMR + Grid Stretching



Baratashvili et al. 2022







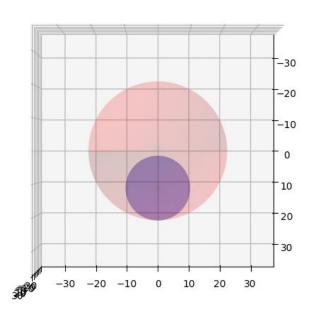


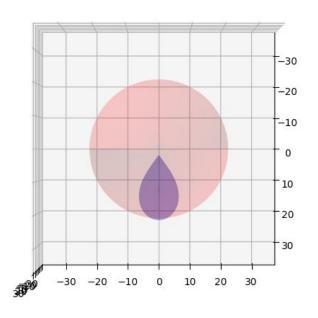


#### Spheromak



#### Stretched Spheromak







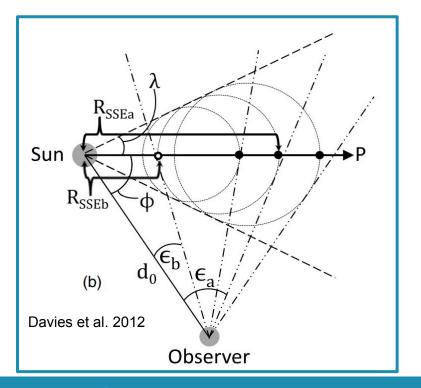








Spheromak ⇒ Self-Similar evolution













Spheromak ⇒ Gibson & Low model (Gibson & Low model (Gibson & Low, 1998)

A realistic flux-rope model

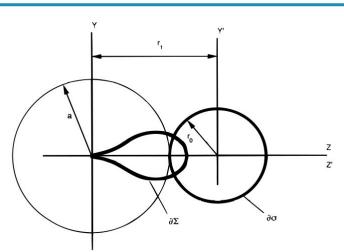


Fig. 5.—Limiting case  $a=r_1-r_0$ , where the leftmost point of the circle is mapped exactly onto the origin. The mathematical stretching transformation takes a circle  $\partial \sigma$  that is located in the Y-Z plane, of radius  $r_0$ , and displaced a distance  $r_1$  from the origin, and maps it to the tear-shaped curve  $\partial \Sigma$ . This contraction "stretches" the space r>a radially inward, under the transformation  $r\rightarrow r-a$  (any points r<a are collapsed onto the origin).











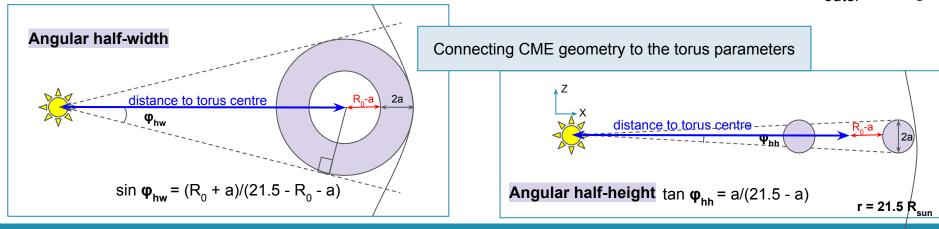
Spheromak







Inner radius:  $R_{inner} = 2R_{\odot}$ Outer radius:  $R_{outer} = 5R_{\odot}$ 

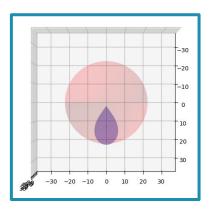


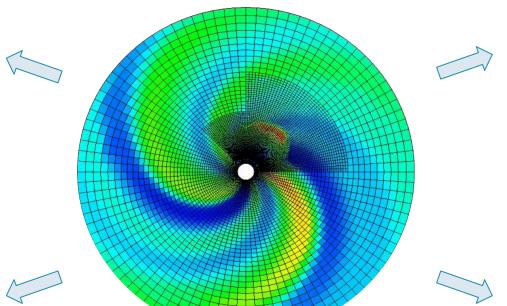




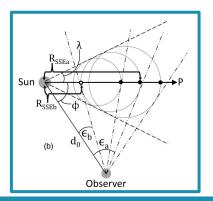


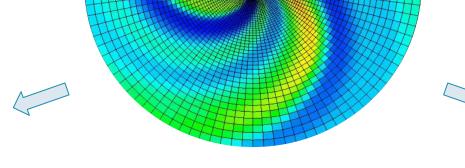












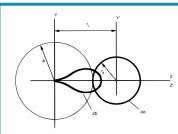


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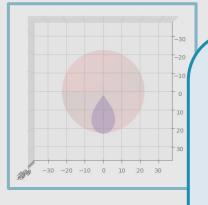












## Sun $R_{SSEb}$ $\Phi$ $(b) d_0 \in b \in a$

# Validation with different case studies



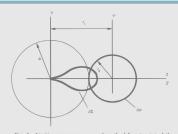


Fig. 5—Limiting case  $a=r_1-r_0$ , where the leftmost point of the circle is mapped exactly onto the origin. The mathematical stretching transformation takes a circle  $\partial\sigma$  that is located in the Y-Z plane, of radius  $r_0$ , and displaced a distance  $r_1$  from the origin, and maps it to the tearshaped curve  $\partial\Sigma$ . This contraction "stretches" the space r>a a radially inward, under the transformation  $r\rightarrow r-a$  (any points r< a are collapsed onto the origin,













## Speed up

	Icarus (Middle) Equidistant	Icarus Stretched NO AMR	AMR 2	AMR 3	AMR 4
Wall-clock times	7h 44m	0h 8m	0h 15m	0h 35m	3h 40m

Simulations are performed on 1 node only (with 36 CPUs) on the Genius cluster at the Vlaams Supercomputing Centre.

Middle equidistant in EUHFORIA ~ 18h

#### **Speed up factors**

	Icarus	EUHFORIA
AMR 3	13.2	30.8
AMR 4	2.1	4.9











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First phase: maintained within MPI-AMRVAC repository ⇒ open-source and publicly available to everyone











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- Being integrated within VSWMC
  - Along with EUHFORIA heliospheric model
  - User-friendly GUI interface











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  - User-friendly GUI interface
- In chain with different coronal models
  - WSA
  - COCONUT











- Flexible Grid
  - Stretching
  - AMR
- Different numerical schemes + limiters available











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Faster results











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**Faster** results

Saved computational resources











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**Faster** results

Saved computational resources

Access to more in-depth research!









Flexible Grid Stretc **AMR** Different Thank you! Access to Saved **Faster** computational more in-depth results research! resources









