

# Tip & Cue AIS-Assisted Gaussian Process Regression for Ship Dynamics Modeling and Cognitive SAR Tasking

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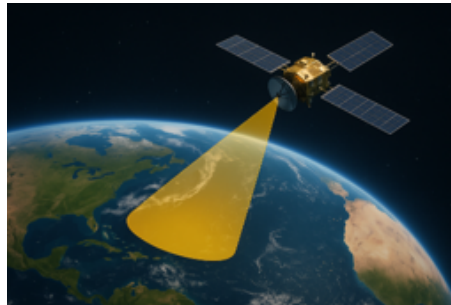


# Motivations and Challenges

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## *Motivations*

- Maritime surveillance as application scenario for Cognitive SAR design
- AIS data for vessel selection and trajectory fitting
- Tip & Cue enables extended monitoring period



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## *Challenge*

- Fit vessel track with sparse AIS messages and observability gap

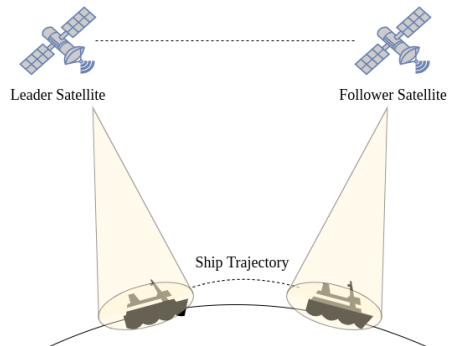


# Tip & Cue Framework

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Tip & Cue involves cooperation among satellites

- Leader satellite selects Area of Interest (*Tip*)
- Follower satellite focuses on selected area (*Cue*)
- Surveillance and emergency response applications



# Tip & Cue Framework

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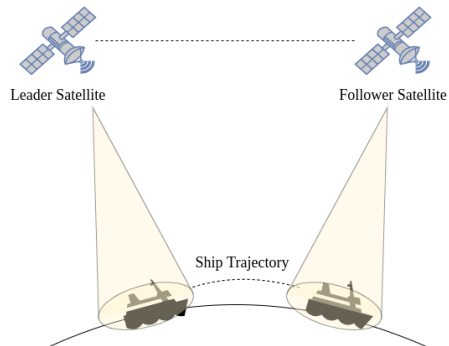
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*Pros:* Extended monitoring of target of Interest

*Cons:* Non-observability period of target of Interest

*Received AIS data to fit overall trajectory*



# AIS Data

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AIS data are

- Provided by cooperative vessels to share their status
- Divided into static and kinematic informations

*Static data*: fixed information over time (vessel type, country of origin...)

*Kinematic data*: information that may change over time

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*Kinematic data:* information that may change over time

*Kinematic AIS data useful for trajectory fitting*

ID	UNIX Times- tamp	Longitude	Latitude	Heading	Speed	Course
2f0f2613	1524381344000ms	23.6deg	37.96deg	167deg	0kn	167deg

# Gaussian Process Regression

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*Gaussian Process*: collection of variables, any finite number of which have a joint Gaussian distribution

A GP is completely define by its *mean function*  $m(x)$  and *kernel*  $k(x, x')$

$$f(x) \sim GP(m(x), k(x, x'))$$

with

$$\begin{aligned} m(x) &= \mathbf{E}[f(x)] \\ k(x, x') &= \mathbf{E}[(f(x) - m(x))(f(x') - m(x')))] \end{aligned}$$

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*The function  $f(x)$ , in this work, is the longitude and latitude time evolution*

# Gaussian Process Regression

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*Gaussian Process Regression*: a supervised learning problem

- Training dataset  $D = \{X, y\}$ : feature  $X$  (time instants) and label  $y$  (longitude / latitude)
- Goal: predict output  $f^*$  for new features  $X^*$

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Output  $f^*$  obtained by maximizing the Log-Marginal-Likelihood and with distribution

$$f^* \mid X, y, X^* \sim \mathcal{N}(\mu^*, \sigma^{*2})$$

where, for unseen time instant  $X$ :

- $\mu^*$  *mean value* of longitude/latitude
- $\sigma^*$  associated *standard deviation*

# Simulation Set-Up

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*Leader* and *Follower* spacecrafts

- AIS observability of 300s each
- Non-observability period of 500s between the two acquisitions
- Leader sends AIS messages via inter-satellite link

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- Freely available, real ground-based AIS dataset
- Only vessels with speed at least of 3kn and sending messages for at least 1100s considered
- Only 25% of available data used to simulate data packet loss

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*Kernel* employed: sum of Radial Basis Function and Dot Product

$$k(x, x') = k_{rbf}(x, x') + k_{dp}(x, x') = \sigma_f^2 \exp\left(\frac{-\|x - x'\|^2}{2l^2}\right) + \sigma_0^2 x \cdot x'$$

where GPR learns the length scale  $l$  and the variances  $\sigma_f^2$  and  $\sigma_0^2$

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# Results - Mean Absolute Error

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Fitting quality on both longitude and latitude evaluated in terms of *Mean Absolute Error*

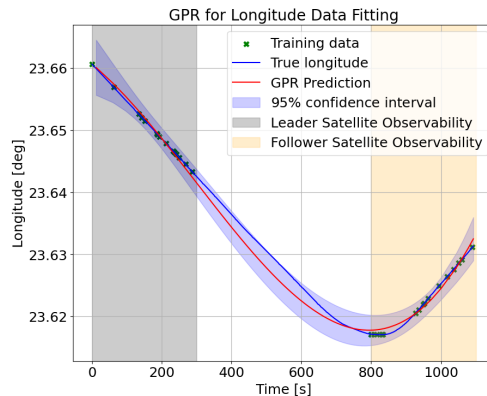
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	MAE Longitude	MAE Latitude
<b>Test Set</b>	0.00124deg	0.00102deg
<b>Non-Obs Test Set</b>	0.00167deg	0.00138deg



# Results - Confidence Interval

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Fitted output  $y^*$  lies in *Confidence Interval* if

$$y^* \in [\mu^* - \alpha\sigma^*, \mu^* + \alpha\sigma^*]$$

where  $\alpha$  depends on selected C.I.

Higher C.I.

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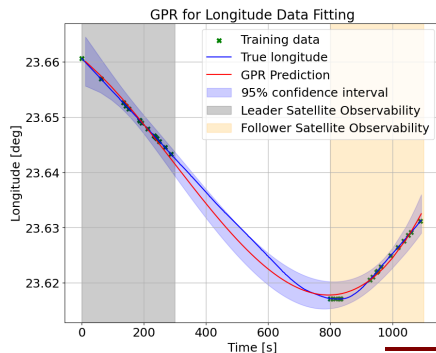
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	Longitude Test Data	Latitude Test Data
99%	88.19%	92.79%
95%	82.49%	87.28%
90%	77.80%	82.71%



# FPGA Porting

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*Gaussian Process Regression* algorithm porting

- Zynq UltraScale+ and Versal Edge FPGAs
- ZCU102 and VE2303 development kits
- VE2302 outperforms ZCU102

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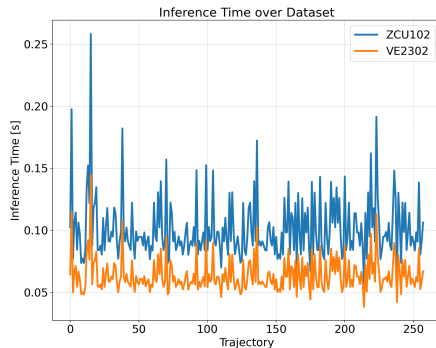
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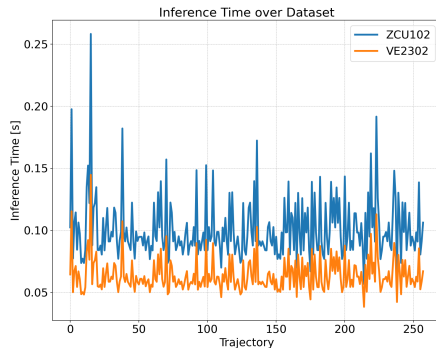
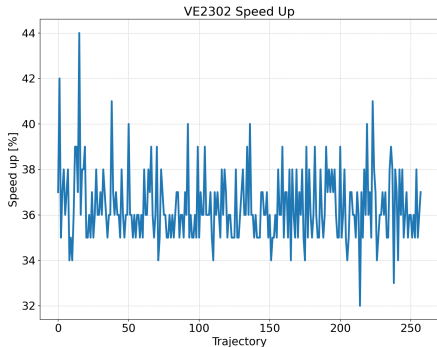


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# Conclusions

Tip & Cue as maritime surveillance set-up

Gaussian Process Regression applied to AIS data fitting

Fitting results in terms of Mean Absolute Error and Confidence Interval

Algorithm porting on two space-qualified FPGAs

